

# ARPES part I

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Ames Laboratory and Iowa State University





## Cliff G. Olson

(July 6th, 1942 - February 21st, 2009)

Stoughton- Clifford Gerald Olson died on Saturday February 21, 2009 at his home in the Town of Dunn at the age of 66. He was born July 6, 1942 in Long Prairie, MN to Clifford and Ethel Olson of Osakis, MN.

He is survived by his wife Donna M. Sansome Olson, whom he married in St. Paul, MN in 1965. He is further survived by a son, Allen (Melissa); a daughter Lynnette; a sister, Jean (Harlan) Chapman, of Schiocton, WI; two grandchildren, Alexander and Ella; and several nieces and nephews. Clifford went to Hamline University in St. Paul for his B.S. degree in 1964 and Iowa State University in Ames for his PhD in physics in 1970. He worked in solid state physics research for Ames Lab throughout his career, with his research being done at the Physical Sciences Lab in Stoughton. A large number of his projects were collaborations with scientists from throughout the United States, Canada, Korea and several European countries. He was awarded the Professional and Scientific Excellence Award in 1996 from Iowa State University. He found photography, woodworking and Donna's embroidery an escape from his research. A memorial service will be held on Thursday, February 26, 2009 at 11:00 am at the Olson Holzhuter-Cress Funeral Home in Stoughton, with Rev. Clyde Cross officiating, followed by a reception at the Stoughton American Legion Post #59 on North Page St. The family will greet friends at the Funeral Home on Wednesday from 5:00 to 7:00 pm. Memorials may be made in Clifford's name to Second Harvest, or to the charity of your choice.

# Outline:

## PART I

- Instrumentation
- Principles of ARPES technique
- Basic properties: band structure and Fermi surface and how to read the data

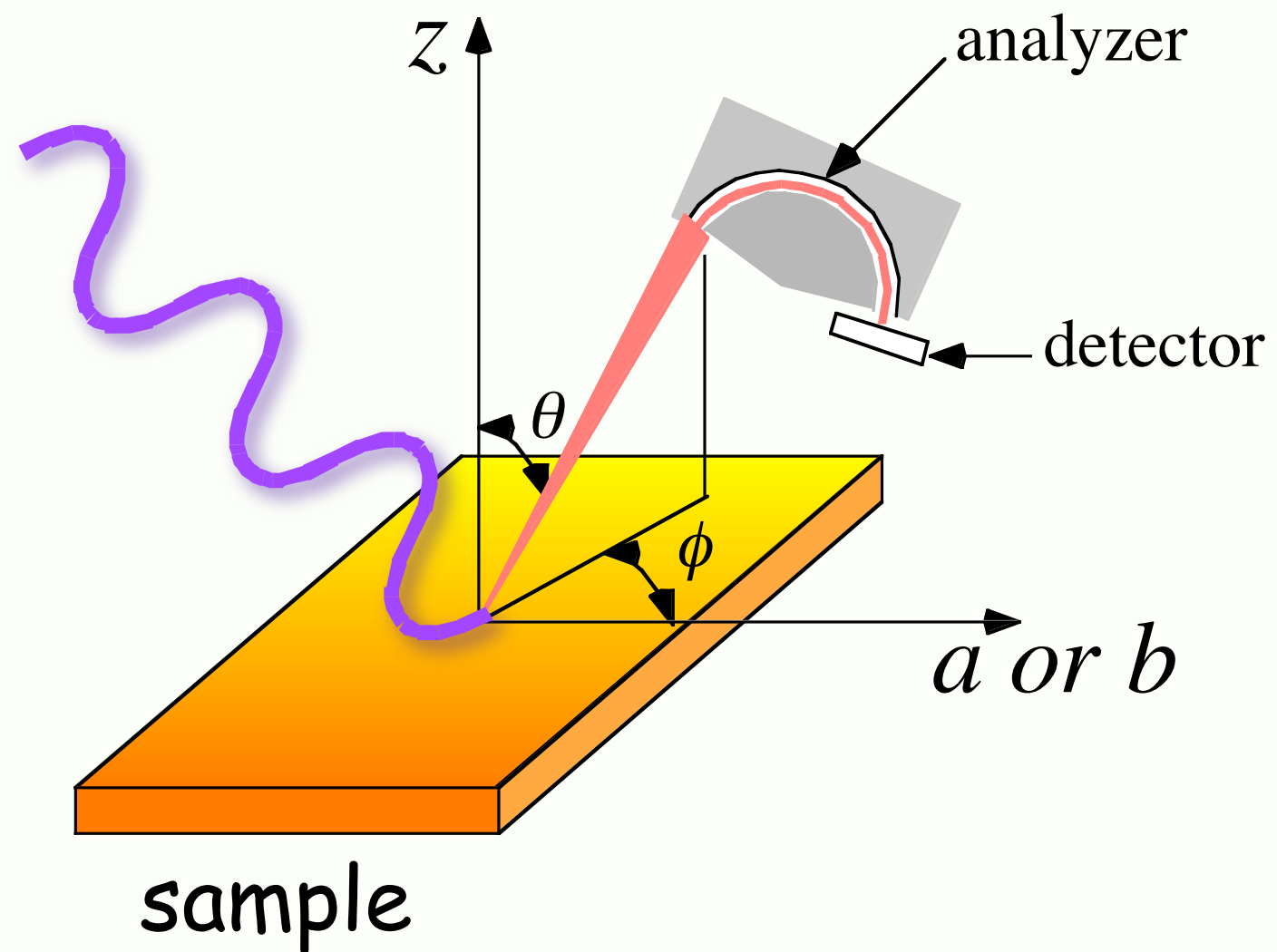
## PART II

Properties measured by ARPES: energy gaps, quasiparticle lifetime, collective modes

## PART III

Discussion of recent, interesting results: superconductivity, magnetism, charge density waves etc

# ARPES experiment





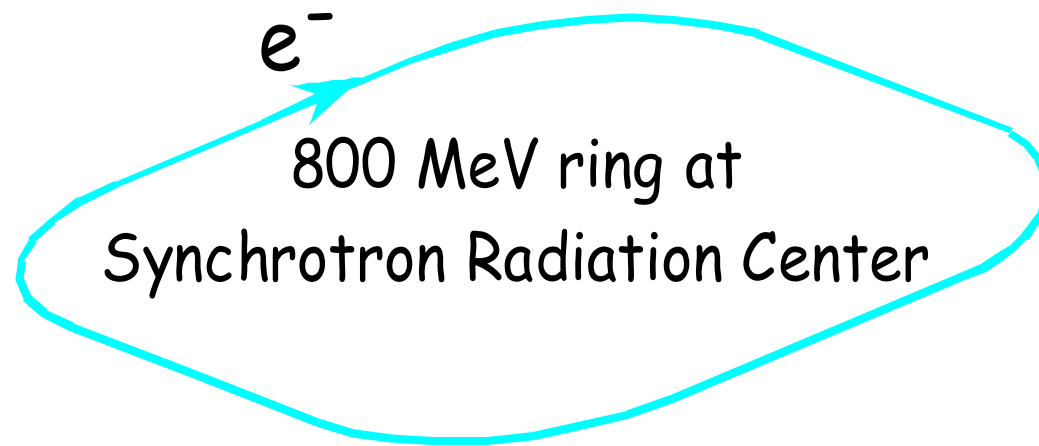
# Vacuum UV sources

Energy range: 7 eV - 1000 eV (or 1 nm to 240 nm).

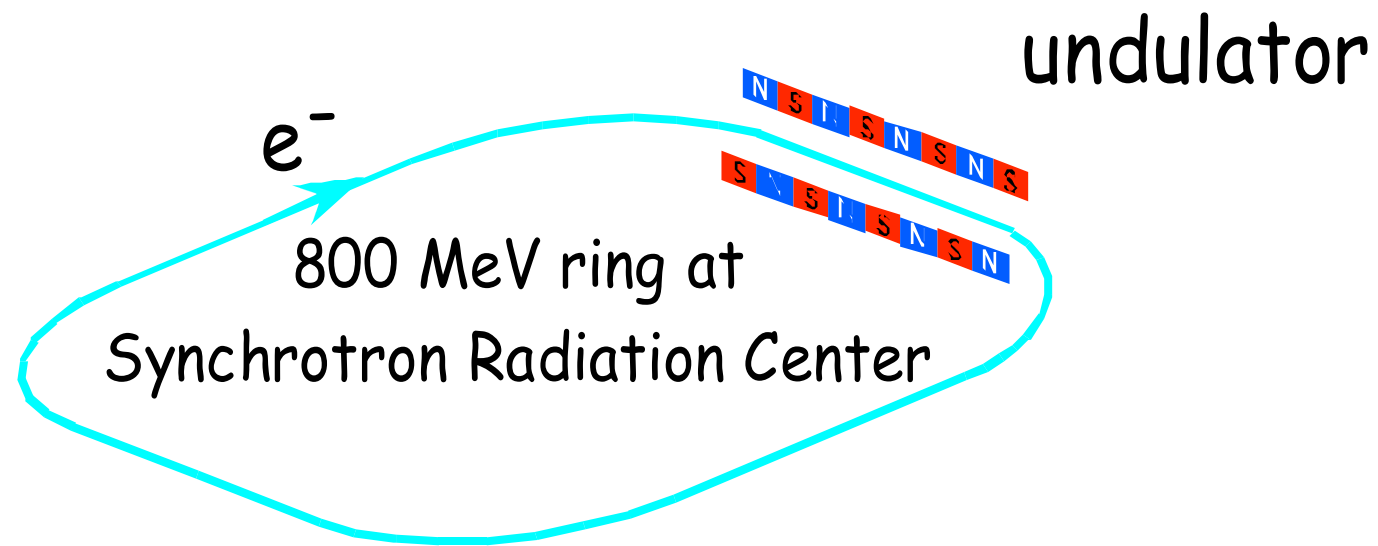
Photons in this energy range are easily absorbed in air with mean free path from few cm to less than 1 mm.

Monochromatic, tightly focused beams are required

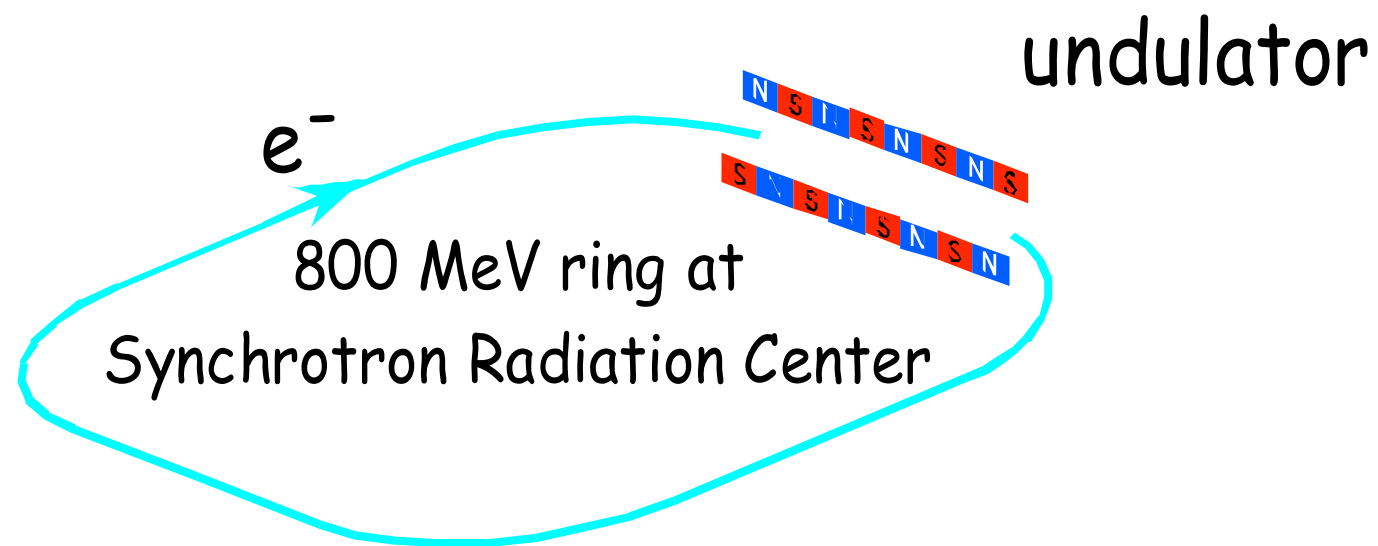
# VUV light from the synchrotron



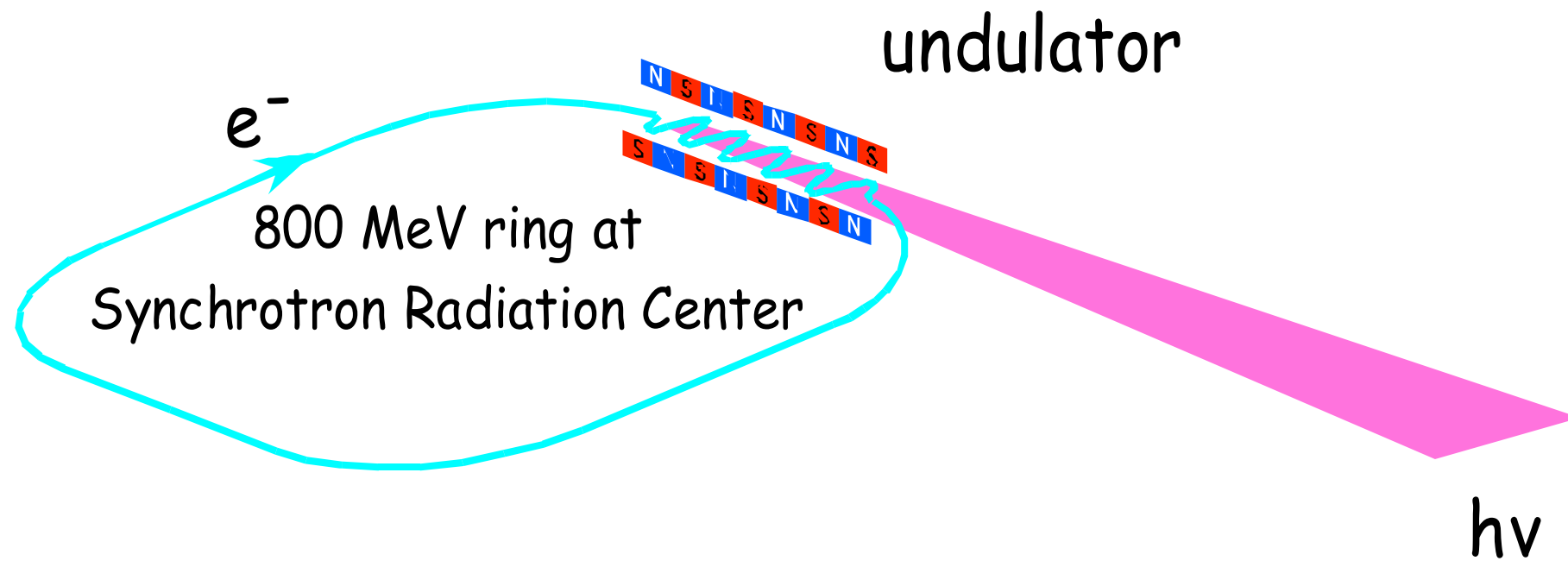
# VUV light from the synchrotron



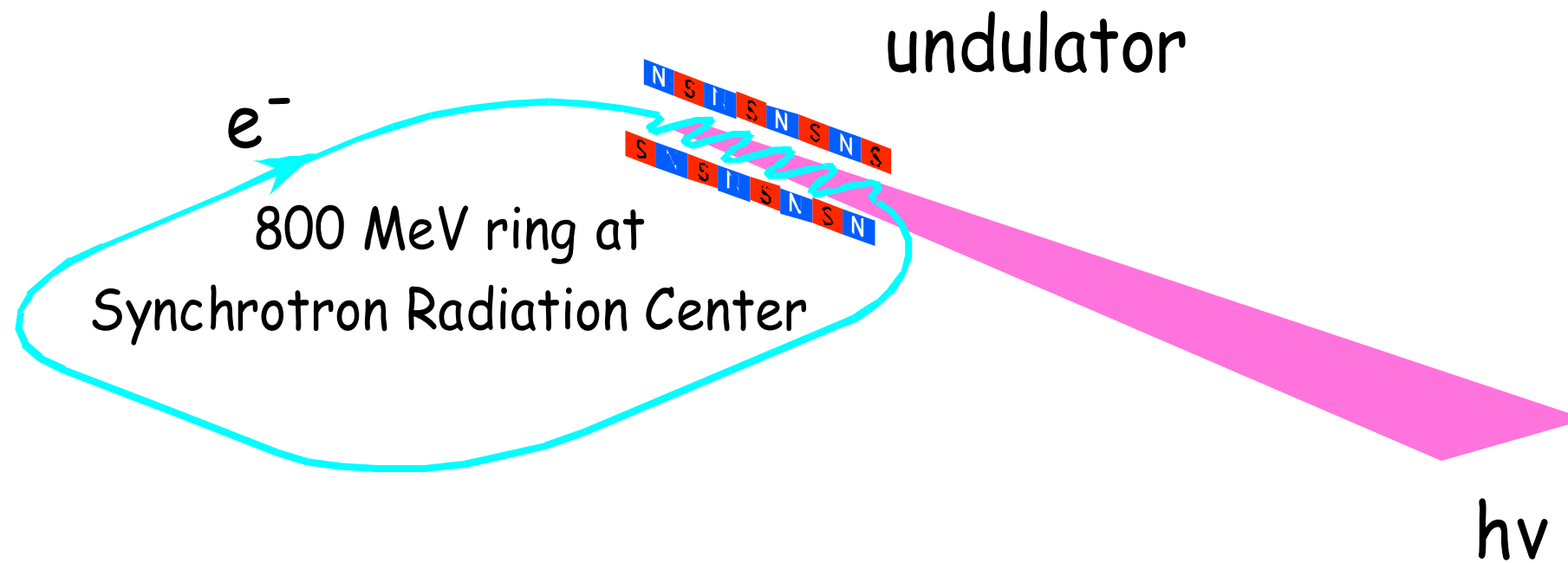
# VUV light from the synchrotron



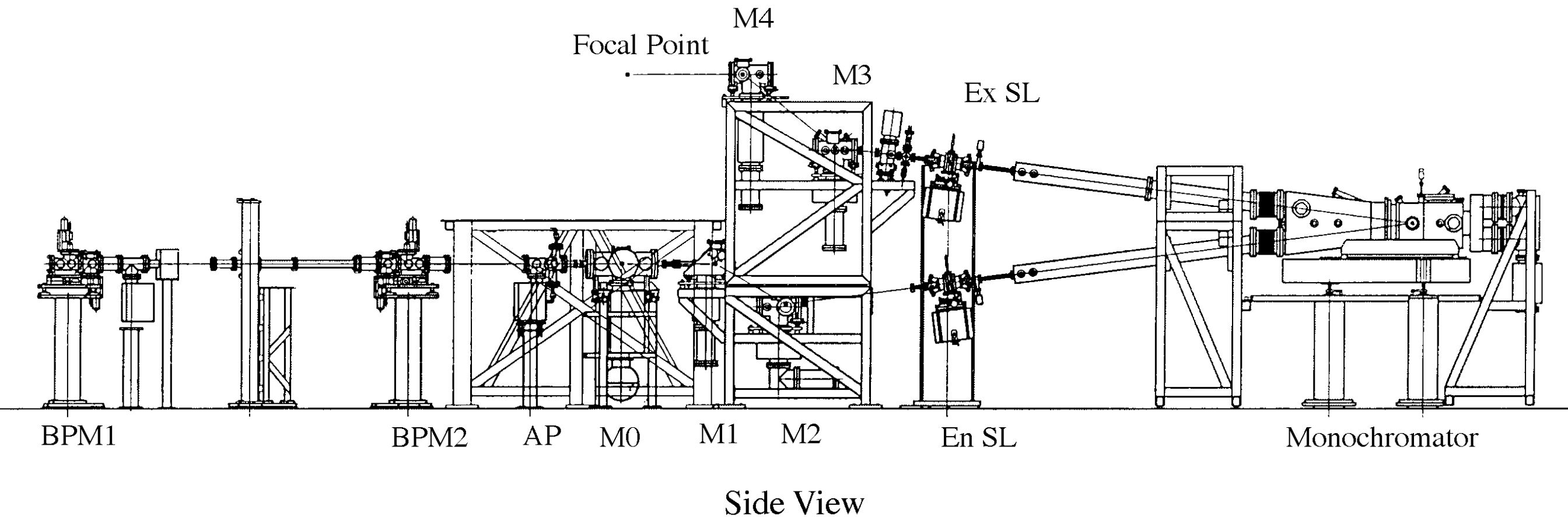
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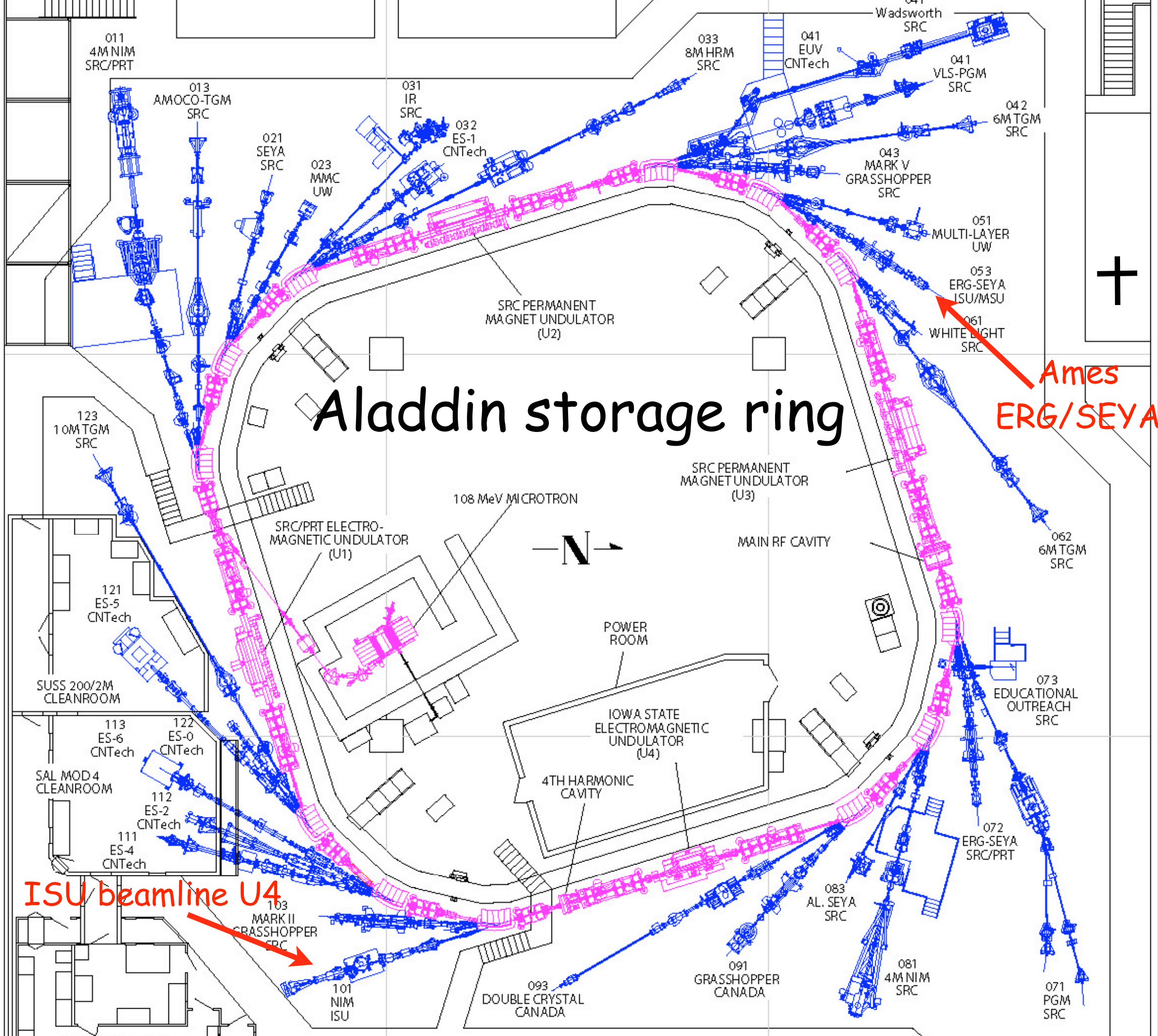


# VUV light from the synchrotron



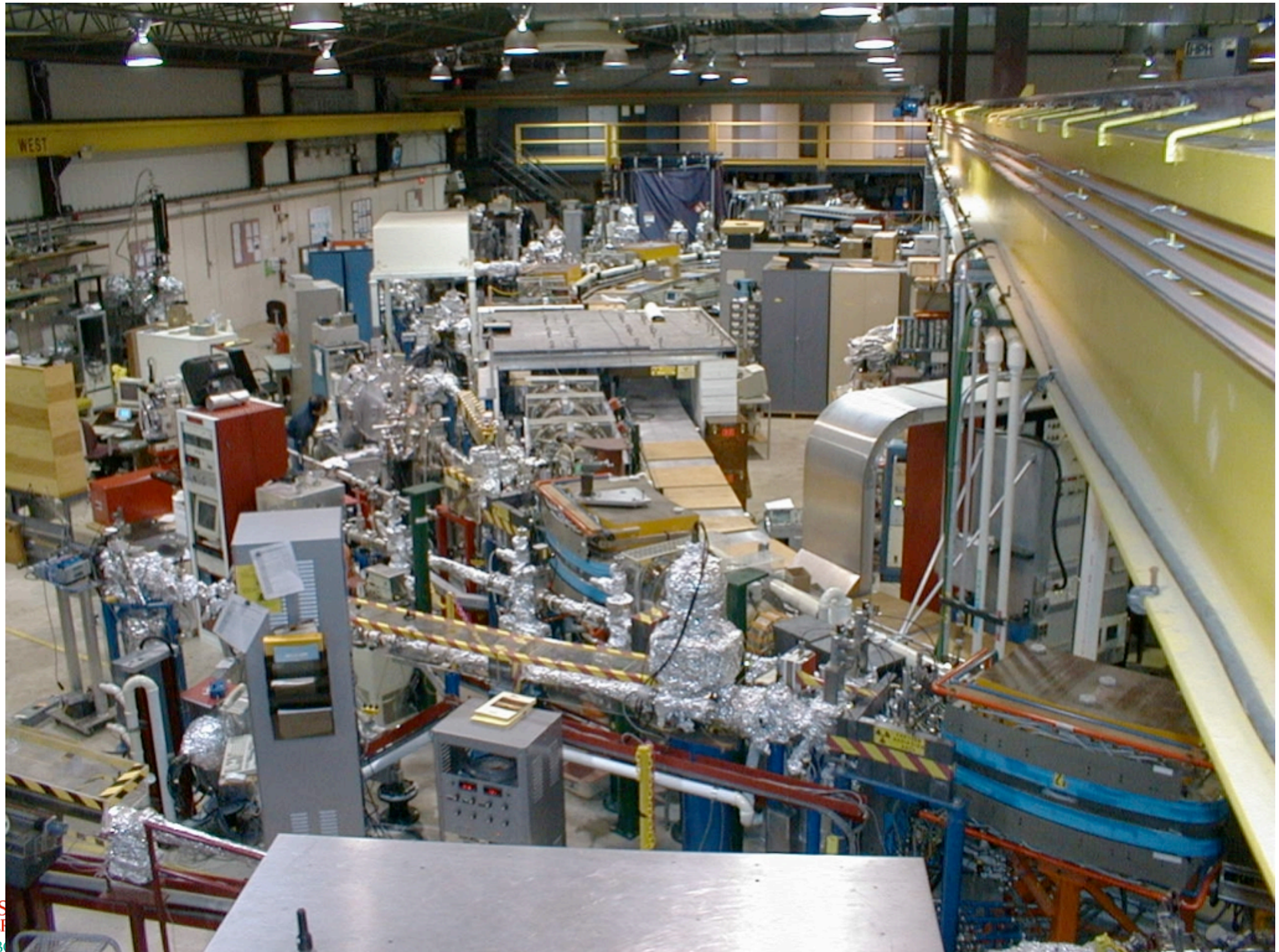
## U1 beamline







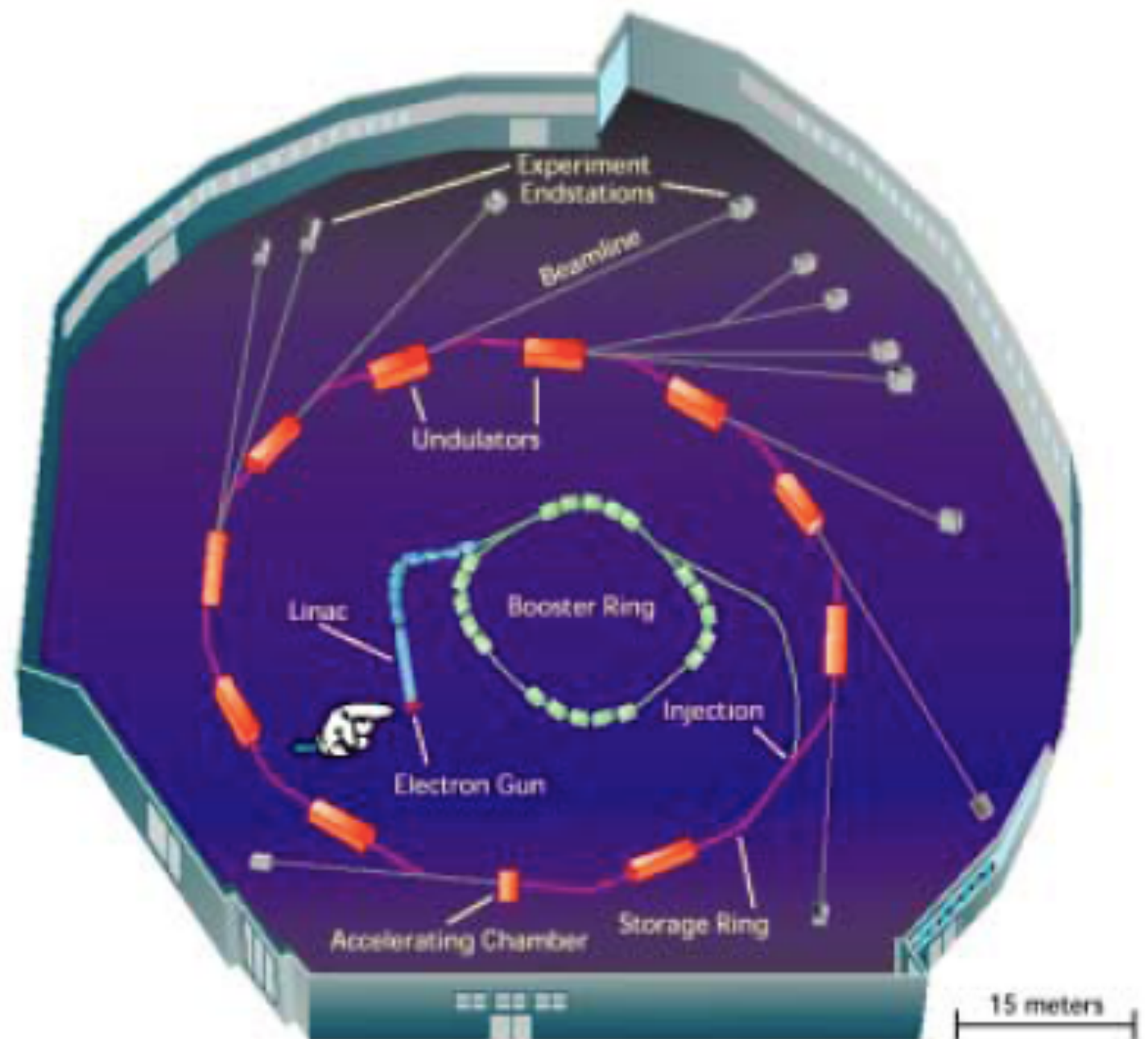
# Alladin at SRC



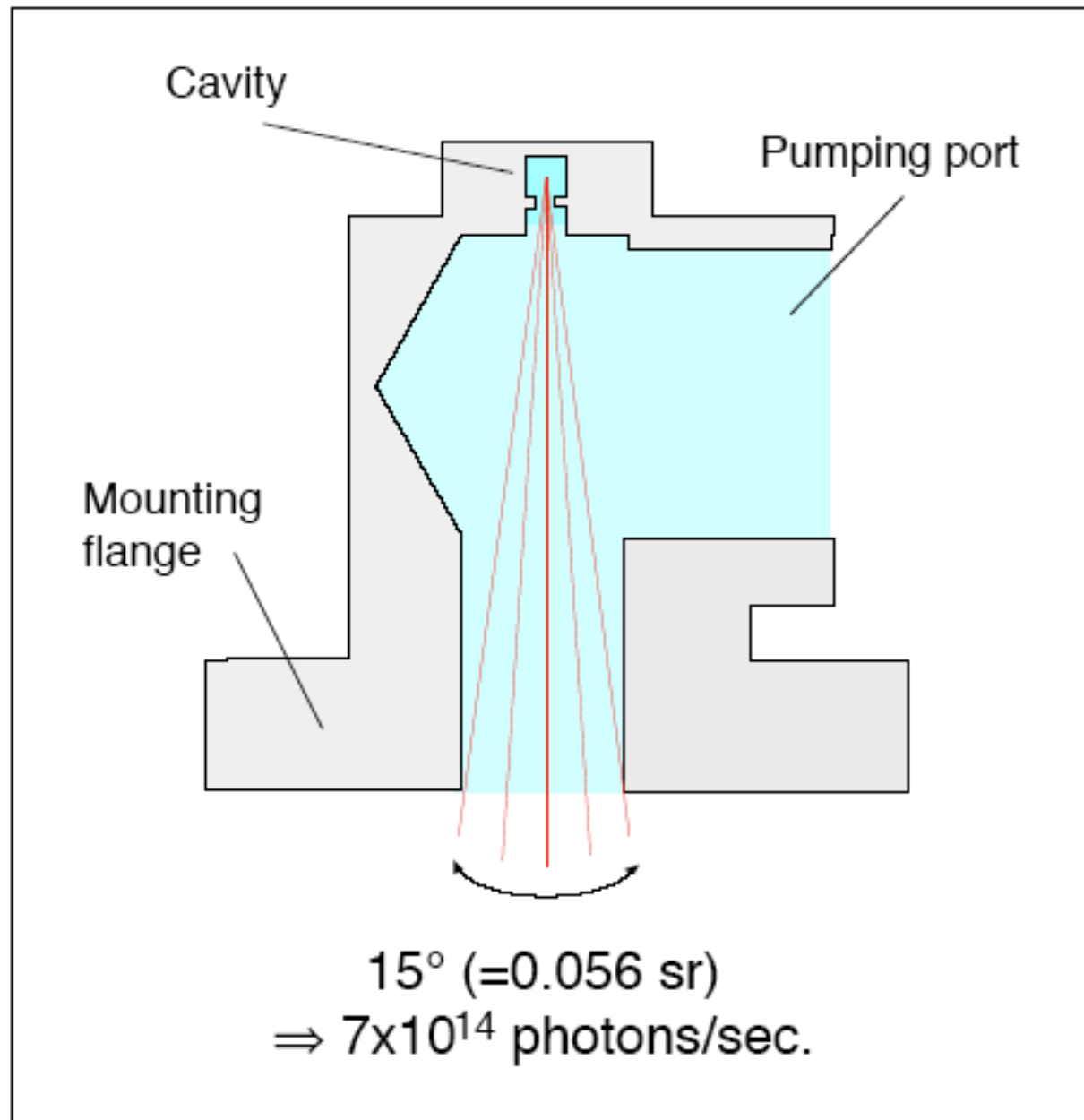


# Advanced Light Source at Lawrence Orlando Berkeley National Laboratory





# Helium ECR lamp

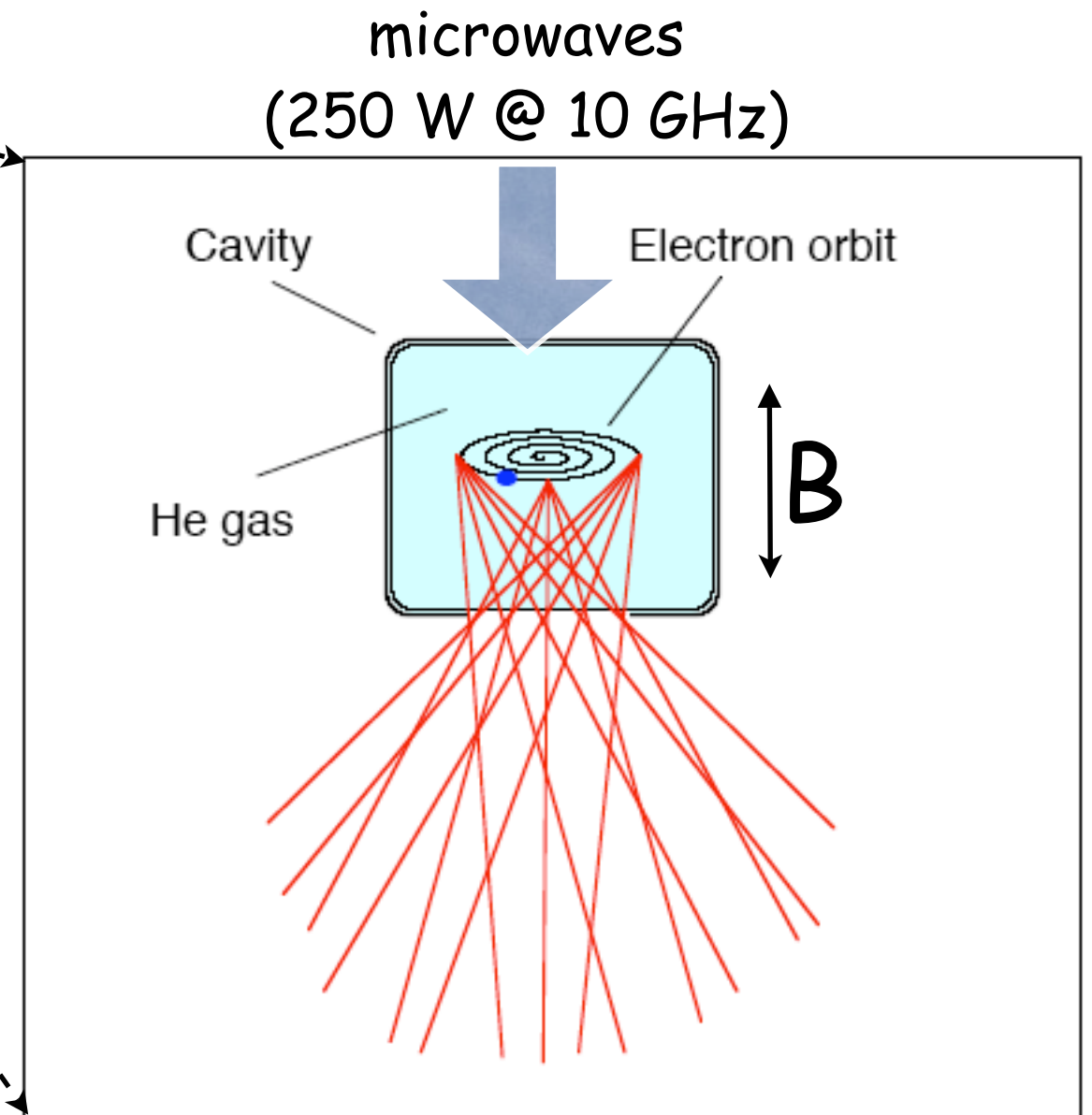
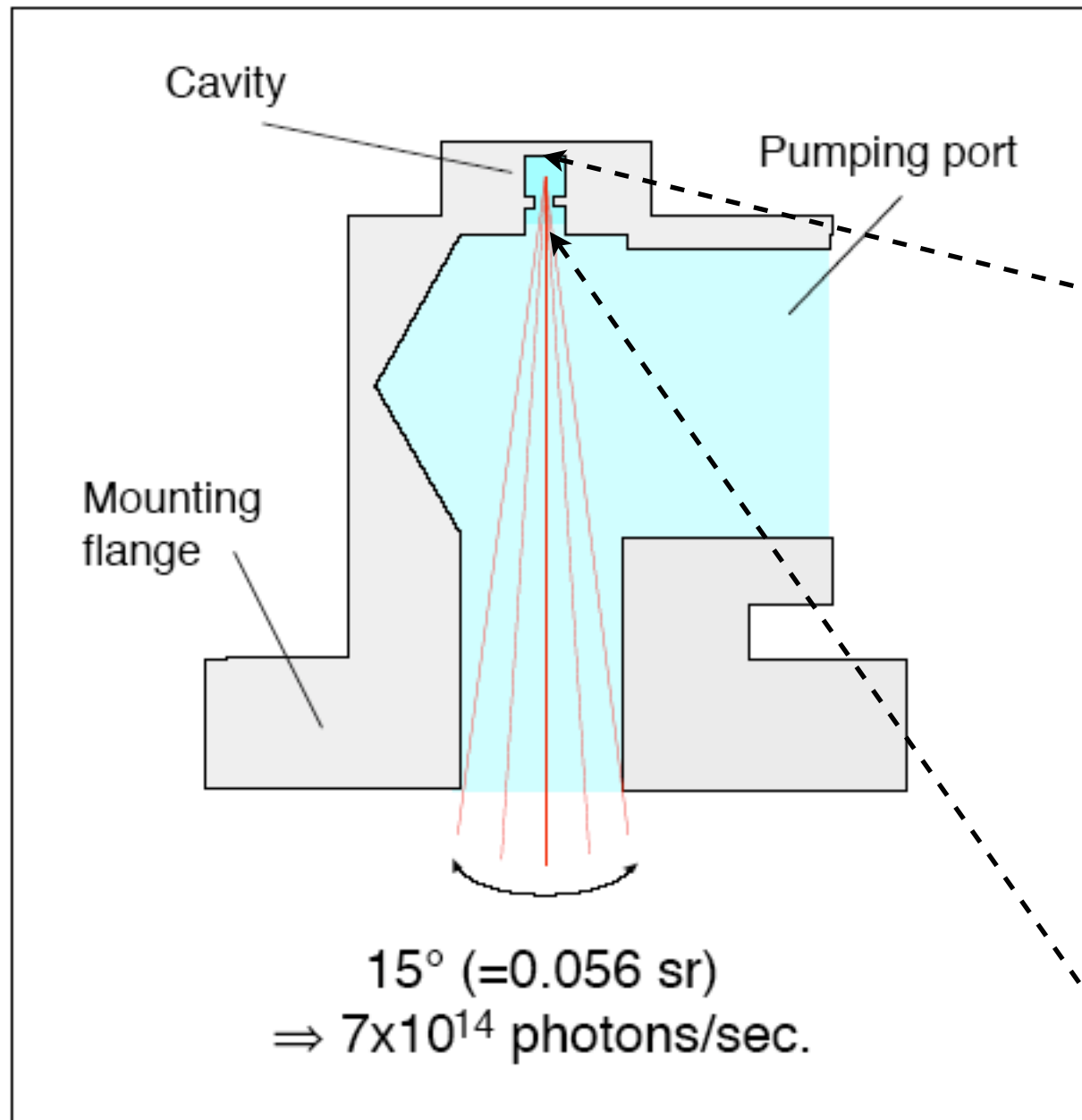


He I - 21.218 eV

He I - 23.087 eV

He II - 40.823 eV

# Helium ECR lamp

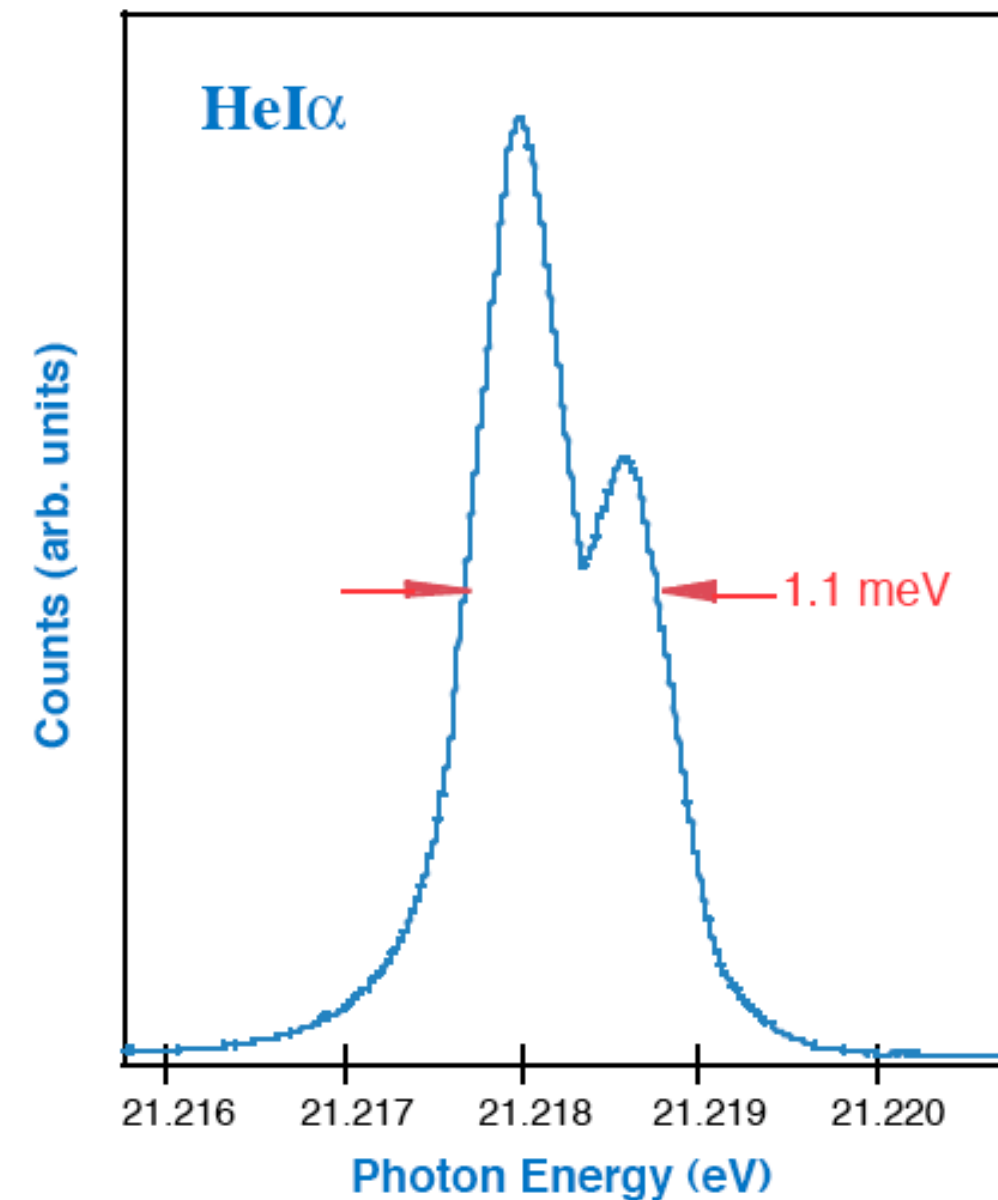
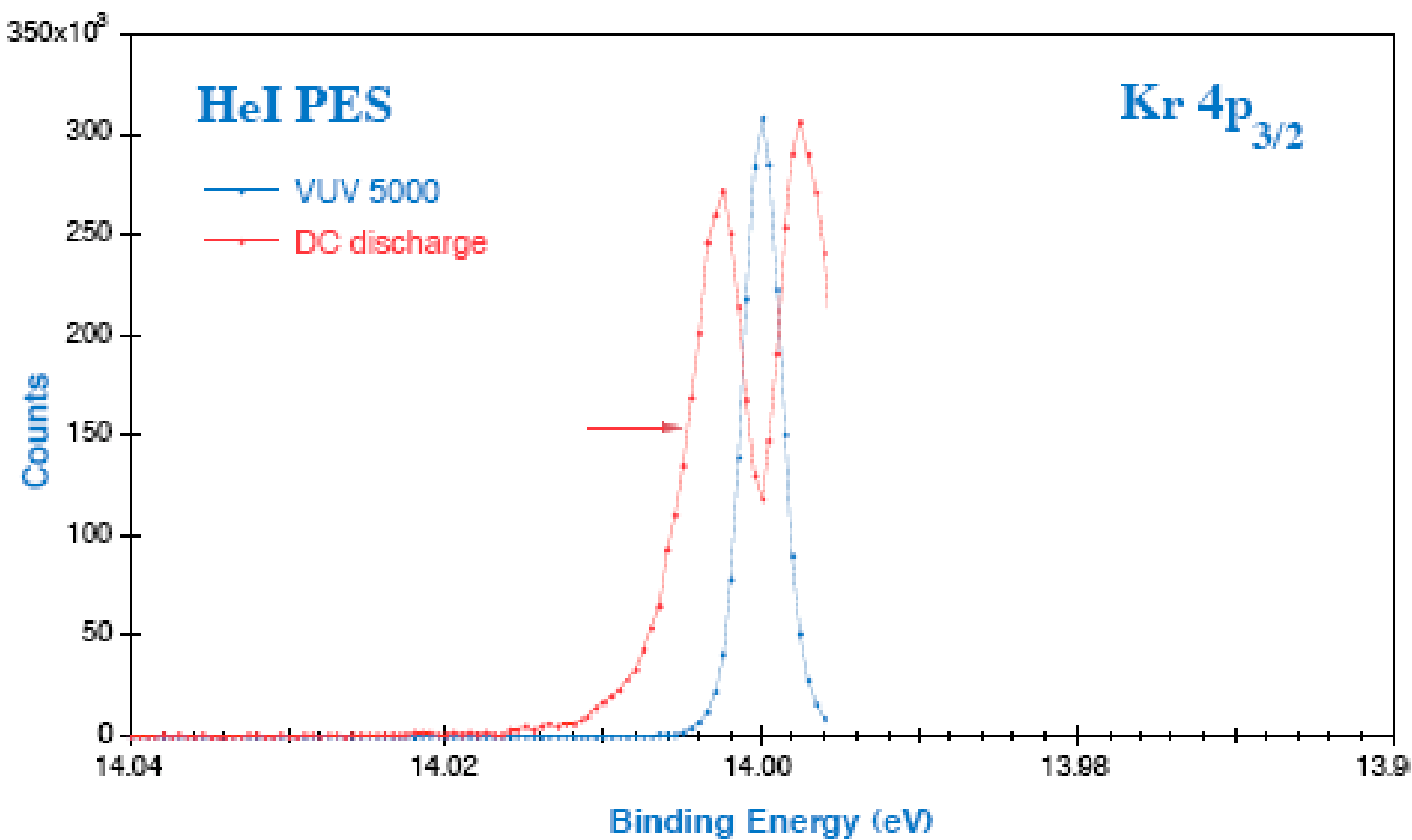


He I - 21.218 eV

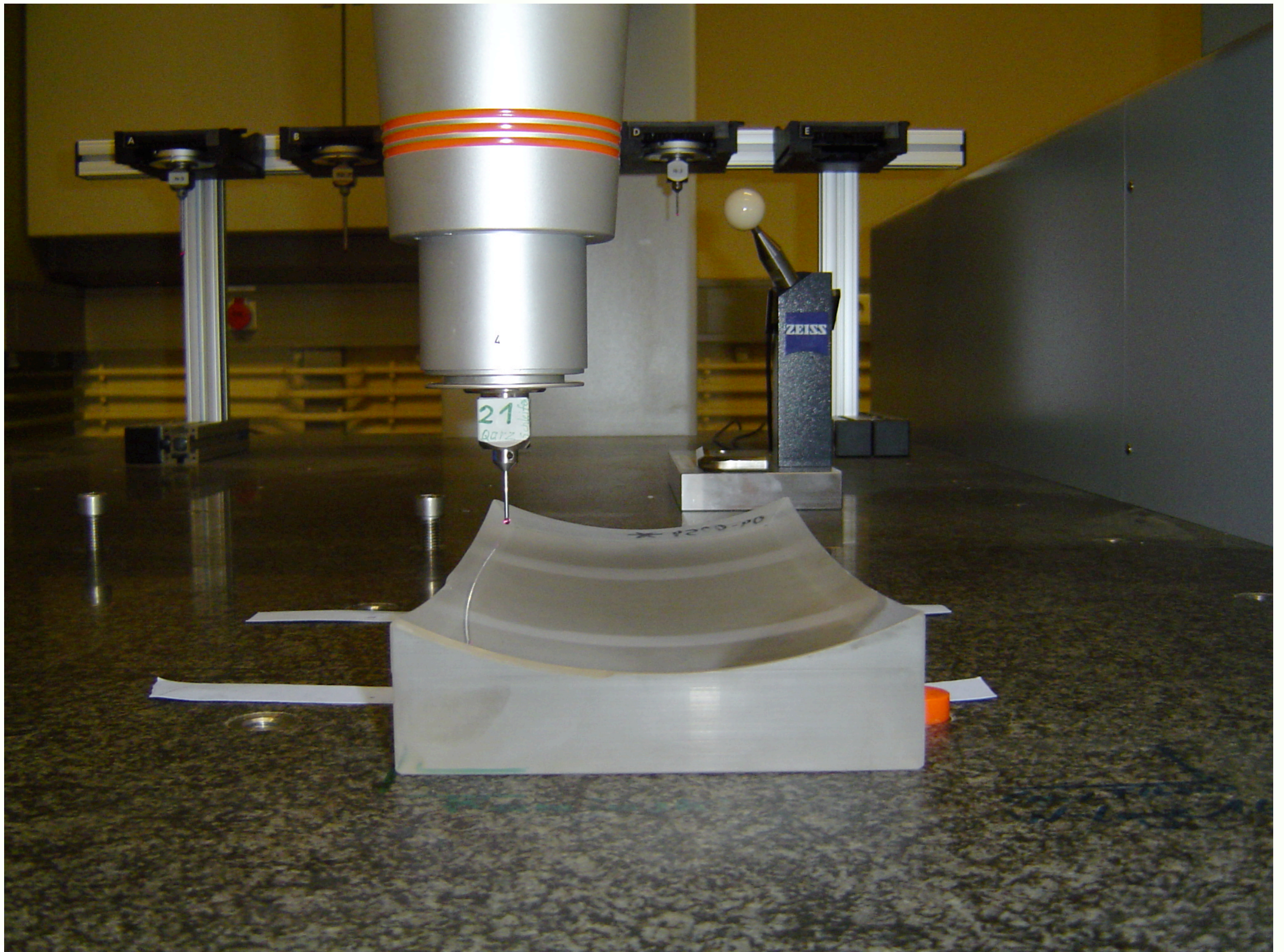
He I - 23.087 eV

He II - 40.823 eV

# Comparison with traditional DC discharge lamps









# New alternative source: UV laser

## Laser

**Photon energy: 6.994 eV**

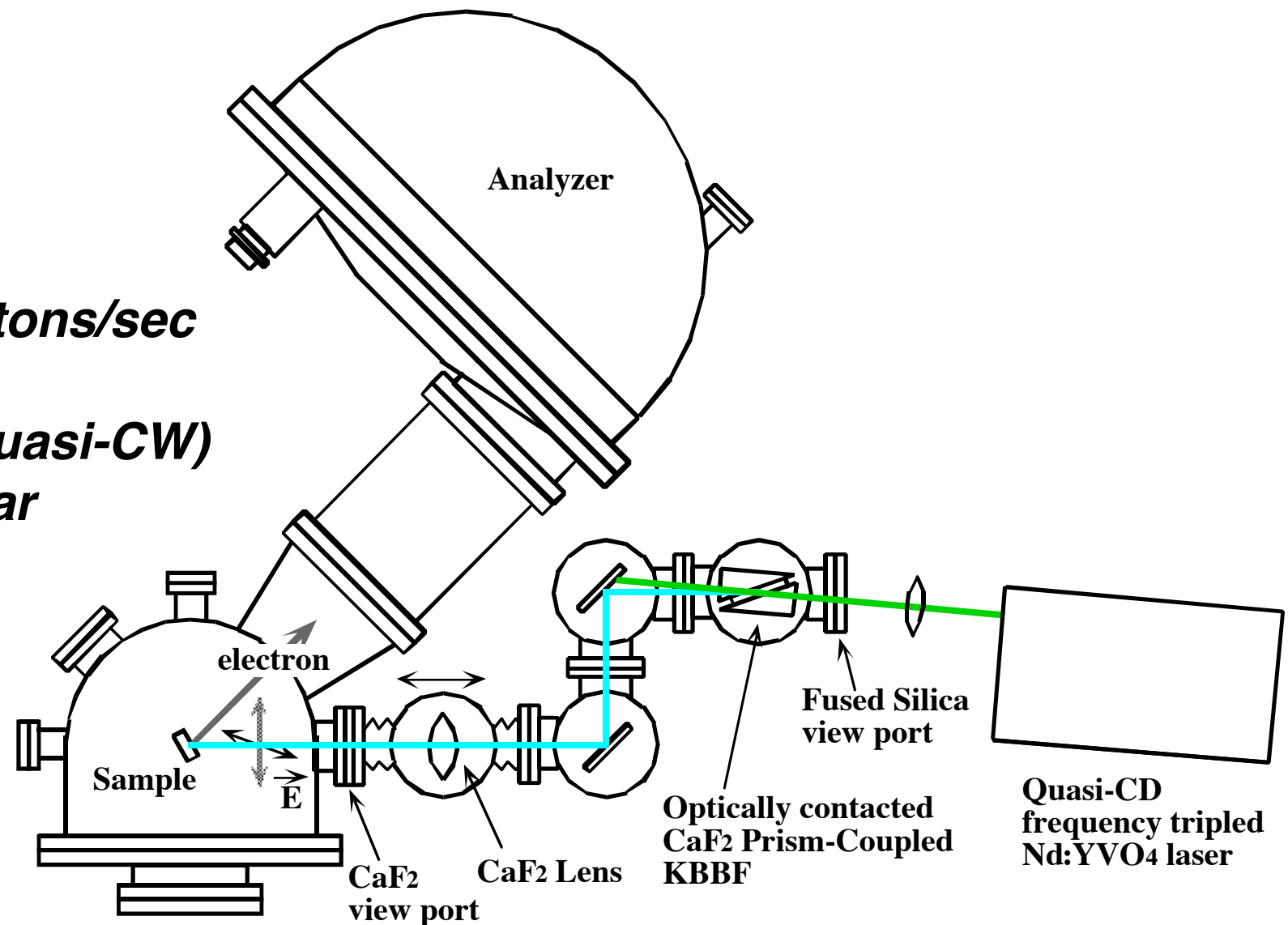
**FWHM=0.26 meV**

**Photon flux:  $2.2 \times 10^{15}$  photons/sec**

**Spot size:  $0.2 \mu\text{m}$**

**Repetition Rate: 80MHz(Quasi-CW)**

**Polarization: linear, circular**



Yokoya et al.

**ARPES Lab of Prof. S. Shin**

*Institute for Solid State Physics (ISSP), University of Tokyo*

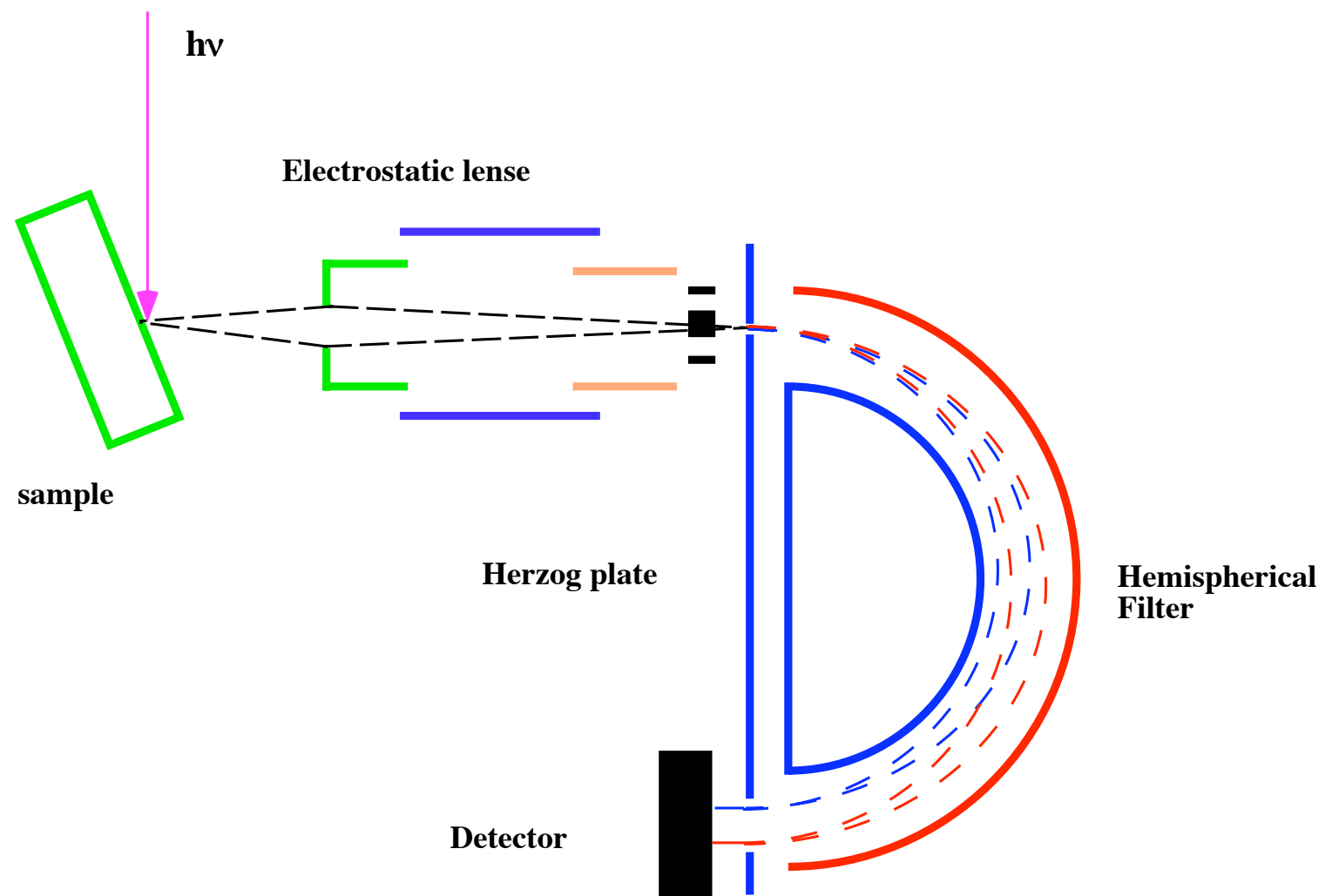
# Electron analyzers

Energy range: 7 eV - 1000 eV

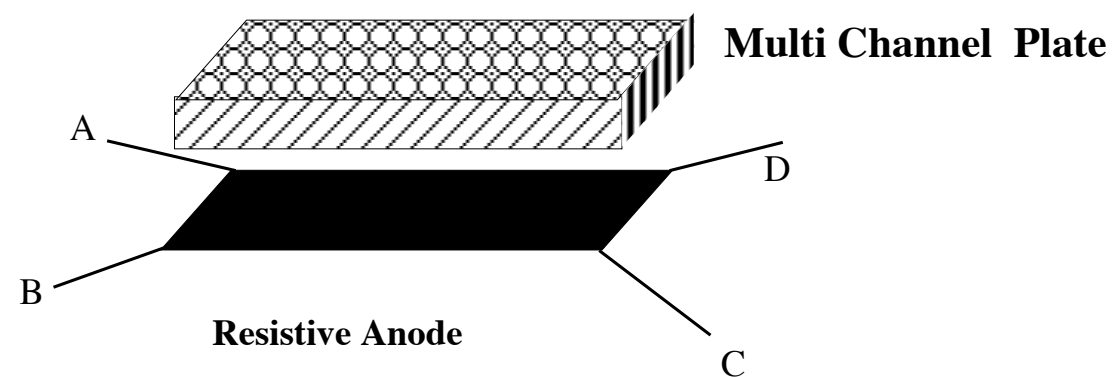
Energy resolution 1-30 meV

Momentum resolution 0.1 deg (1/400 of BZ)

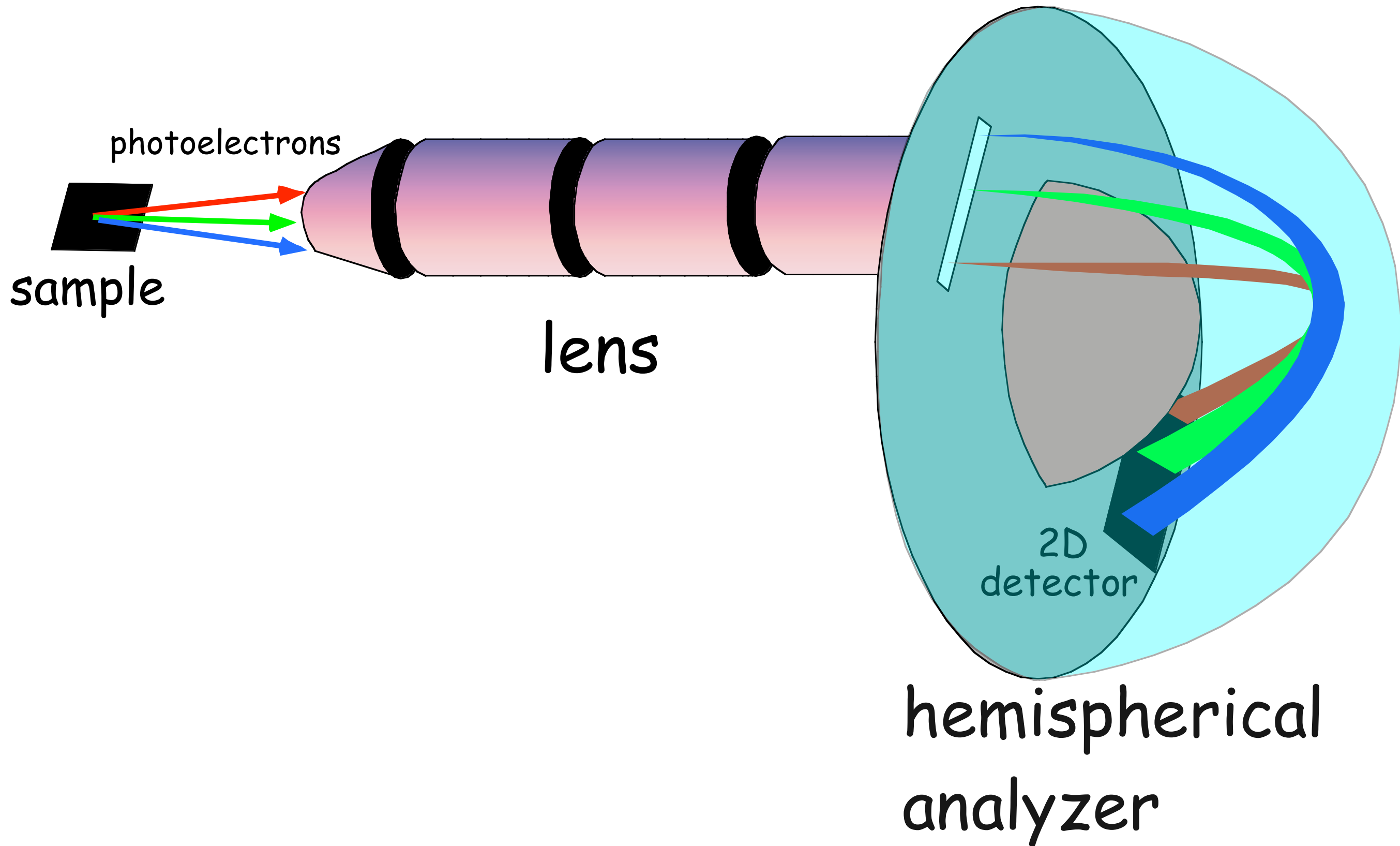
Single channel/multichannel



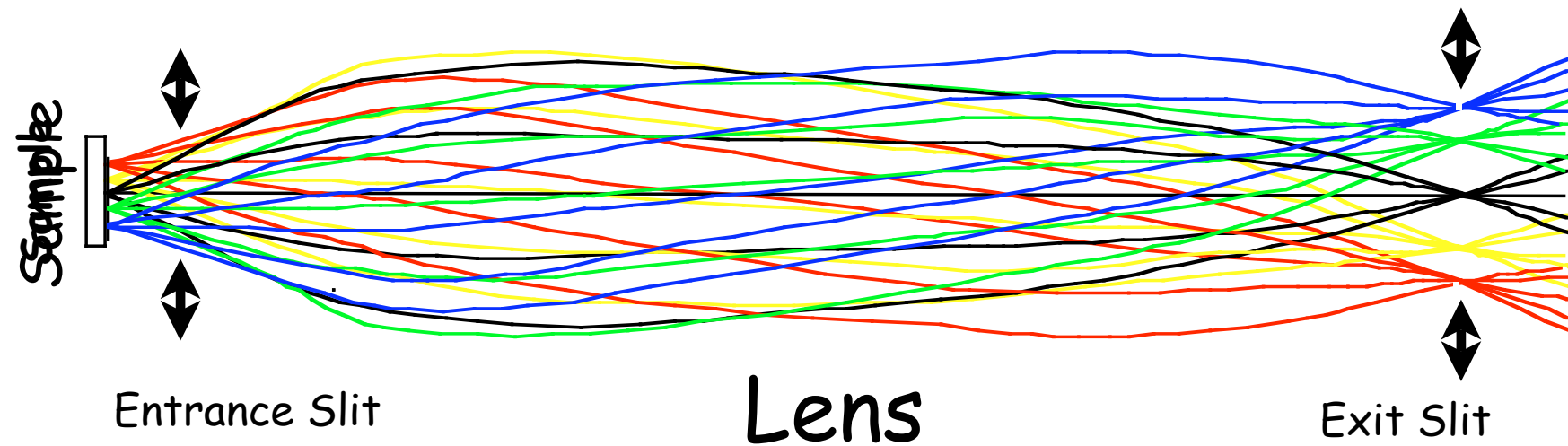
### Position Sensitive Detector



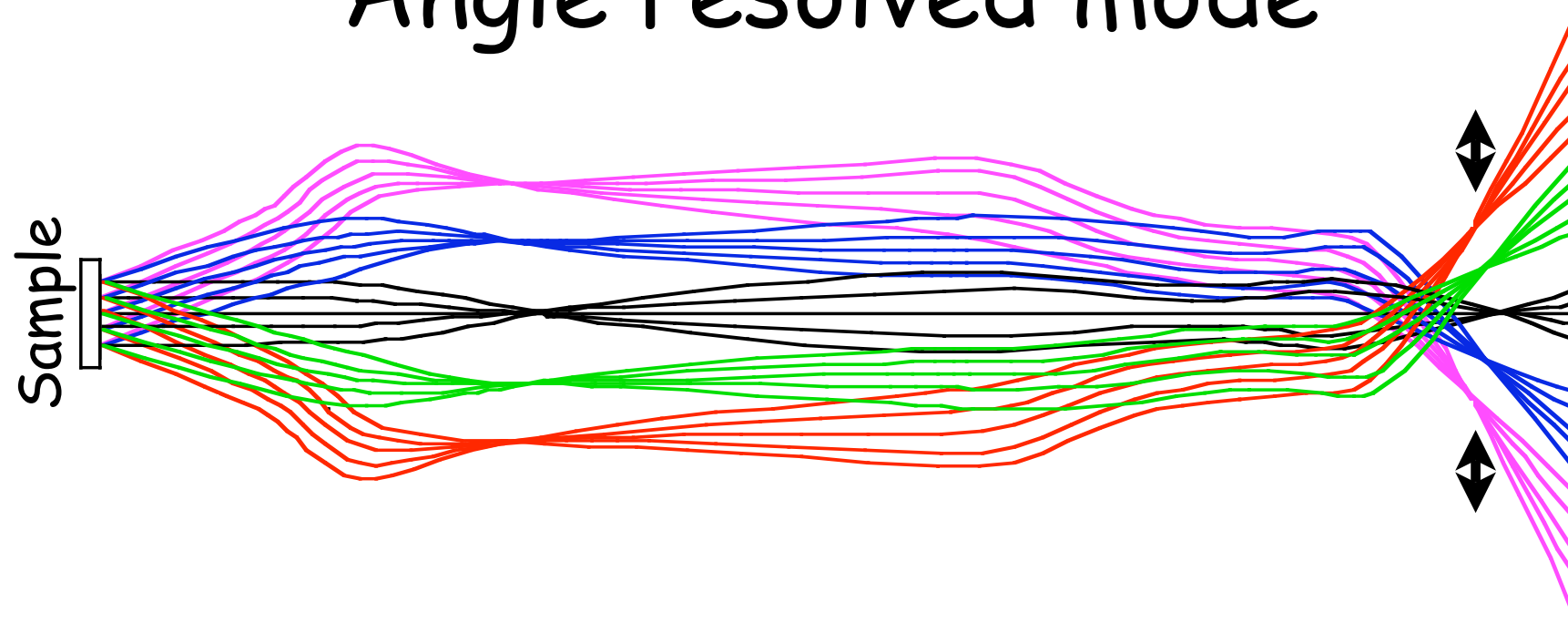
# Electron analyzer



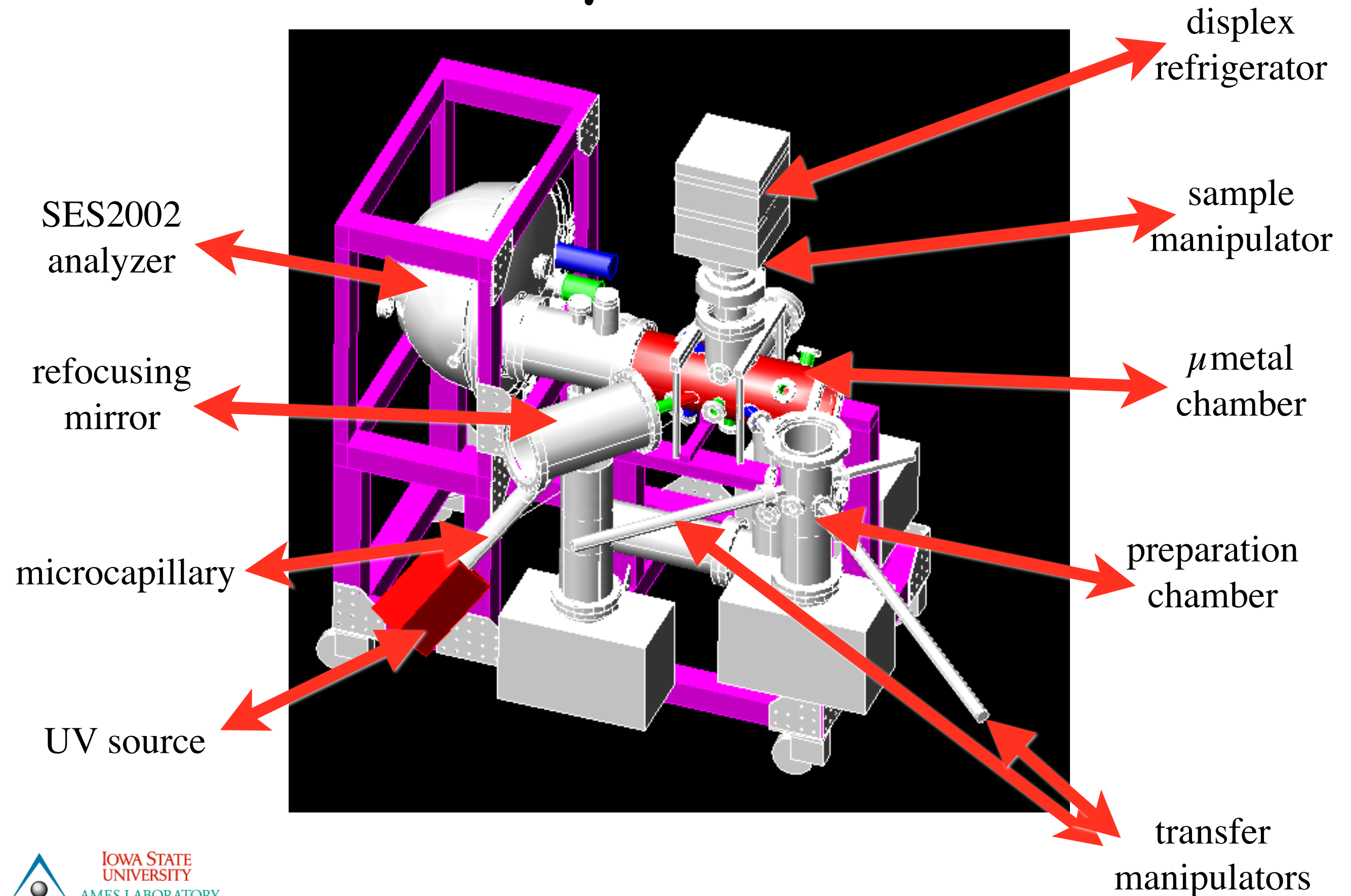
# Transmission mode



# Angle resolved mode



# Laboratory based ARPES





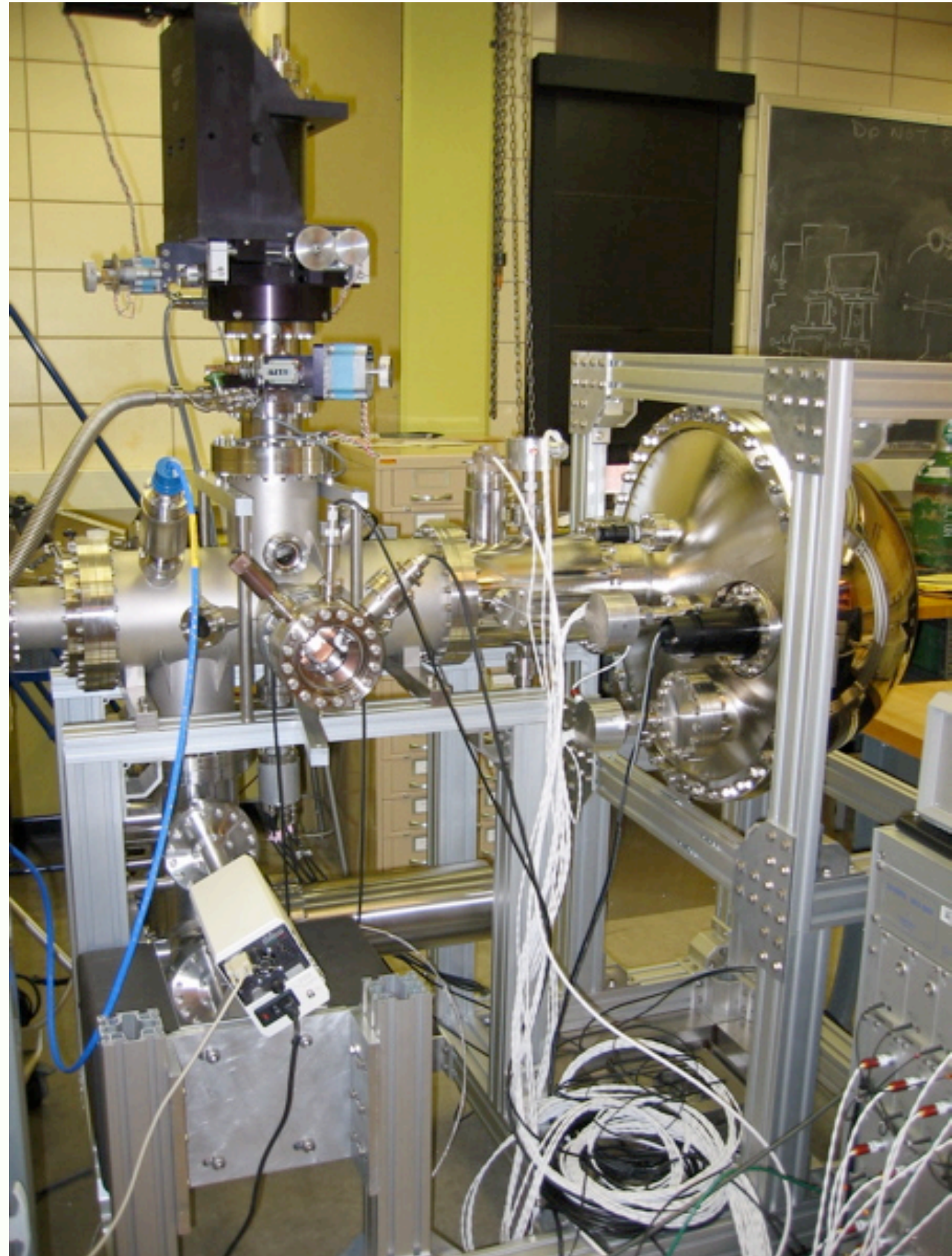
... high precision lab-based ARPES system

Energy resolution:  
 $\sim 1$  meV

Angular resolution:  
0.1 deg.

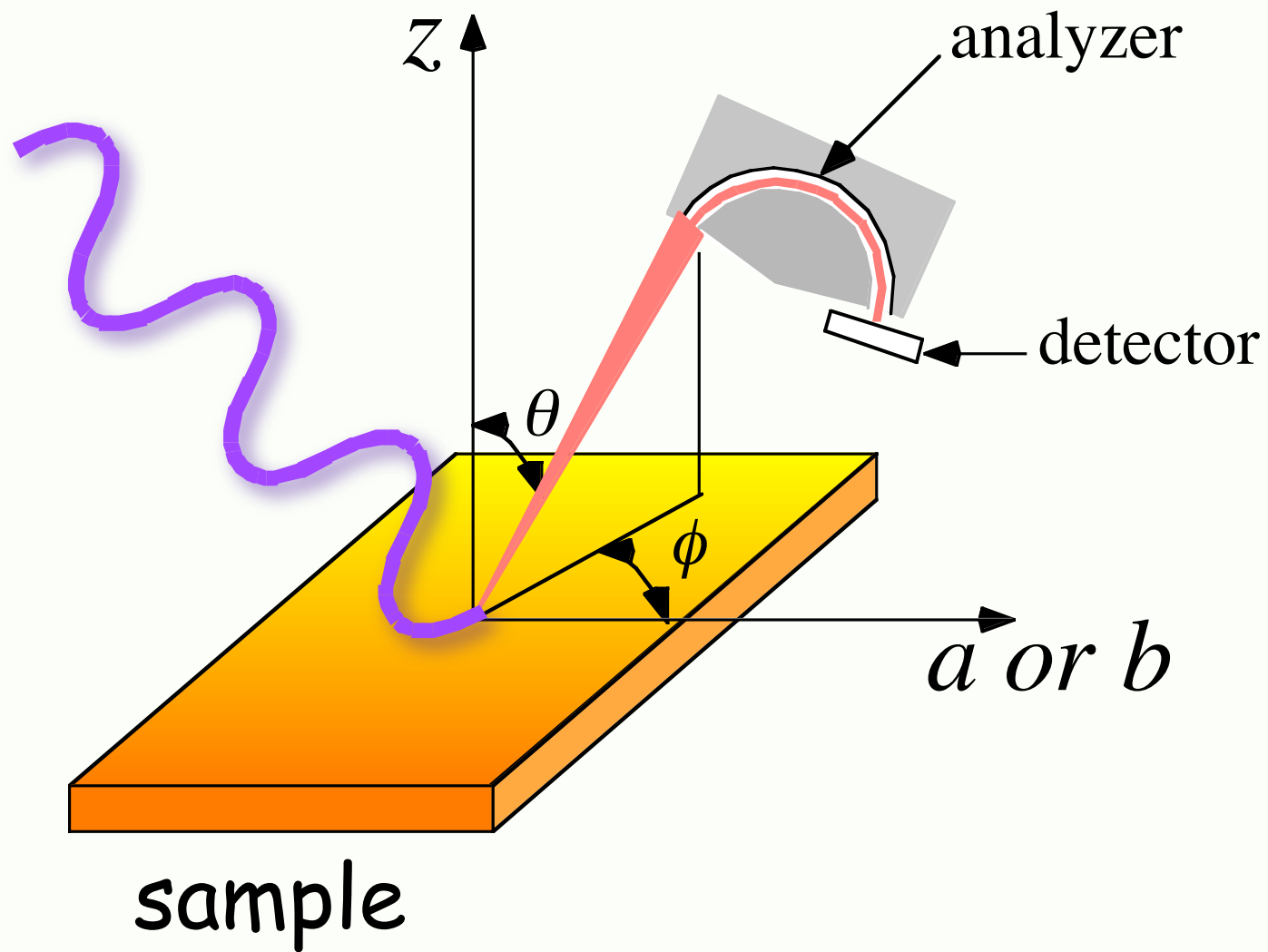
UV source:  
 $10^{13}$  photons/sec.

Sample positioning:  
 $\sim 1 \mu\text{m}$





# ARPES experiment



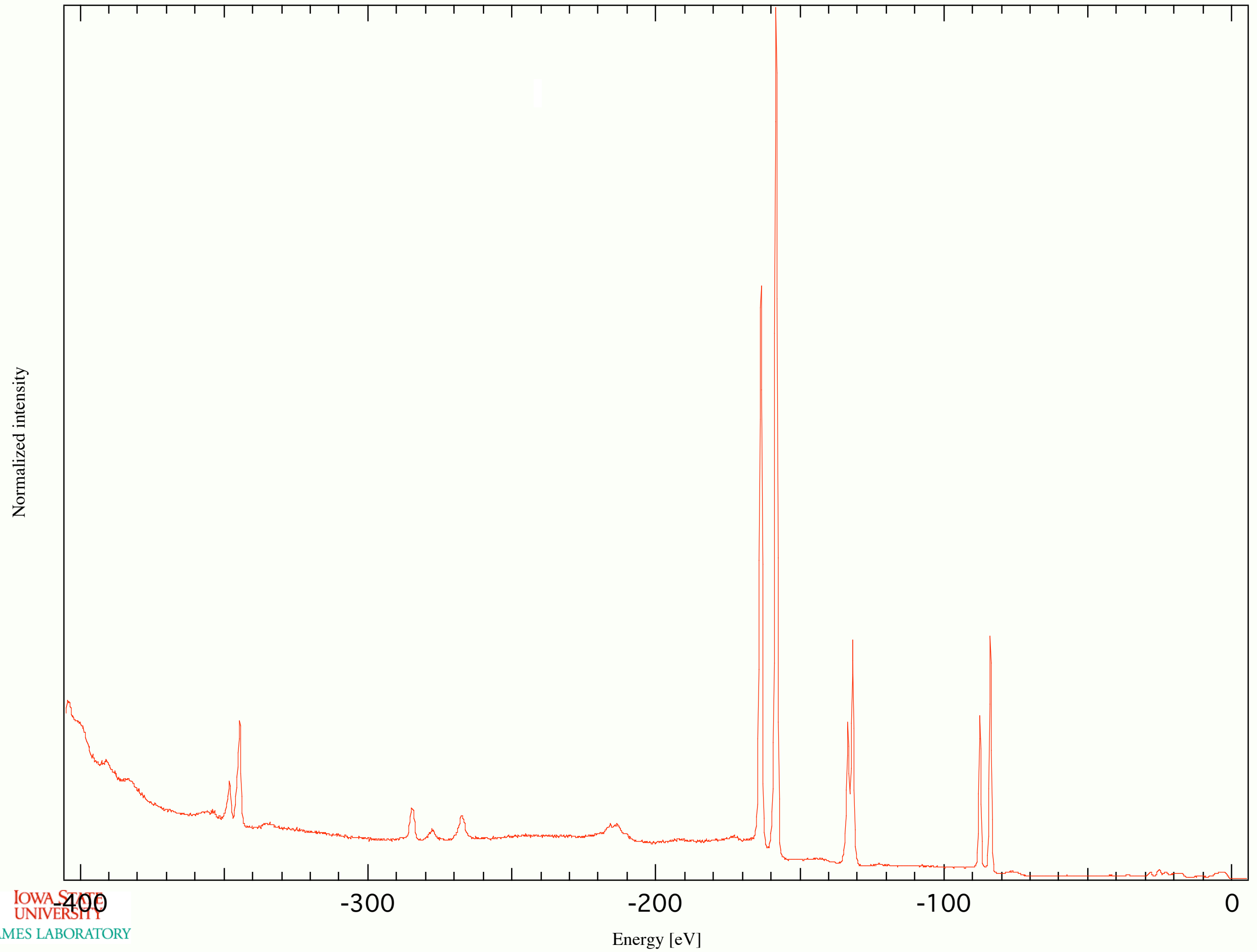
We need:  
 binding energy -  $E_b$   
 initial momentum -  $k^i$

$$E_b = E - h\nu + W$$

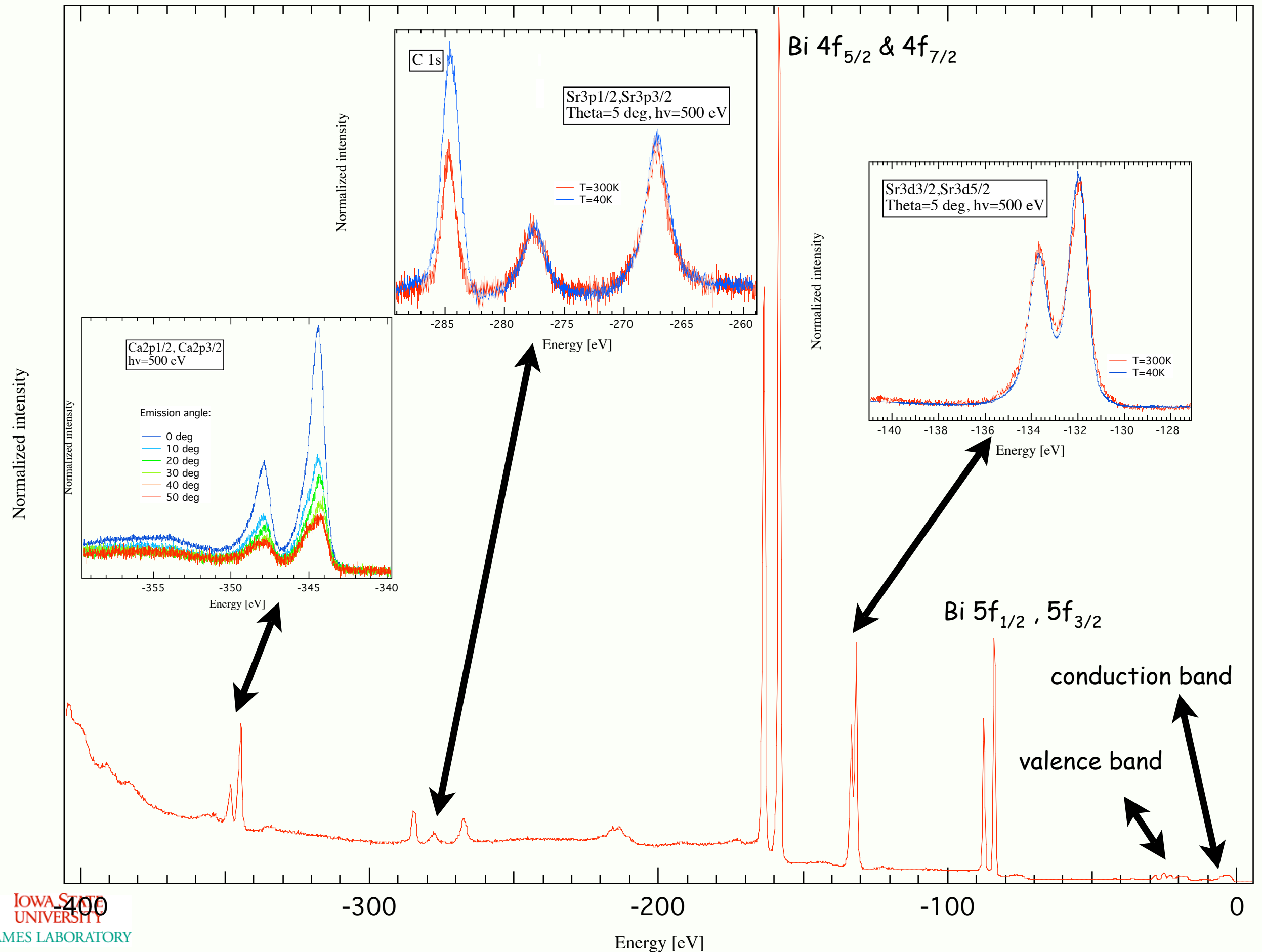
$$k_{||}^i = k_{||}^f = \sqrt{2mE/\hbar^2} \sin\theta$$

$$k_{\perp}^i = k_{\perp}^f - G = \sqrt{2mE/\hbar^2} \cos\theta - G$$

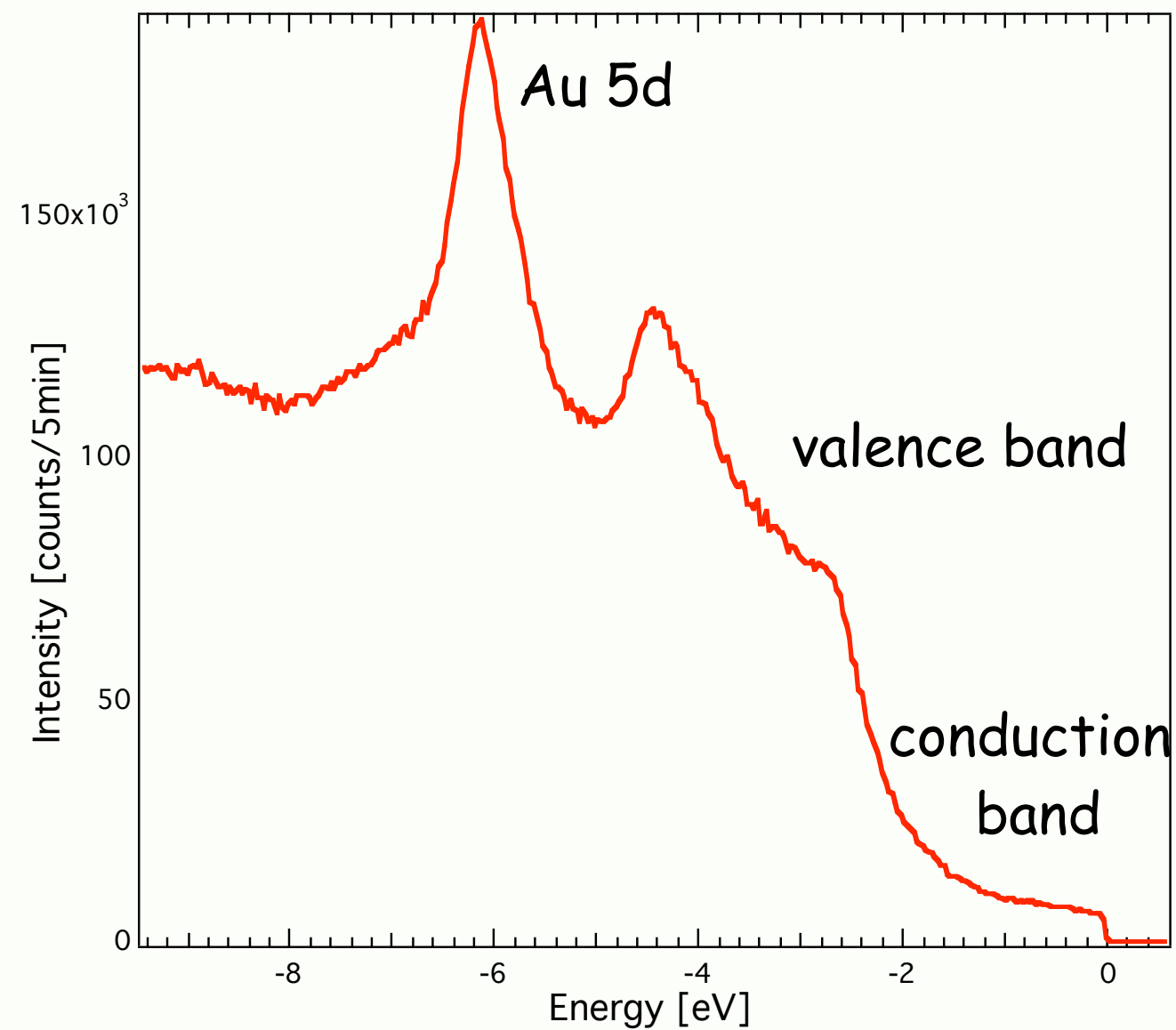
# typical photoemission spectrum from Bi2212



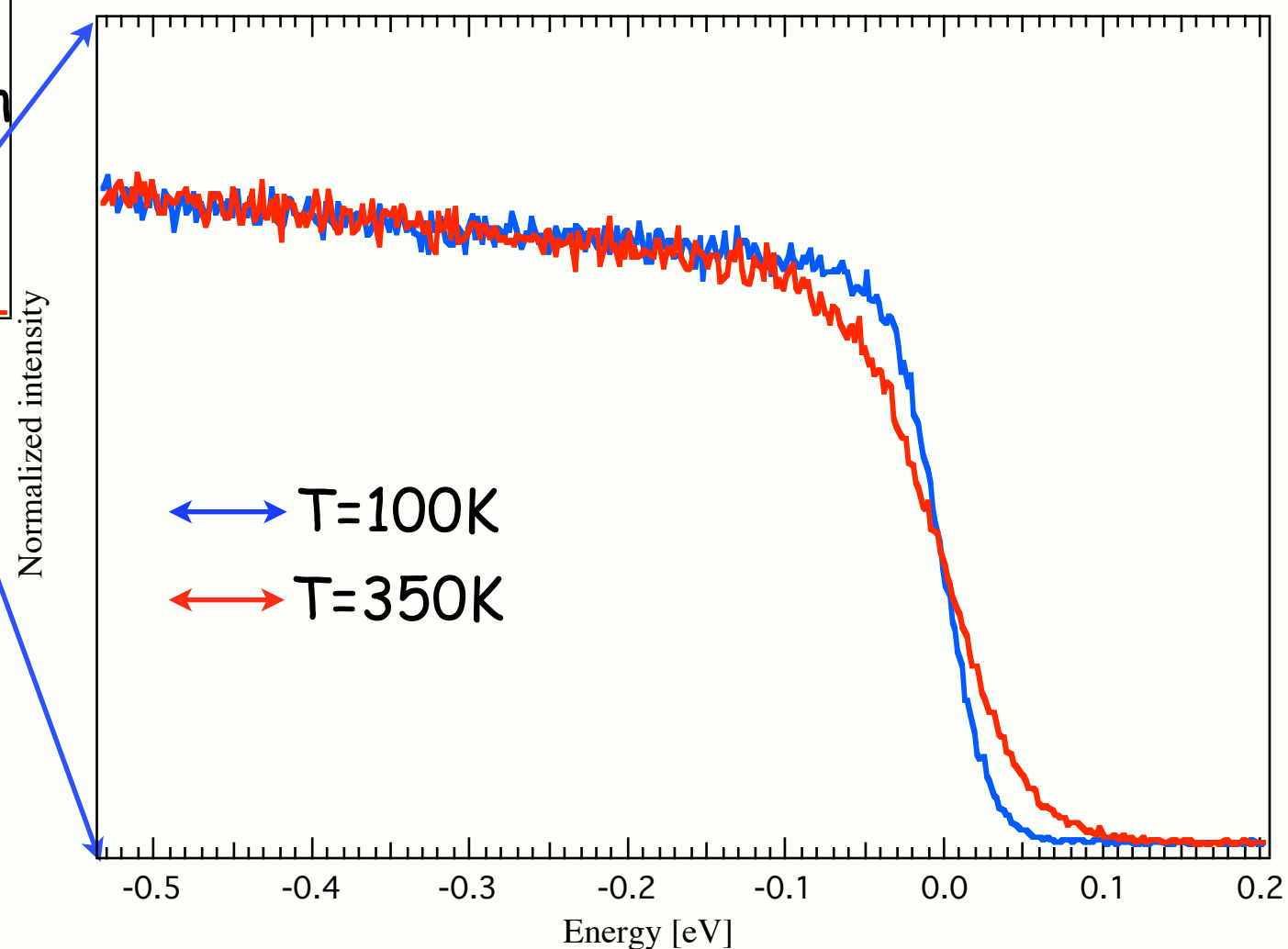
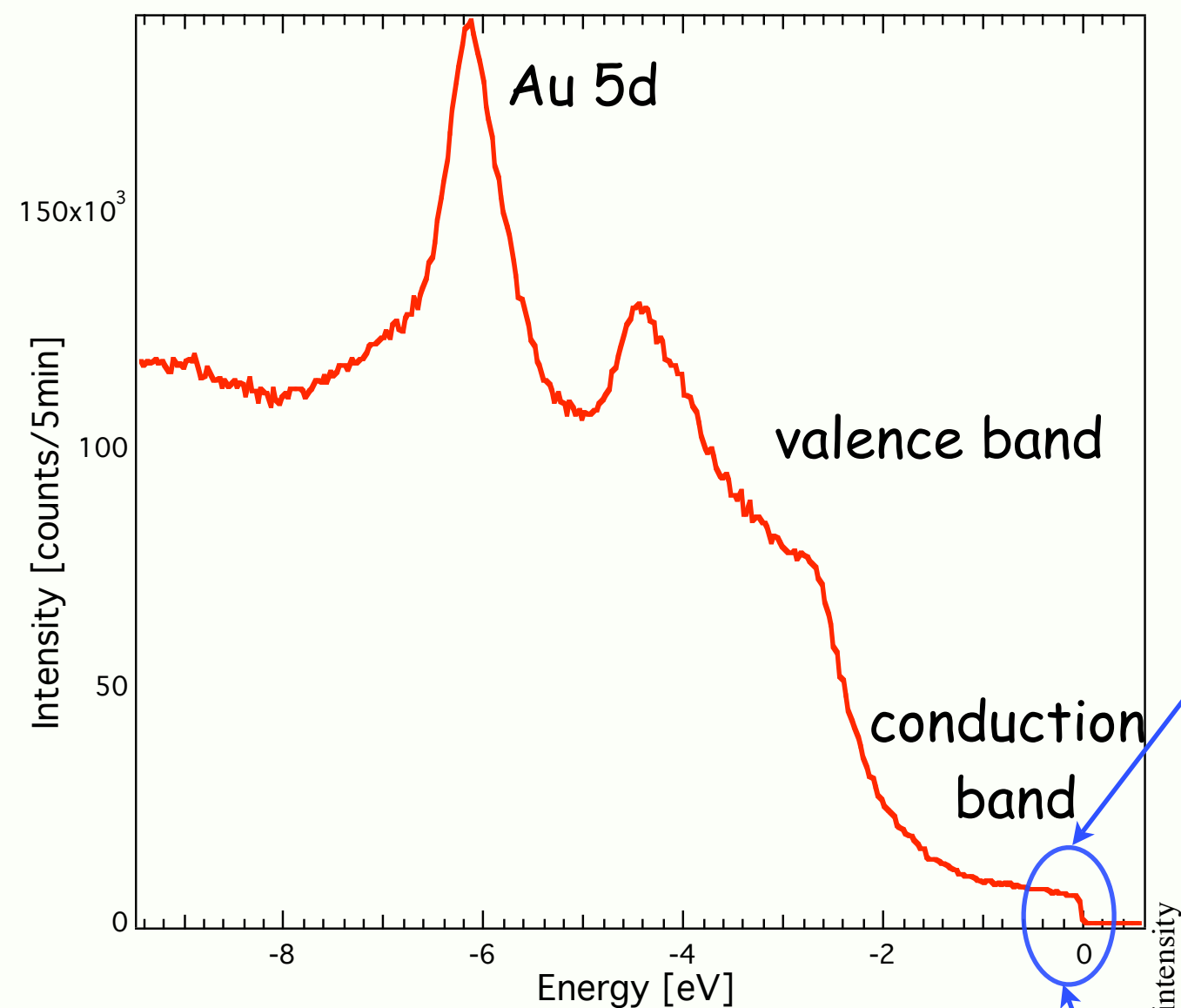
# typical photoemission spectrum from Bi2212



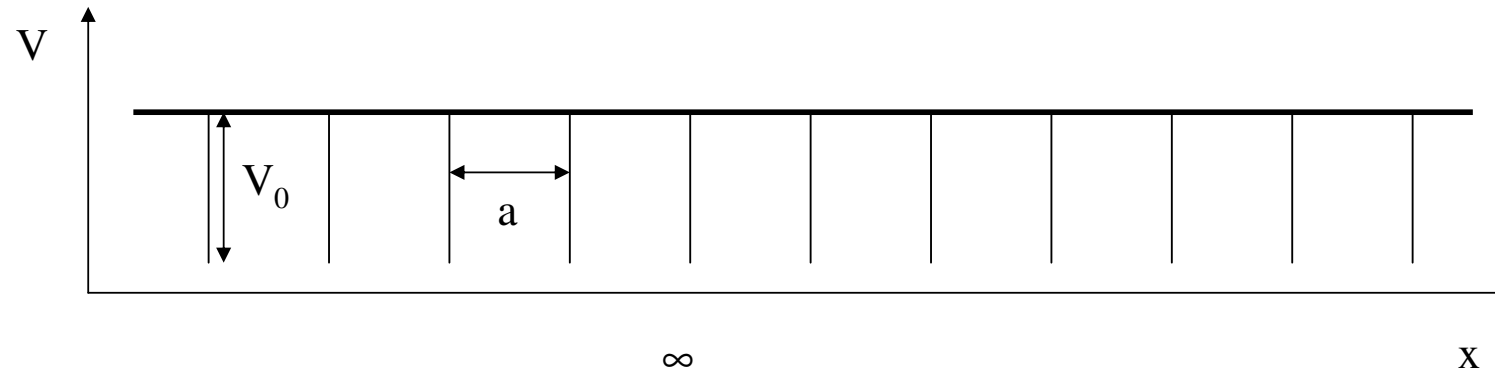
# Valence and conduction bands - simplest example: poly Au



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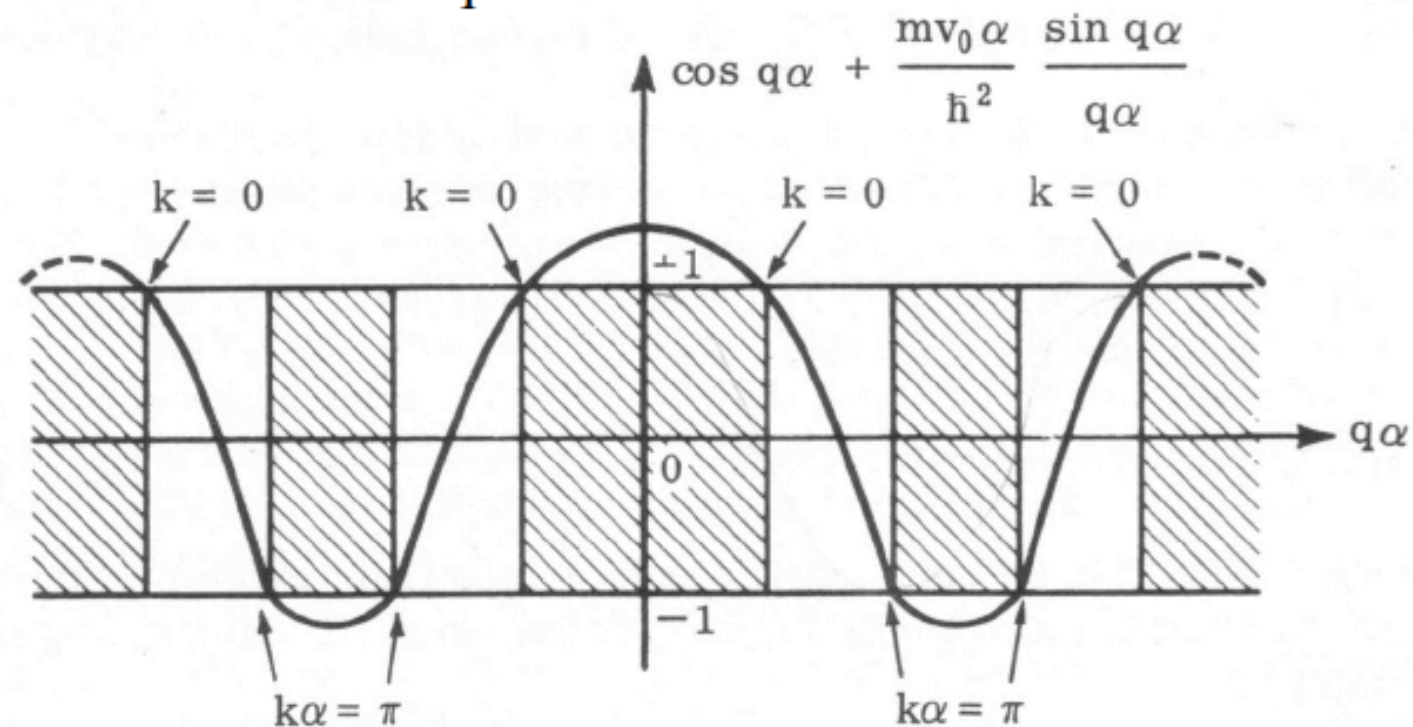
The Krönig-Penney model:

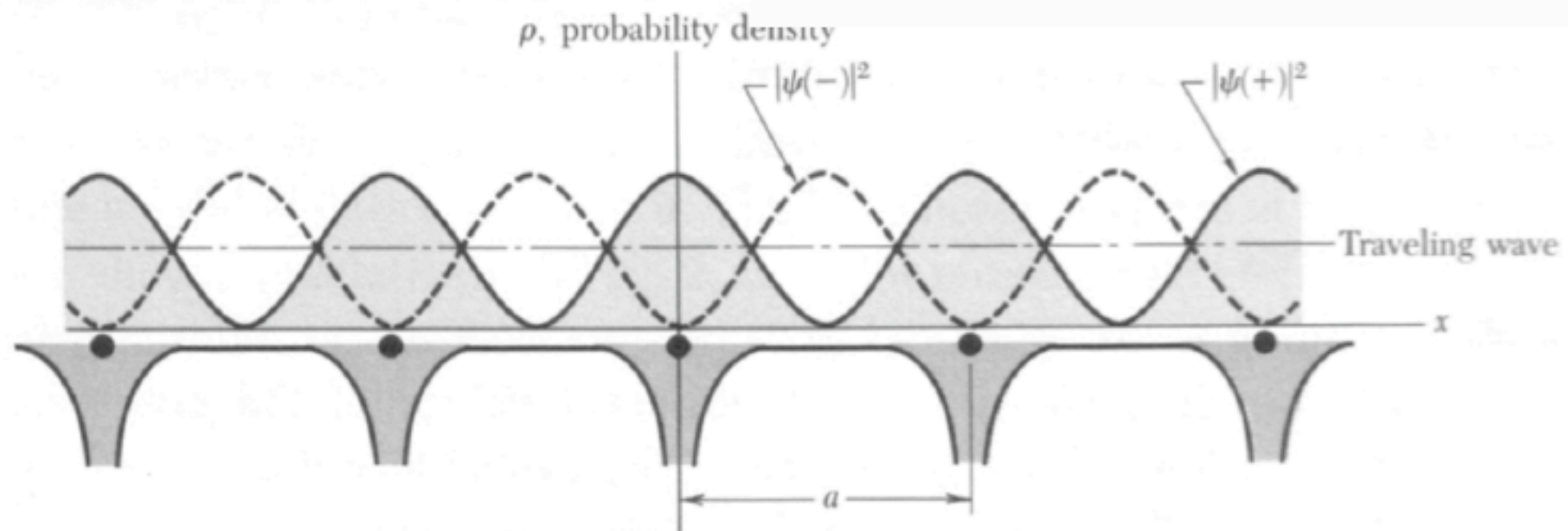
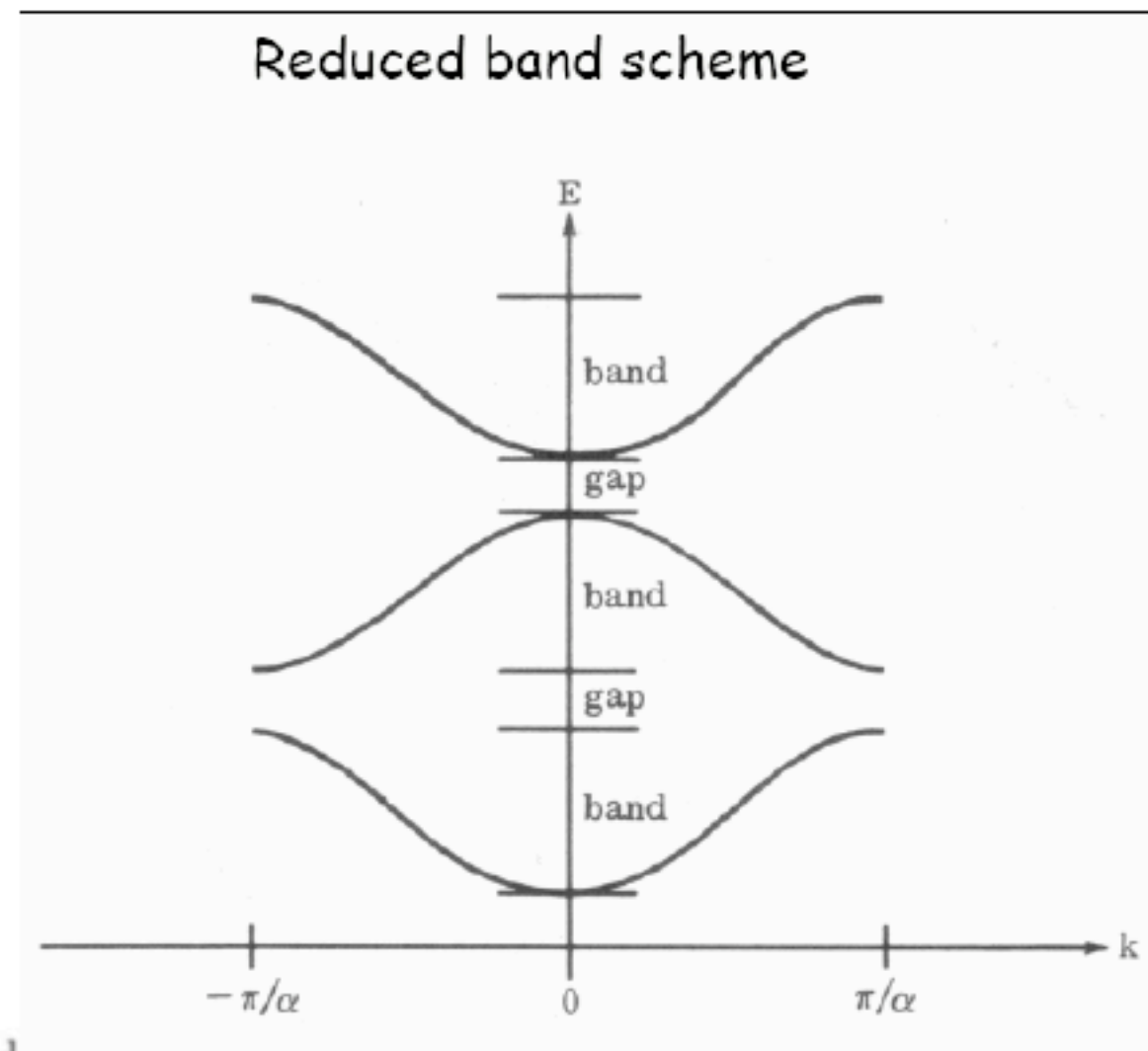
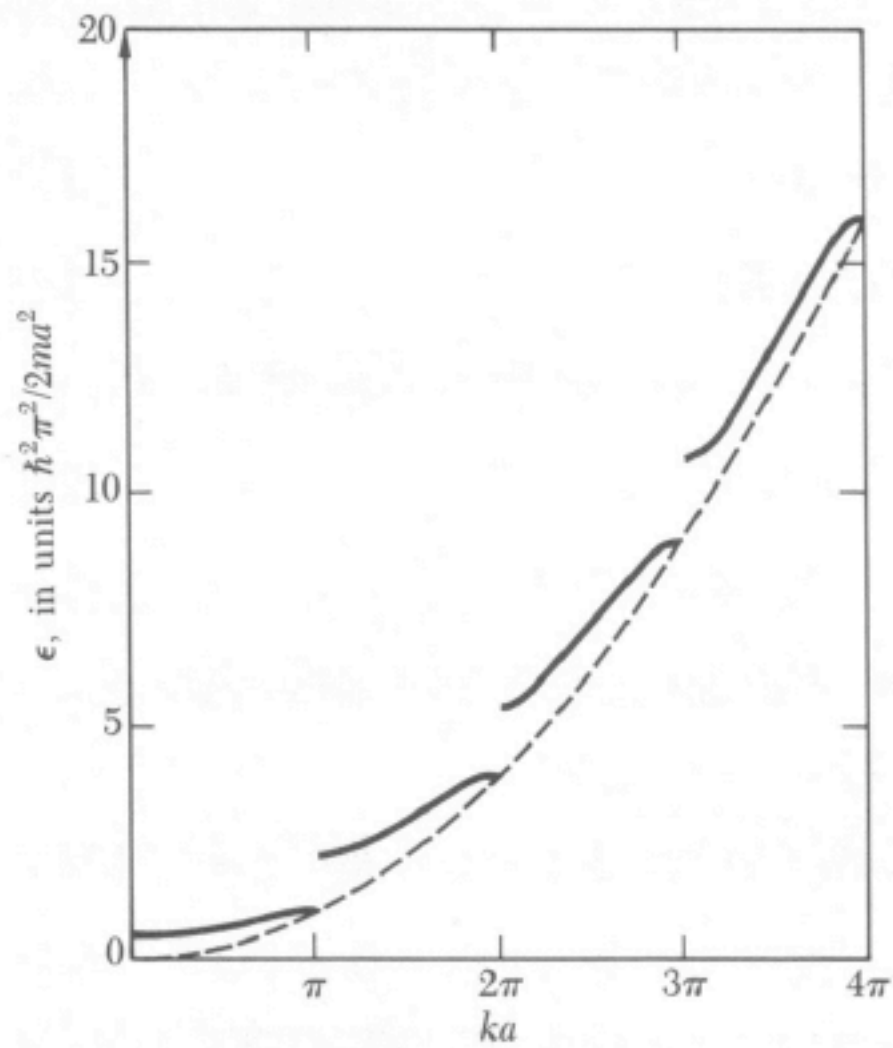


$$V = \sum_{-\infty}^{\infty} V_0 \delta(x - na)$$

$$\left( E + \frac{\hbar^2}{2m} \frac{d^2}{dx^2} \right) \psi(x) = \sum_{-\infty}^{\infty} V_0 \delta(x - na) \psi(x)$$

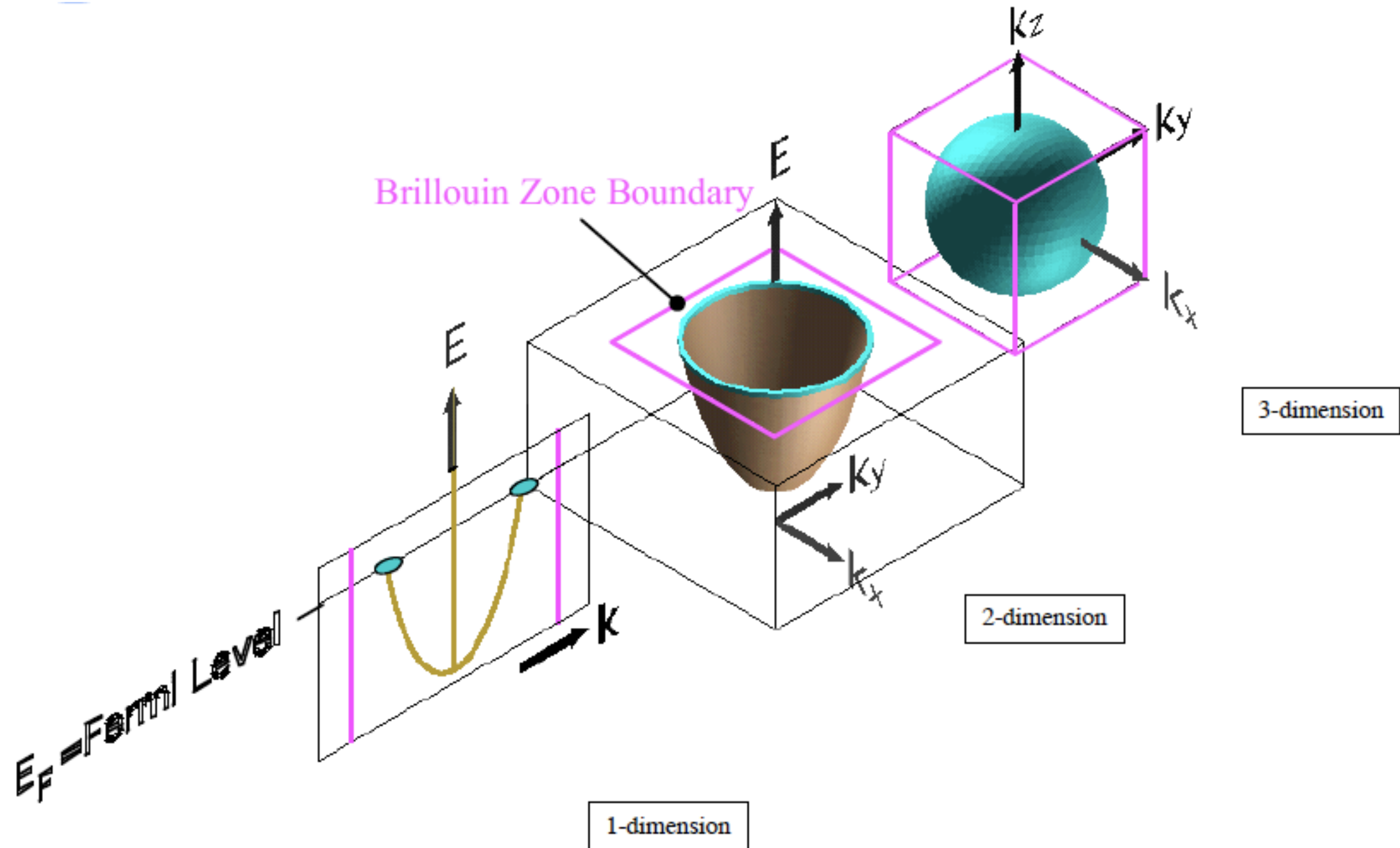
Thus:  $\cos ka = \cos qa + \frac{mV_0 a}{\hbar^2} \frac{\sin qa}{qa}$





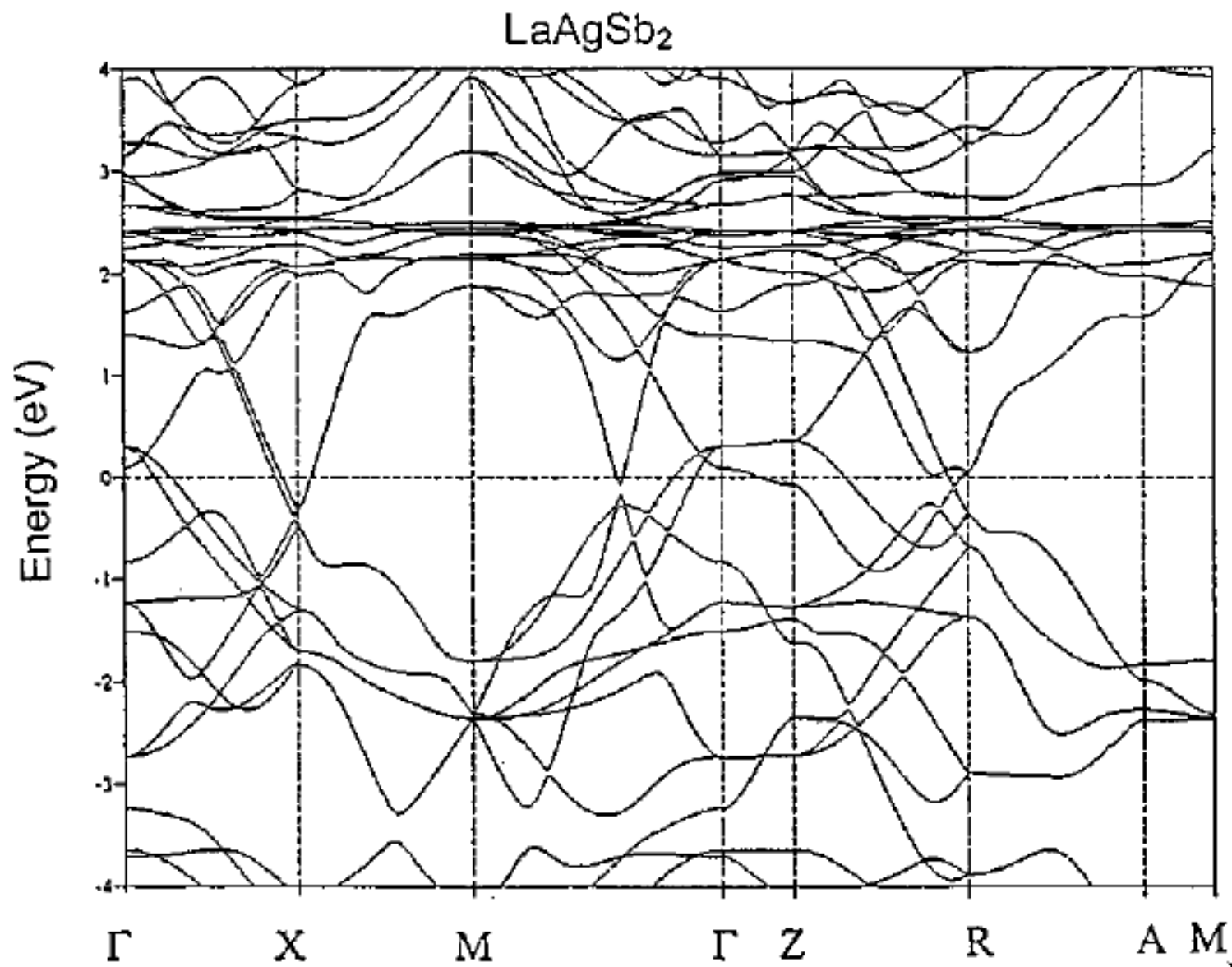


# Fermi surface

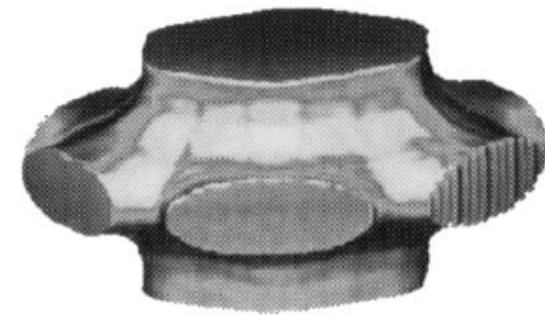
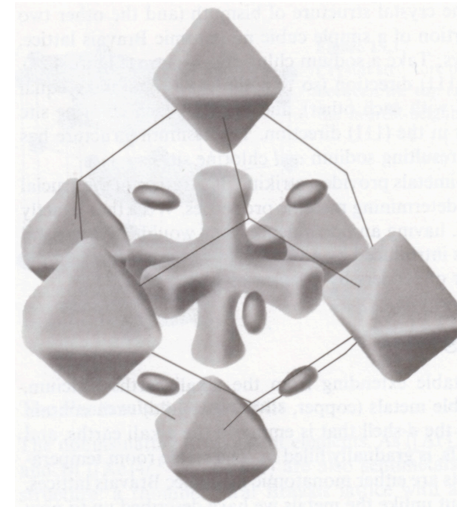
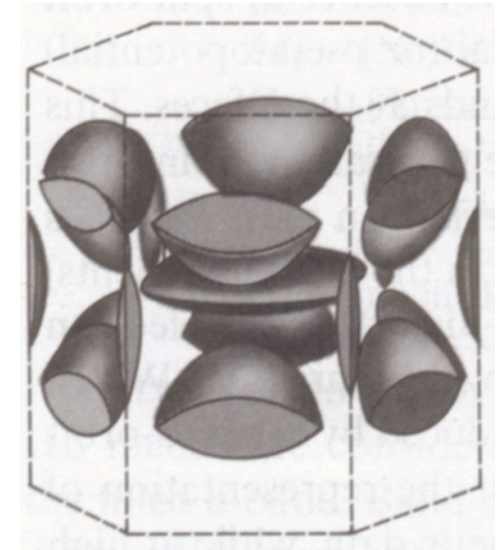
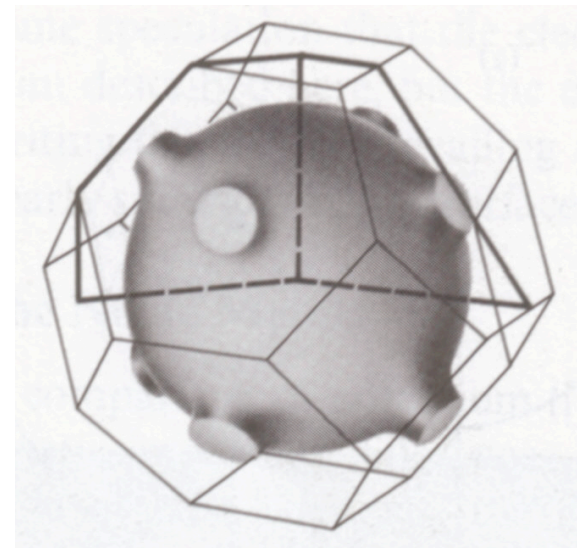
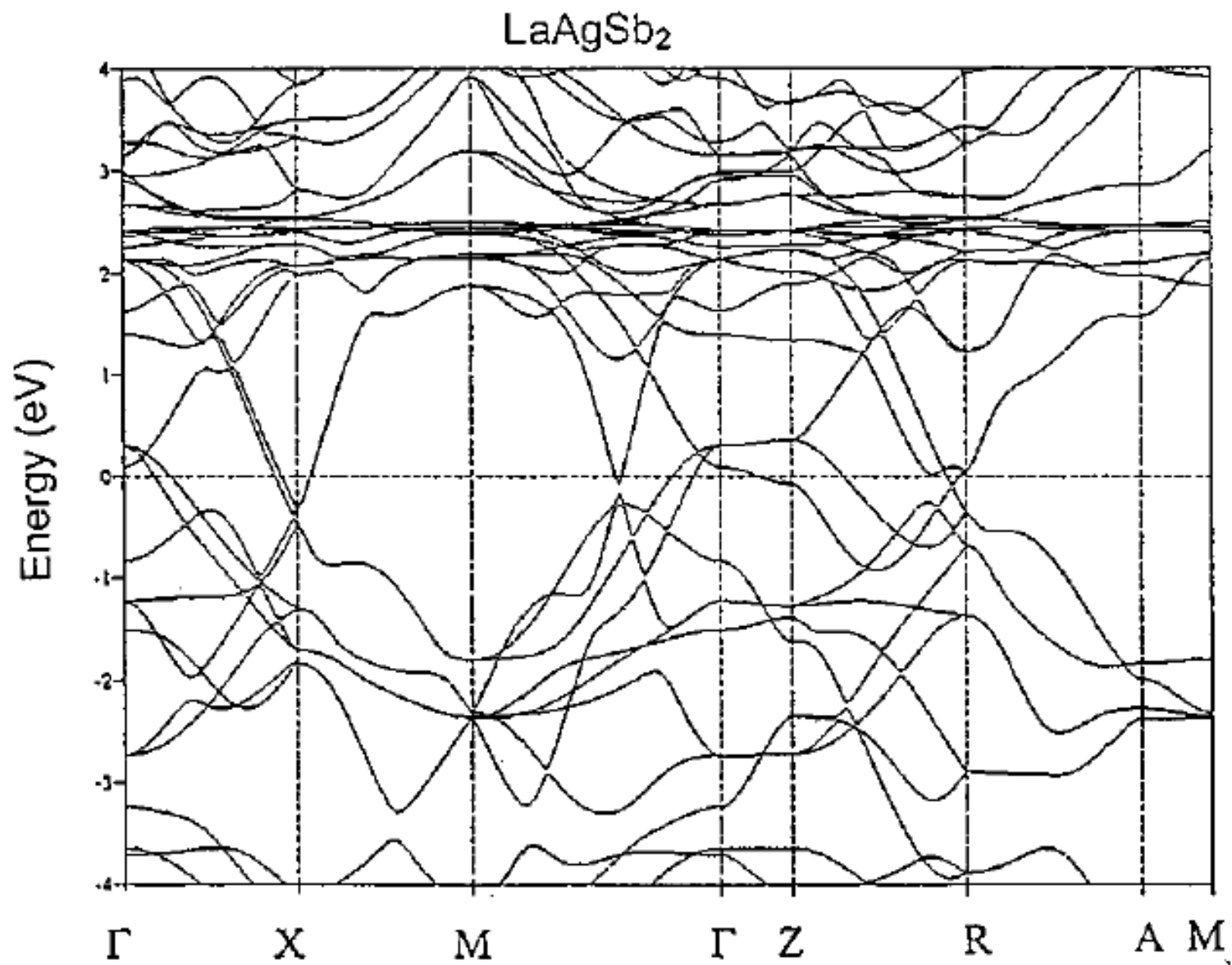


E. Rotenberg, Berkeley-Stanford Summer School 2001

# Band structure and Fermi surface - real world

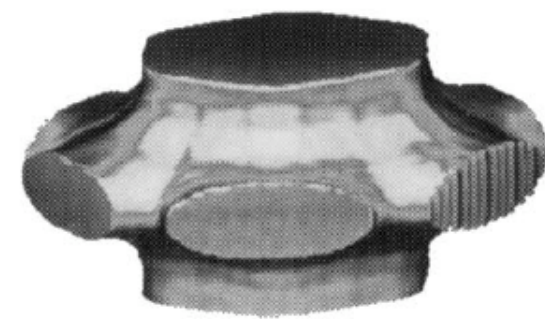
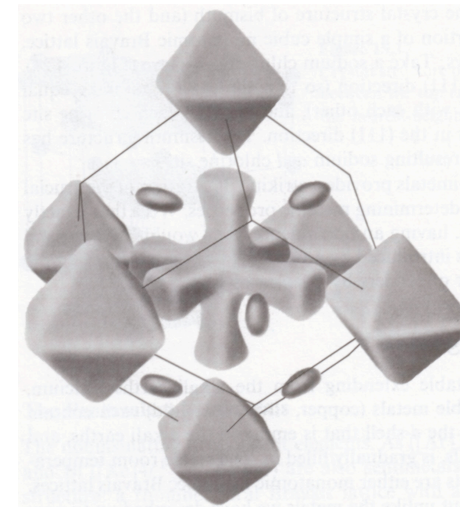
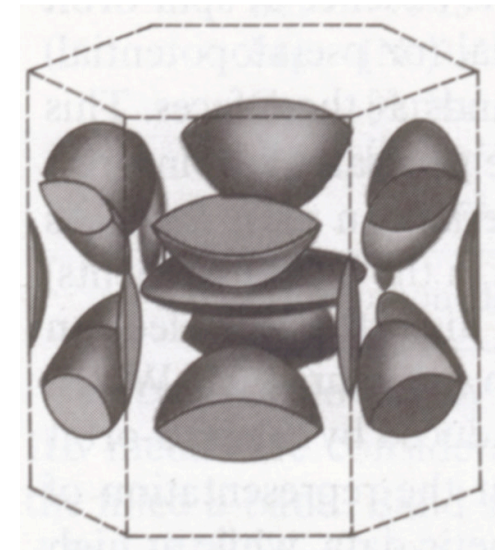
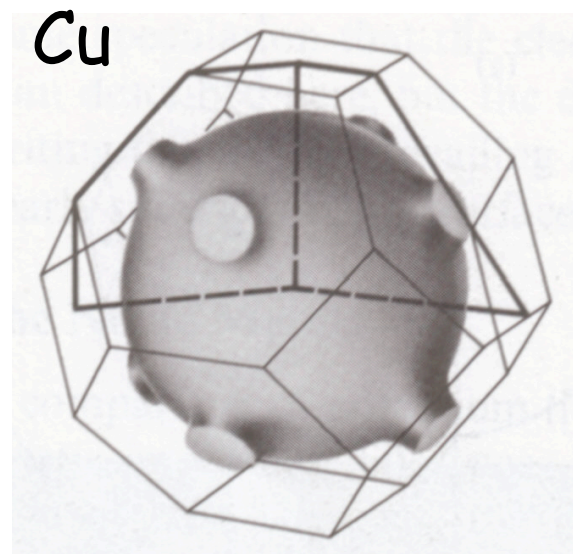
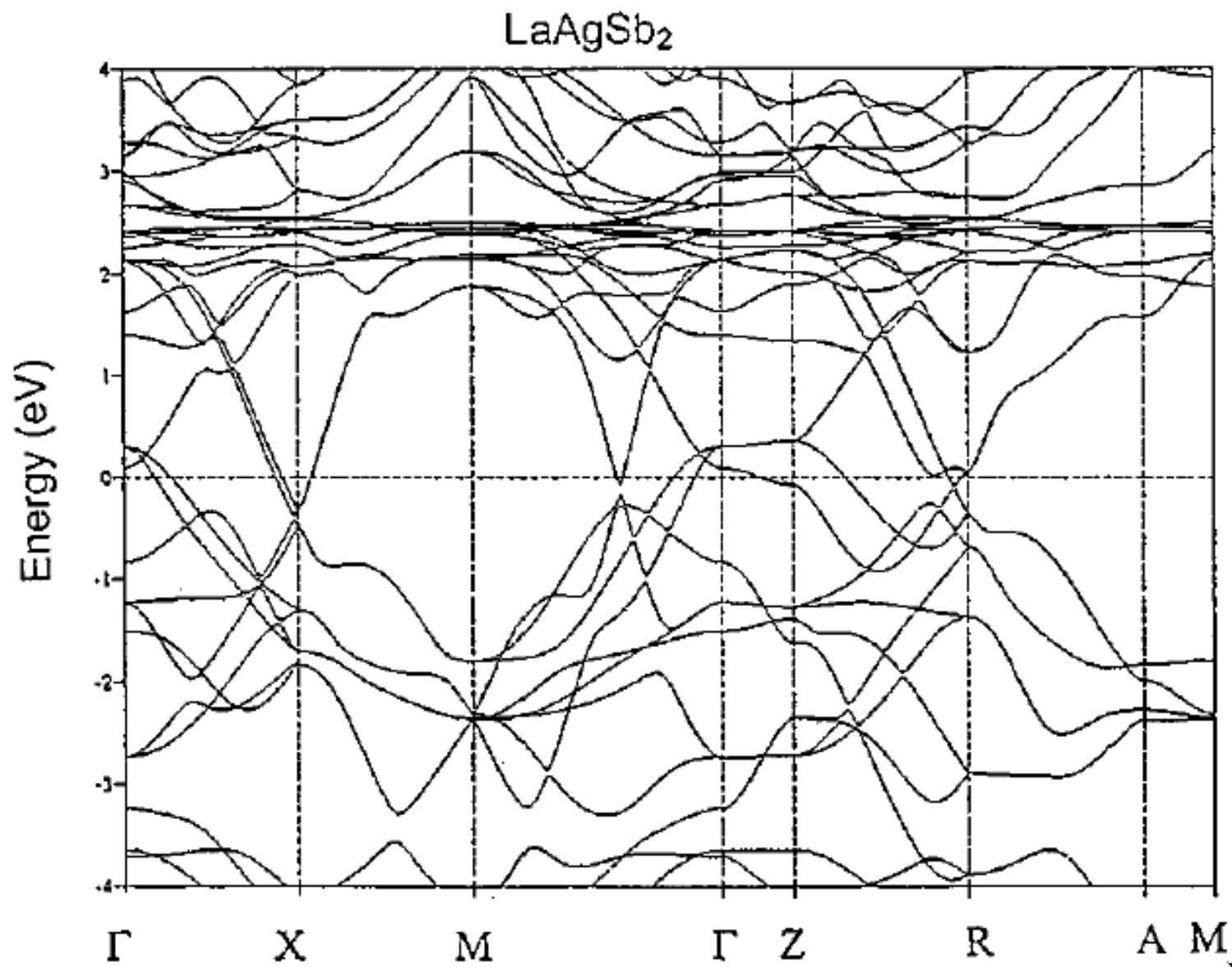


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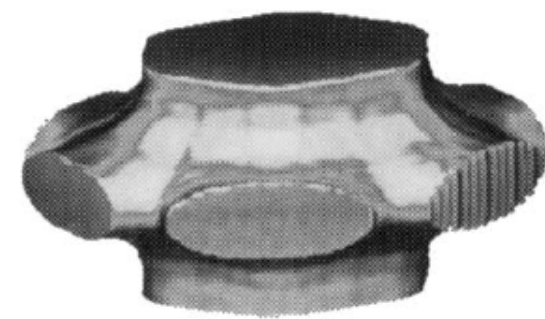
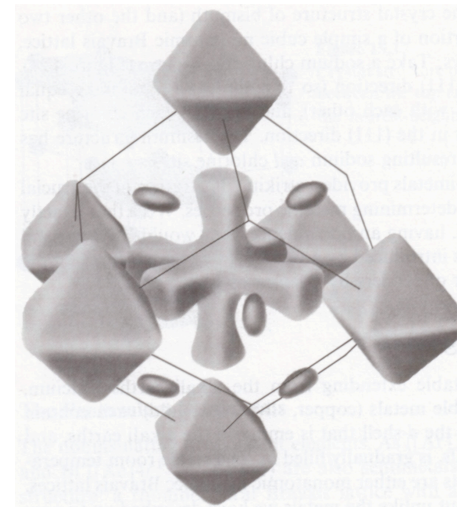
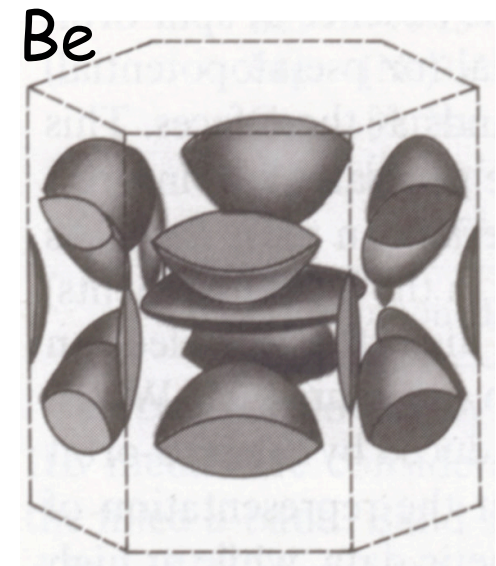
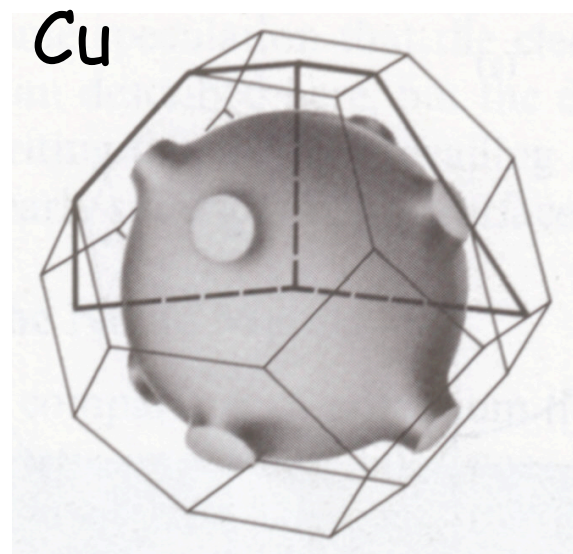
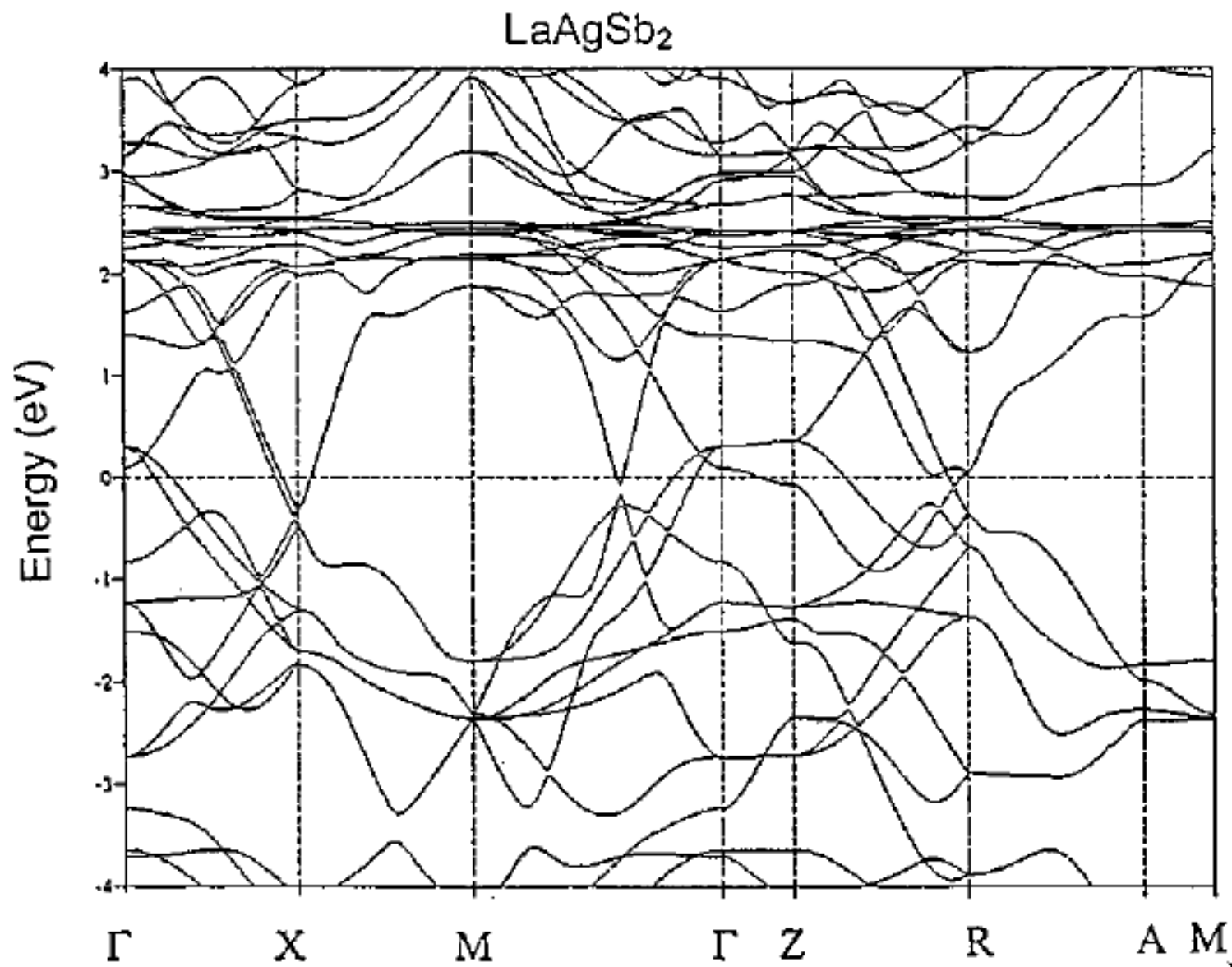




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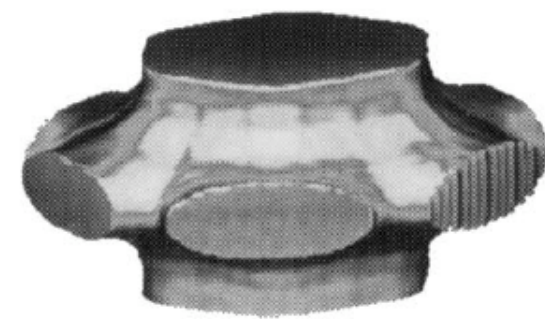
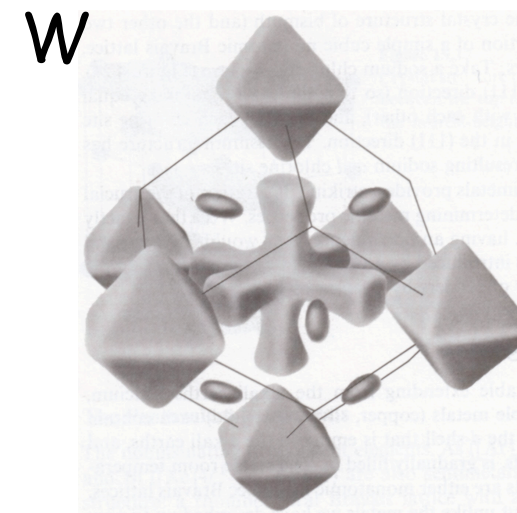
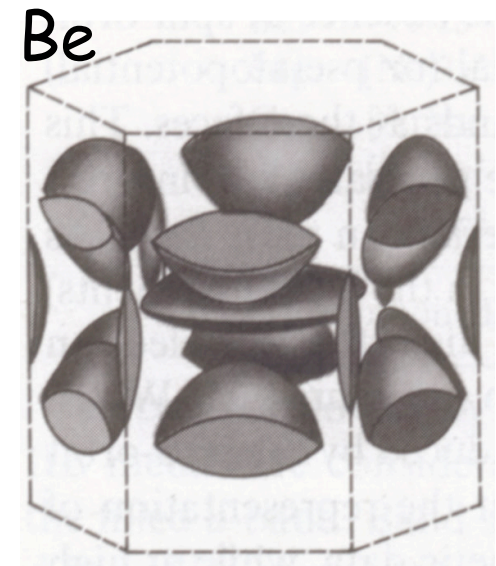
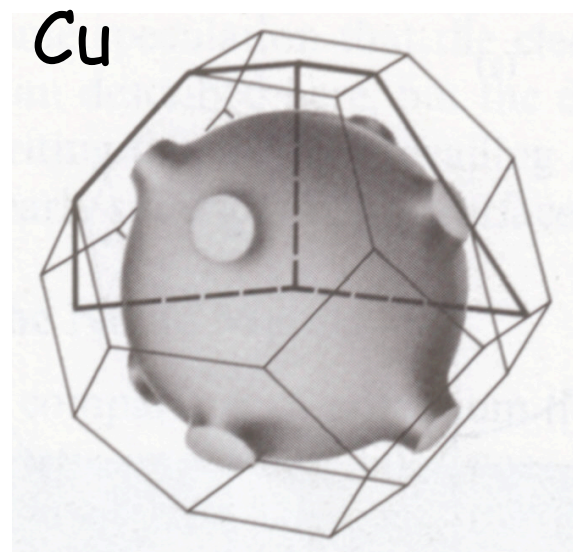
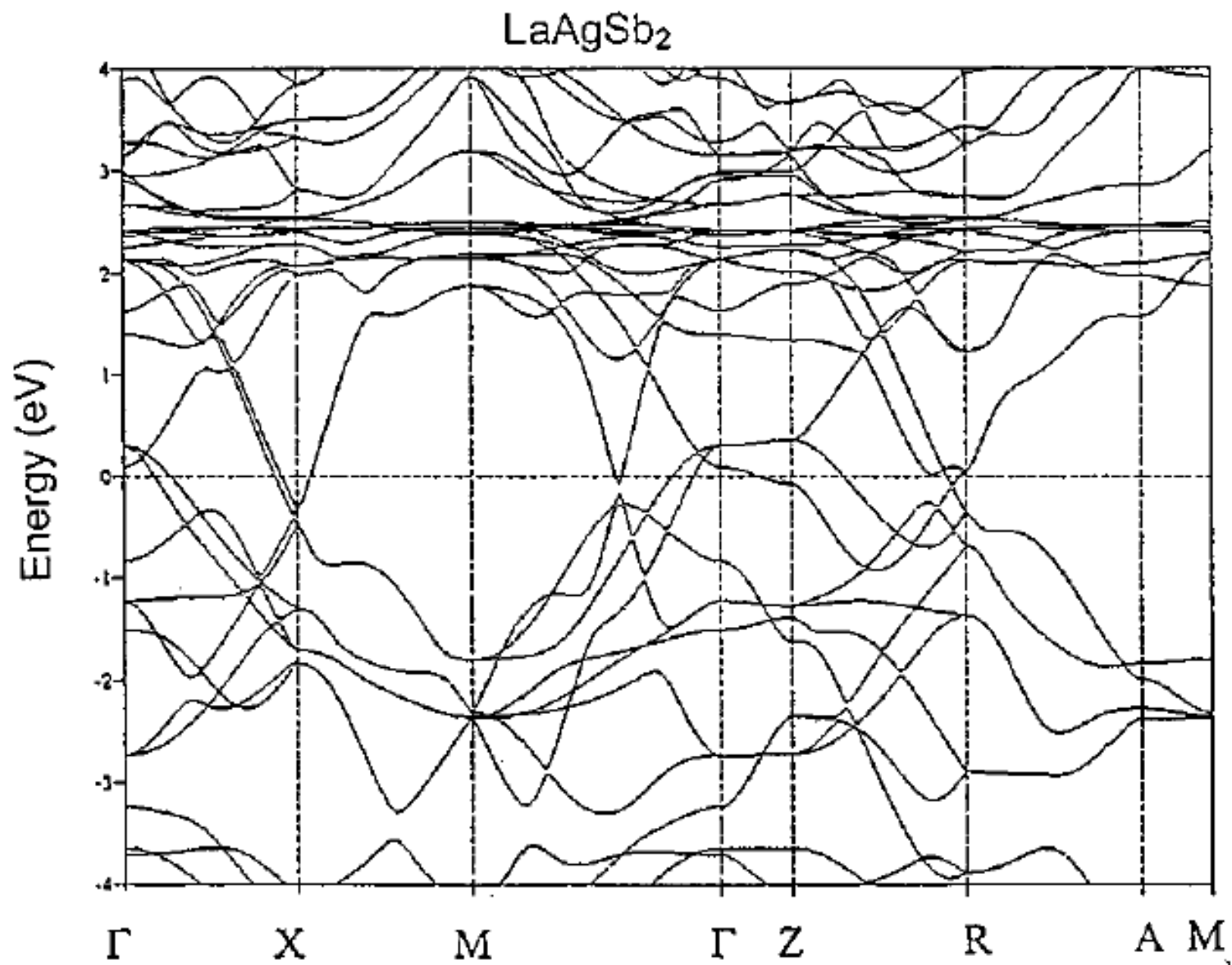


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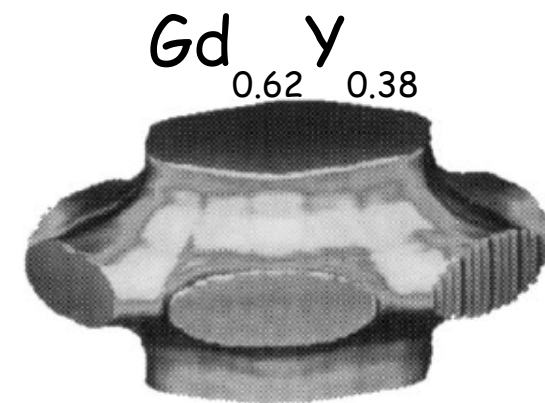
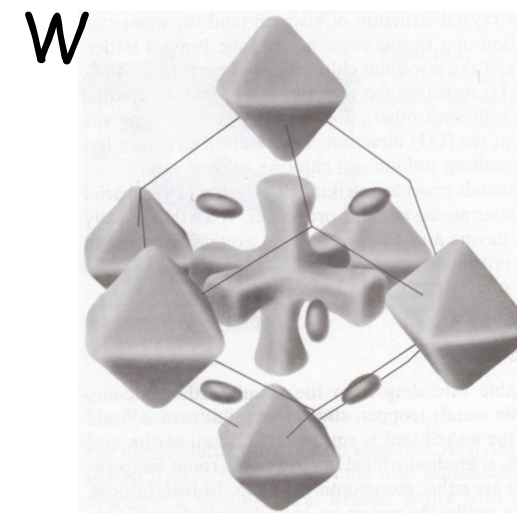
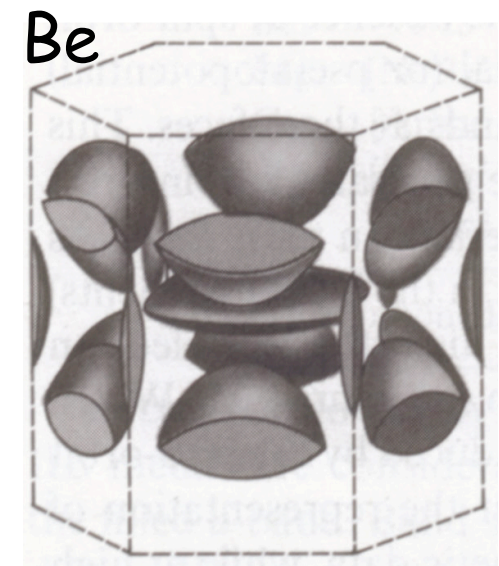
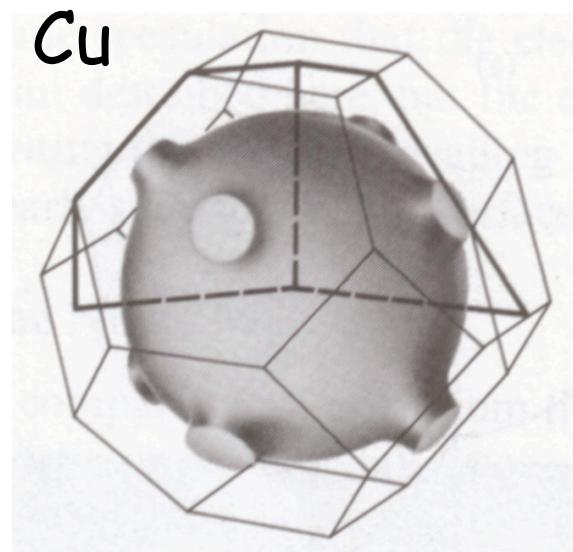
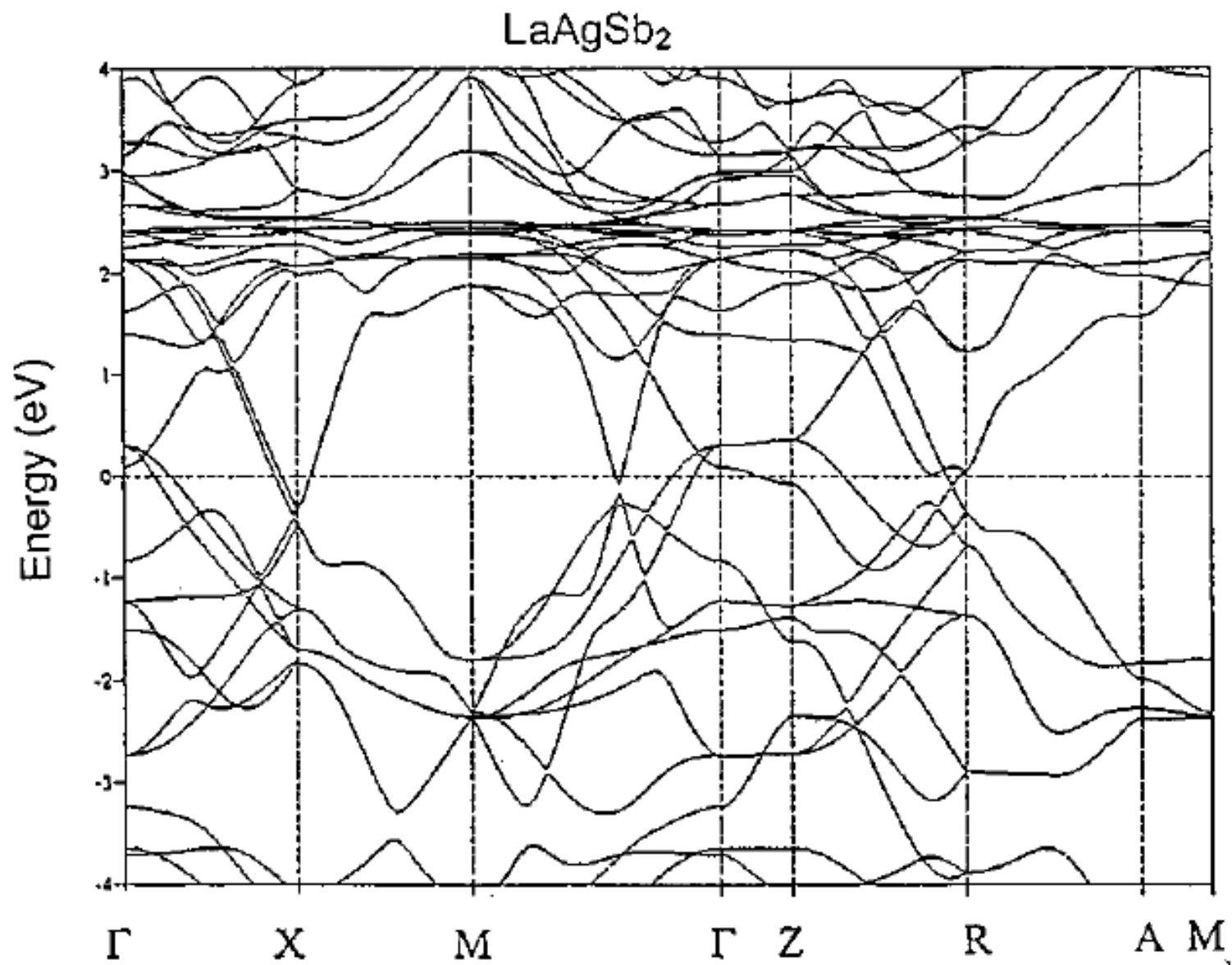




# Band structure and Fermi surface - real world



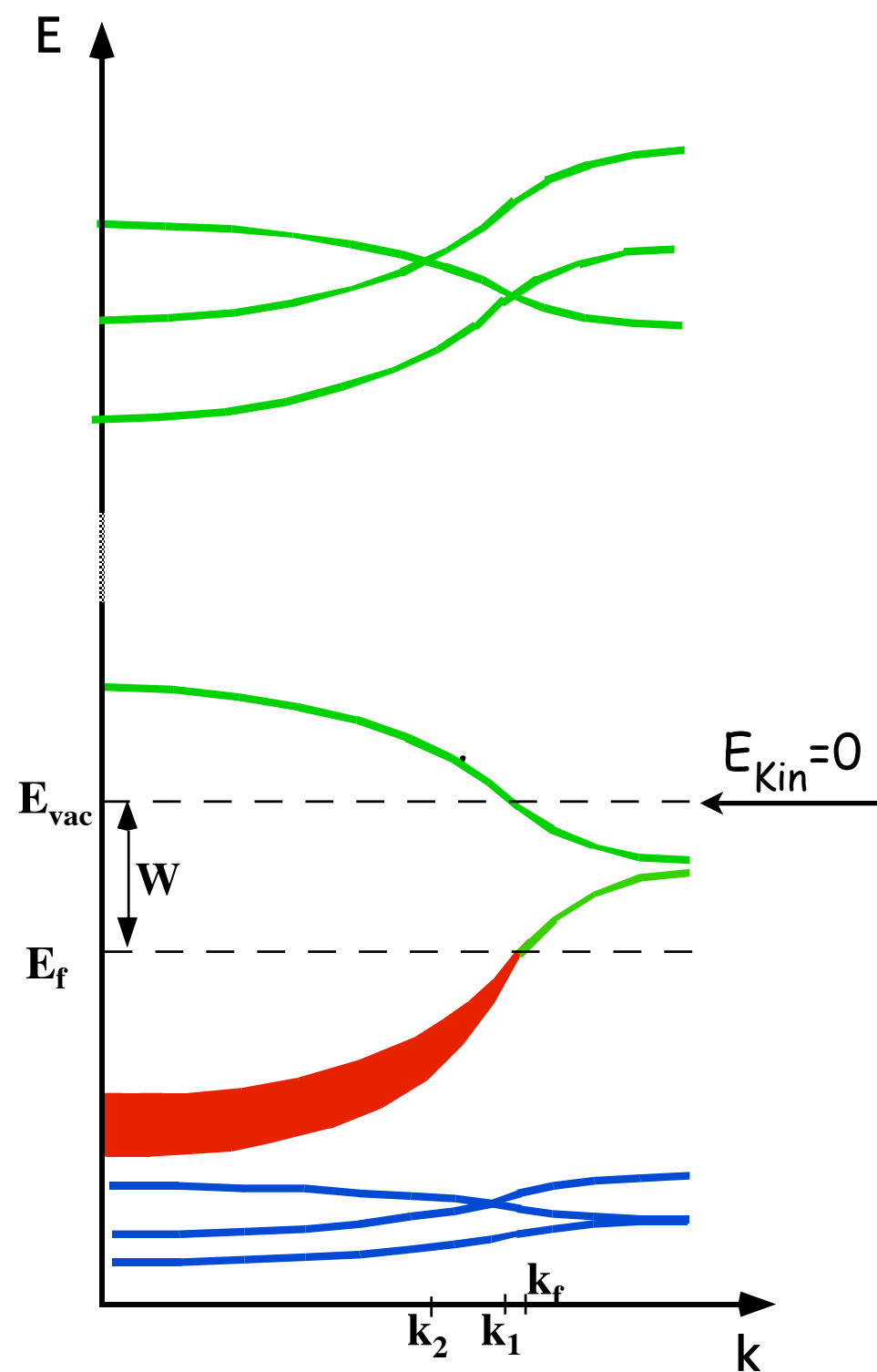
# Band structure and Fermi surface - real world





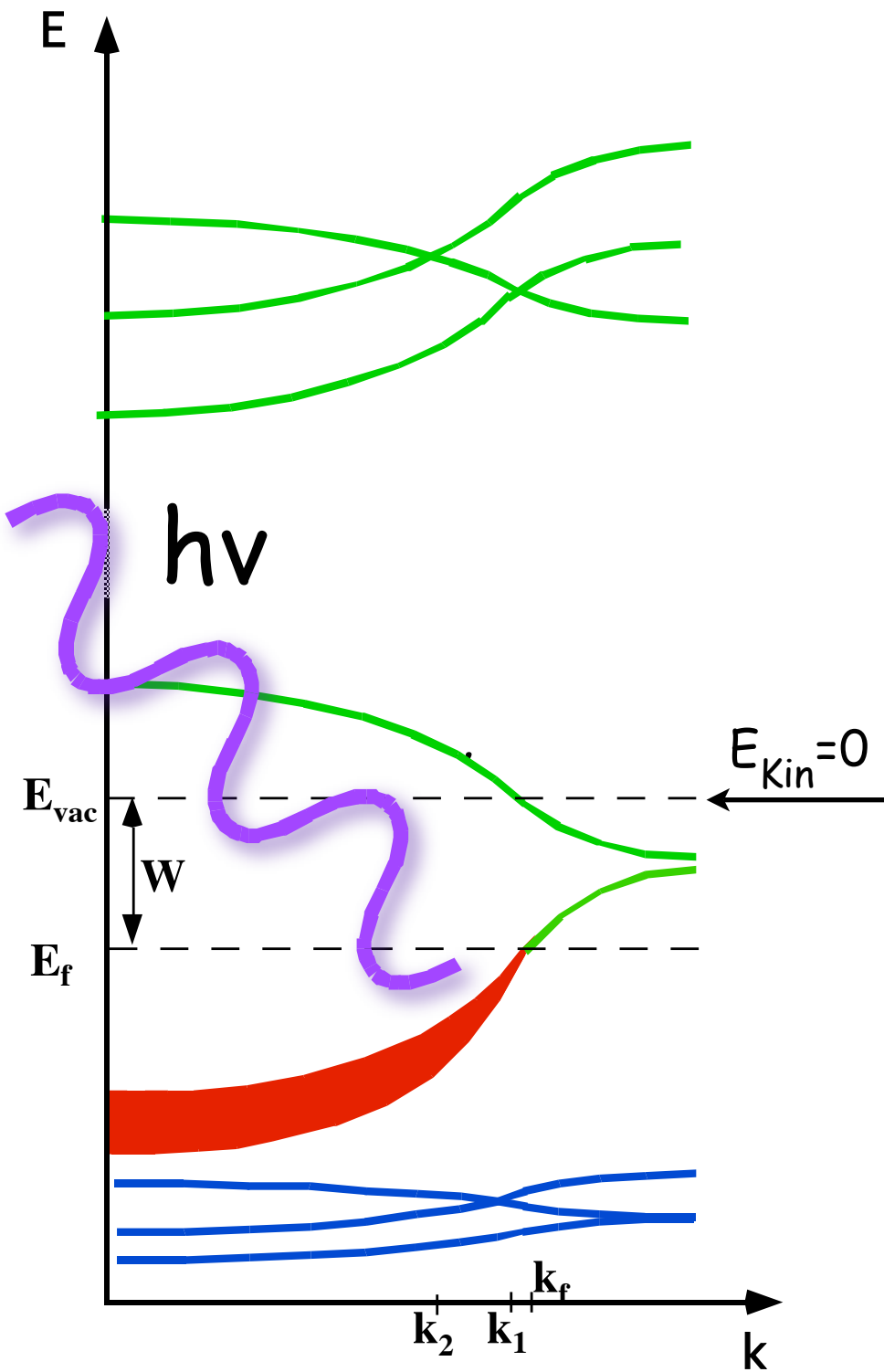
## Electronic structure

## ARPES spectra



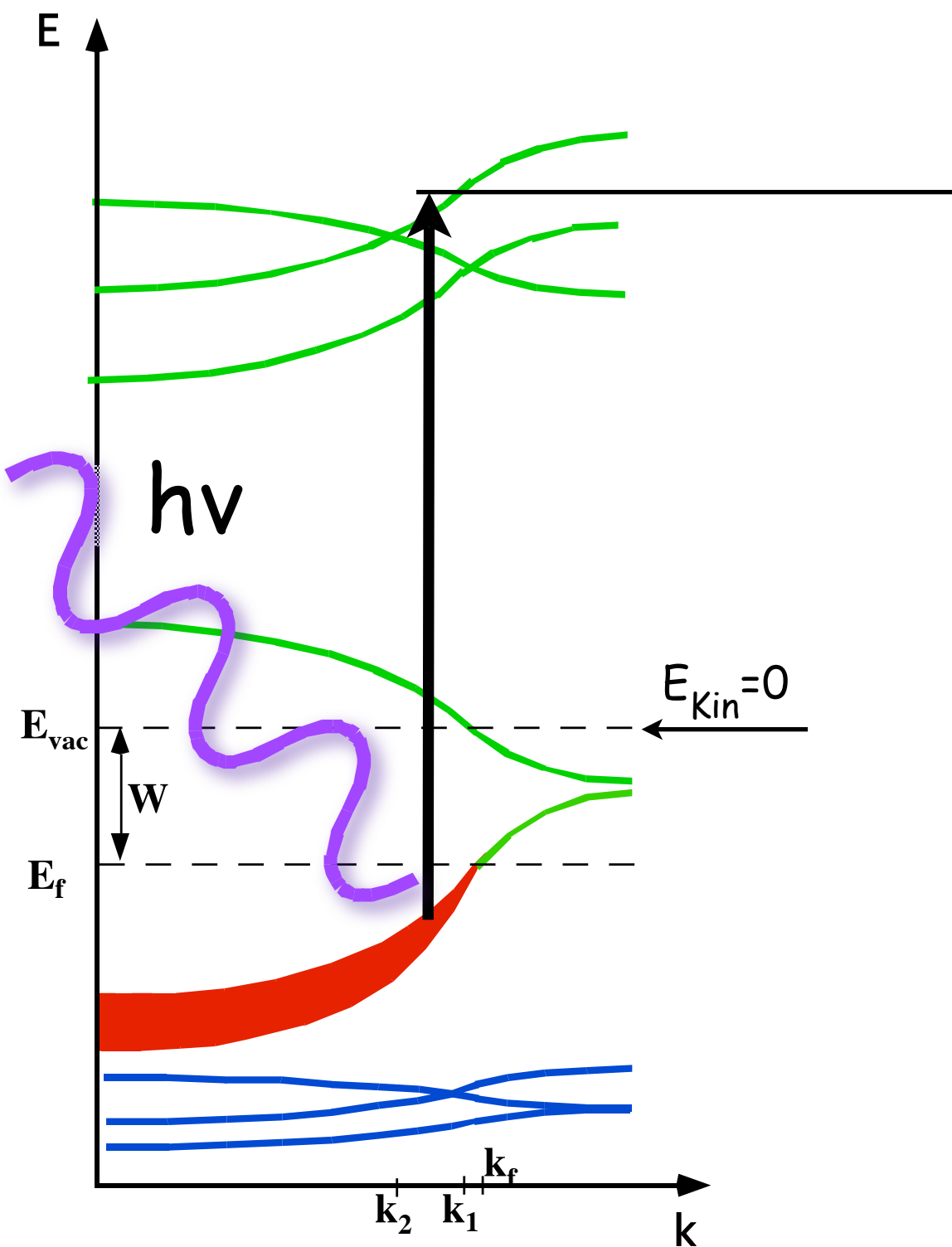
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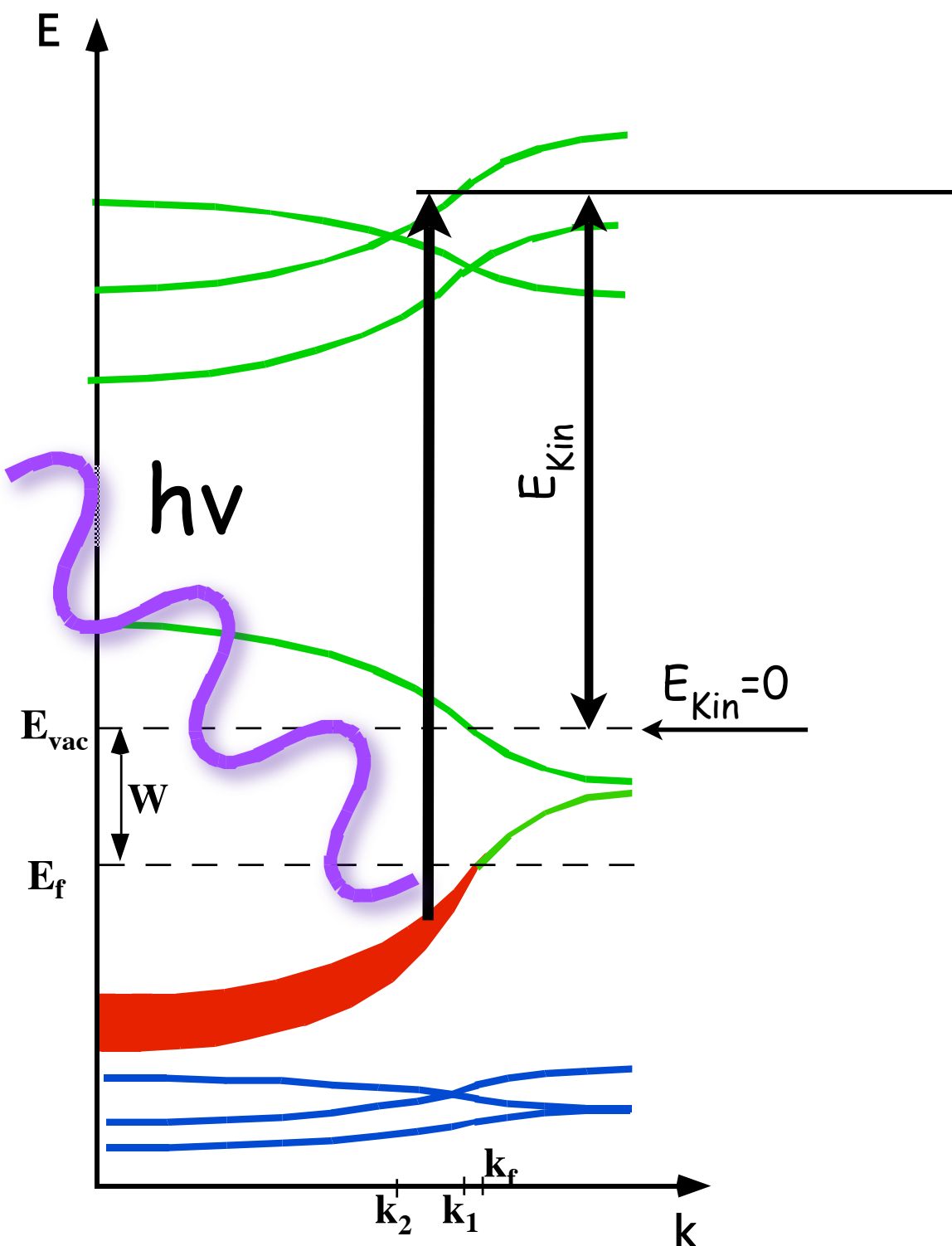
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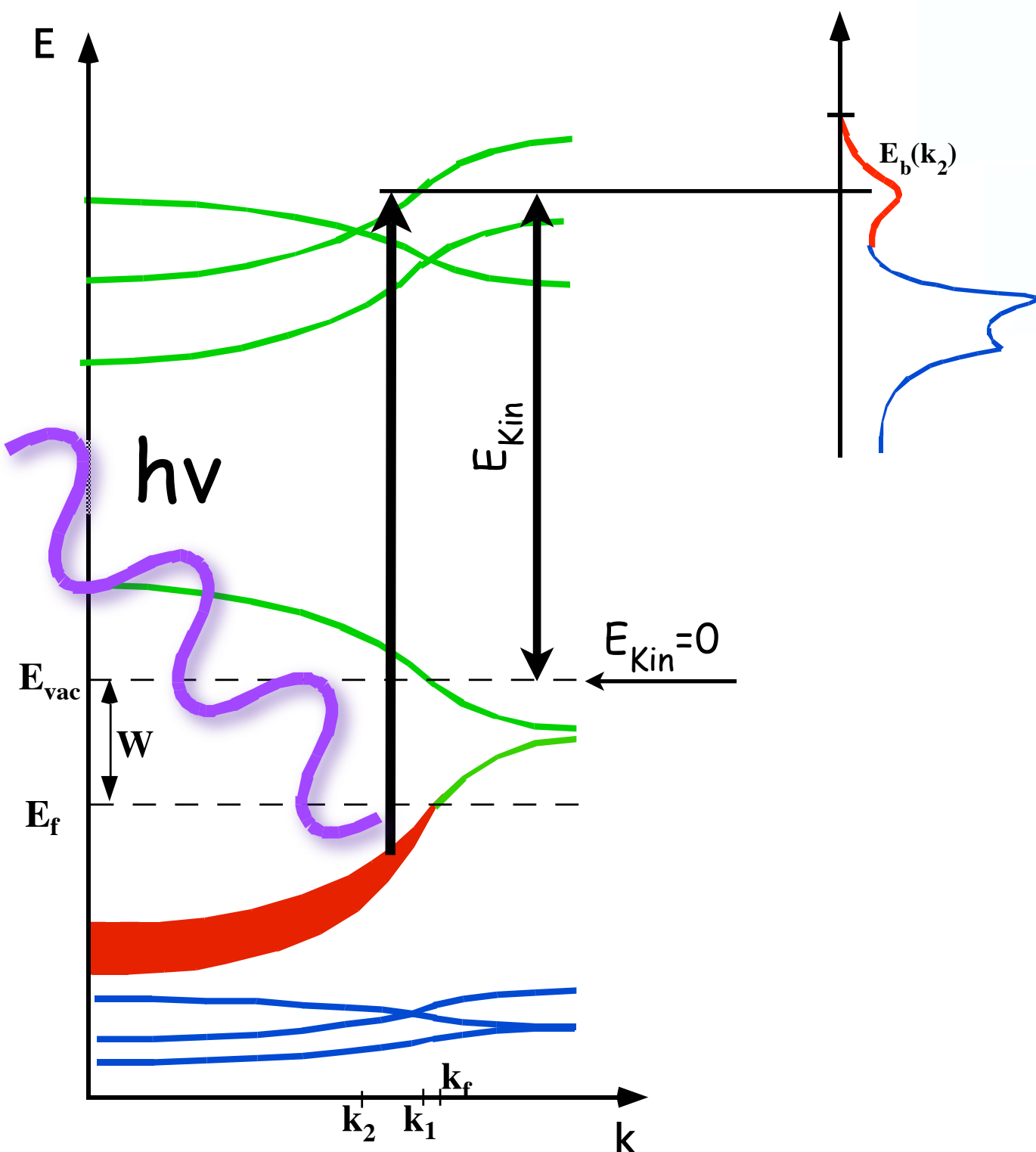
# Electronic structure

# ARPES spectra



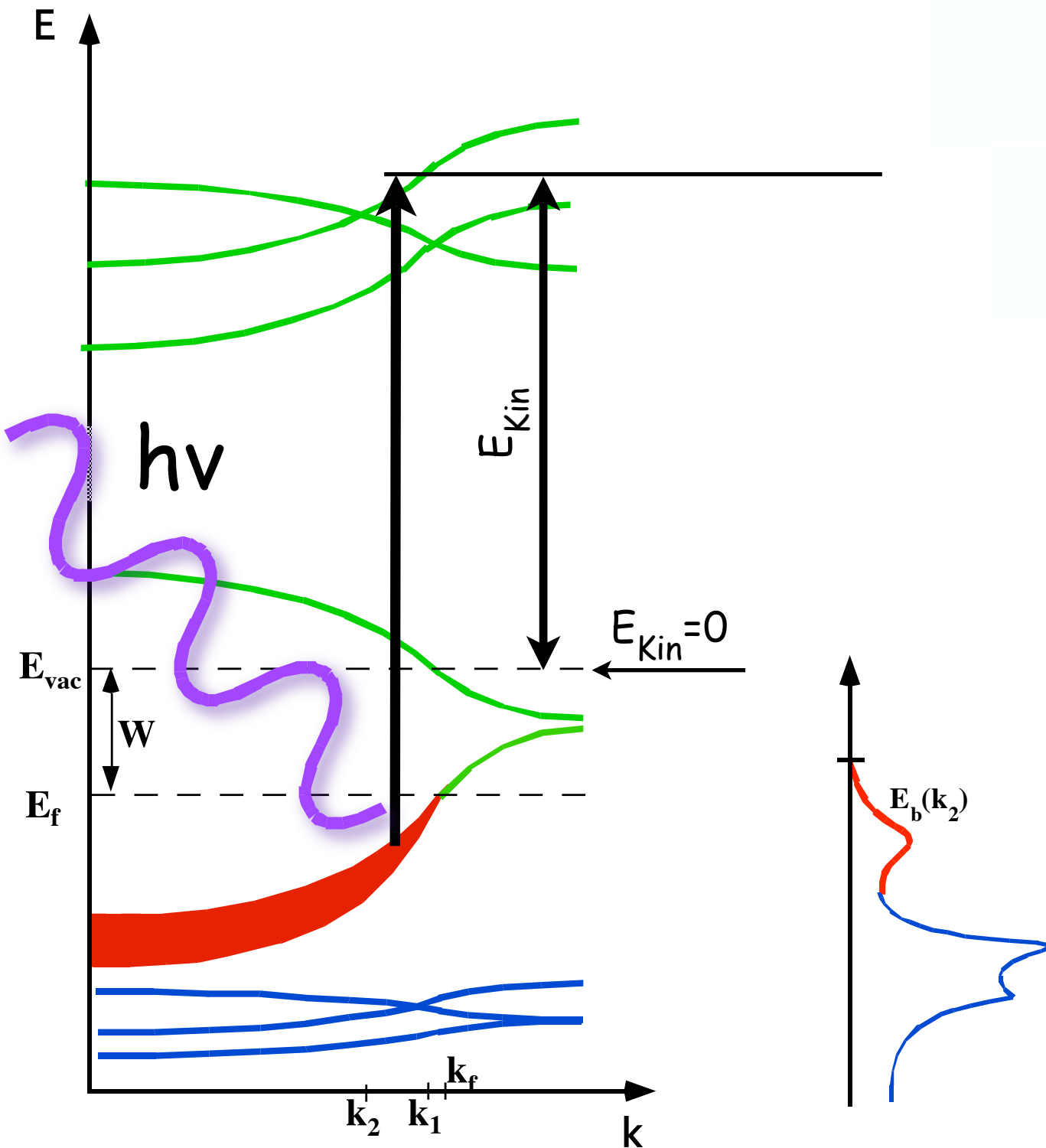
Electronic structure

ARPES spectra



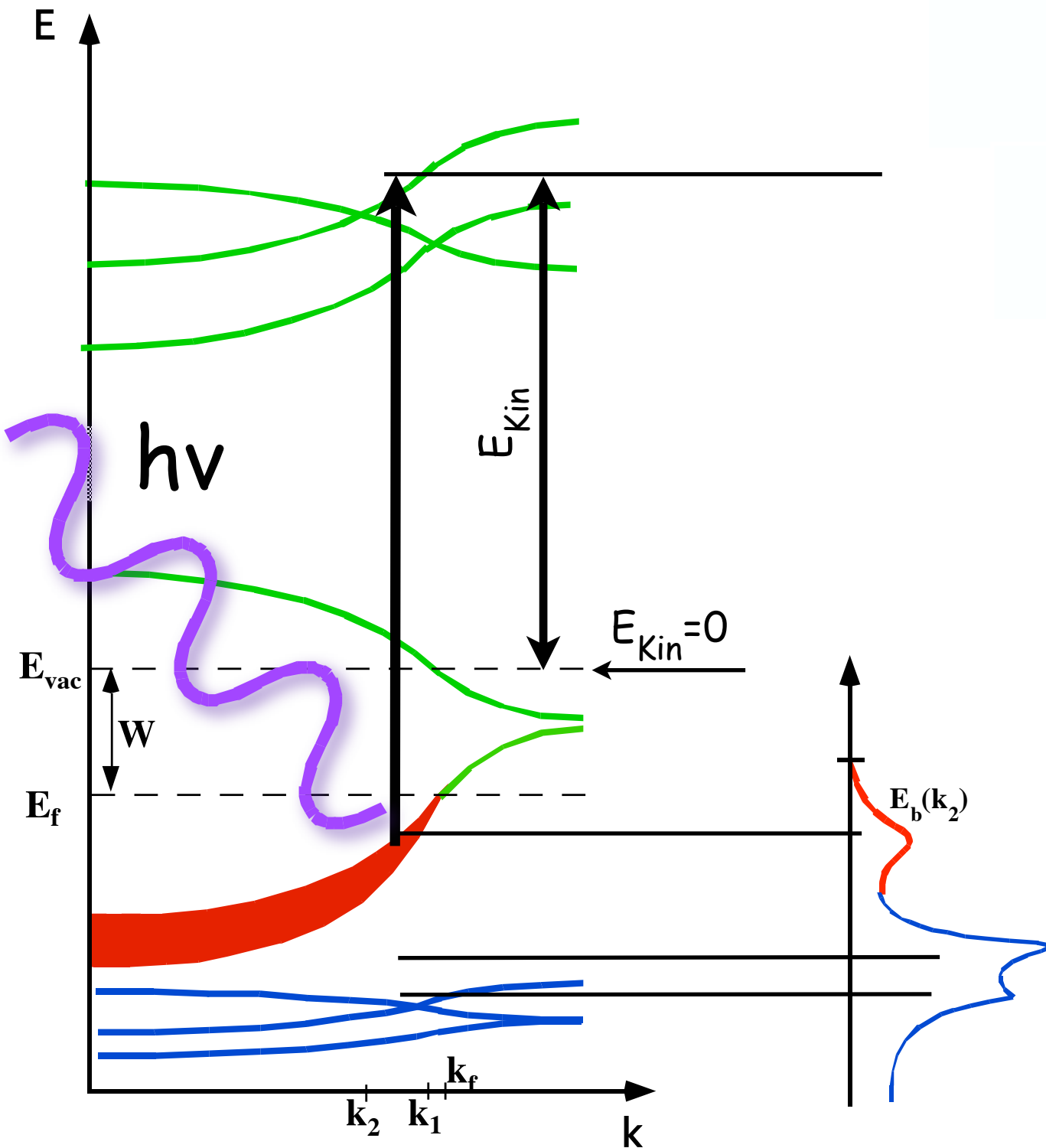
# Electronic structure

# ARPES spectra



# Electronic structure

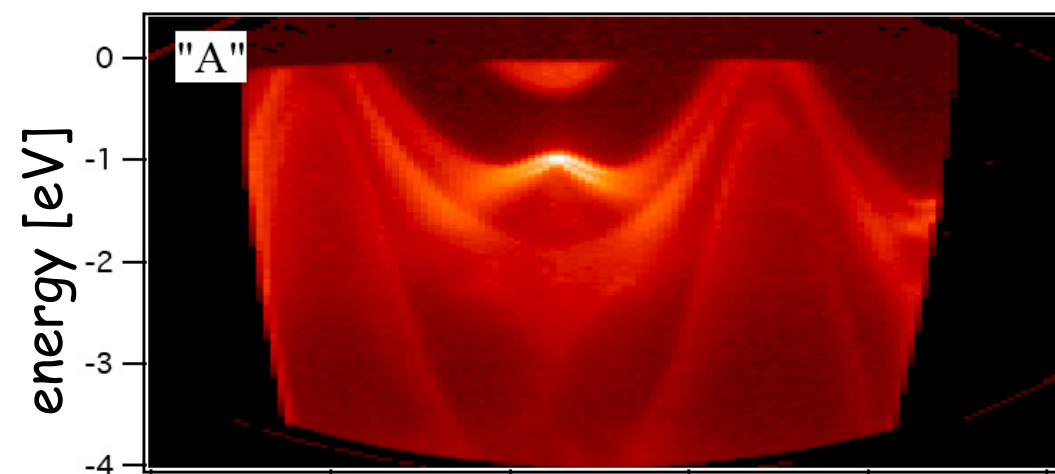
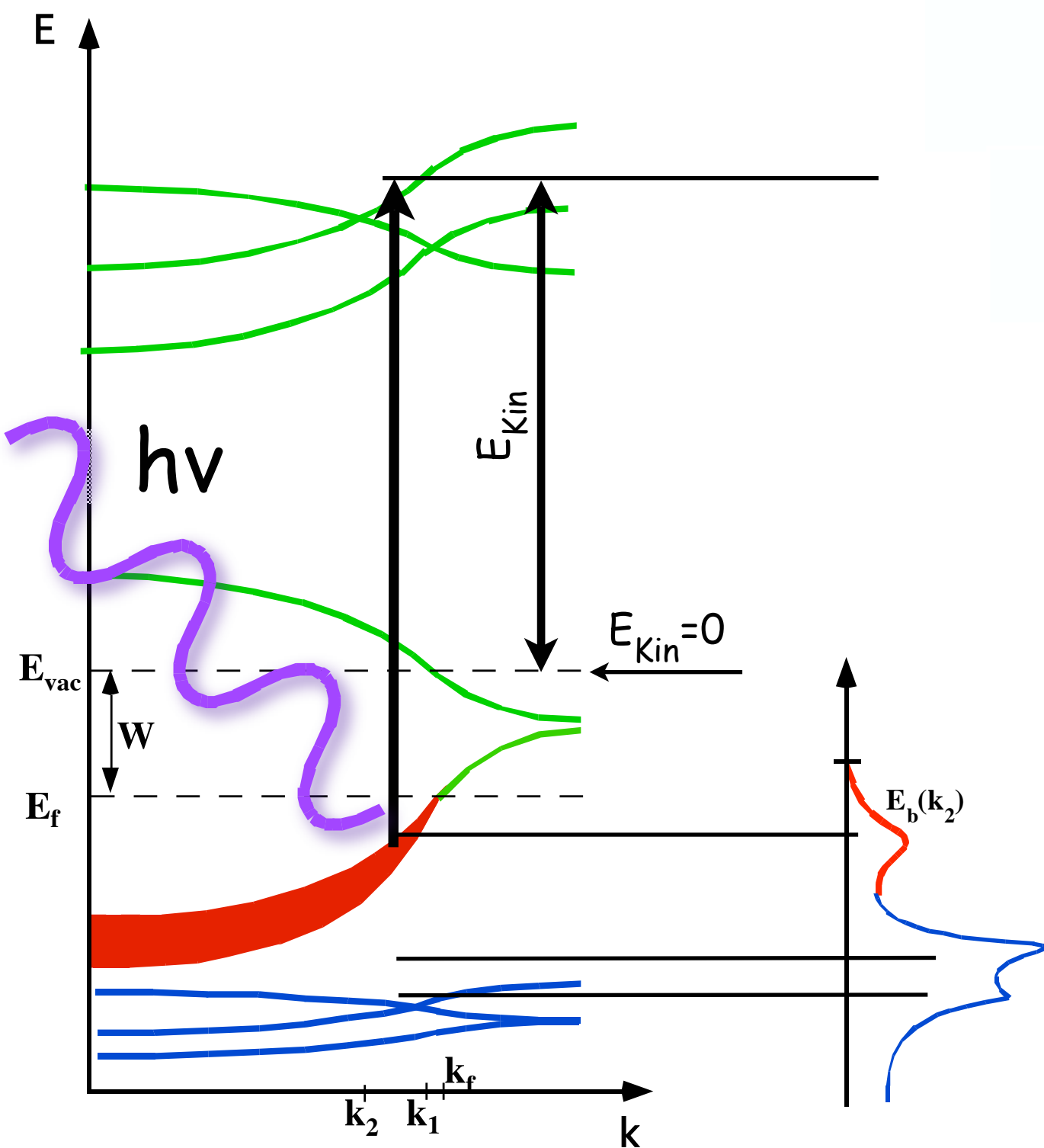
# ARPES spectra





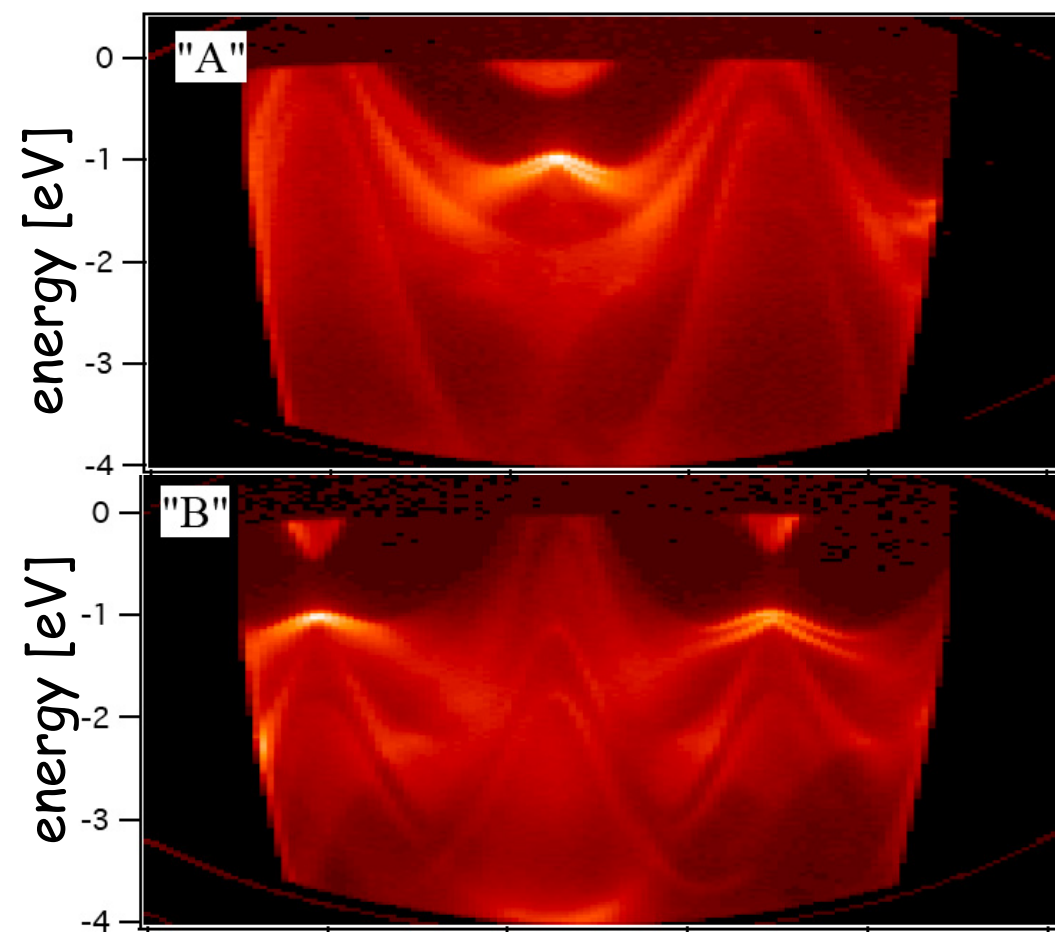
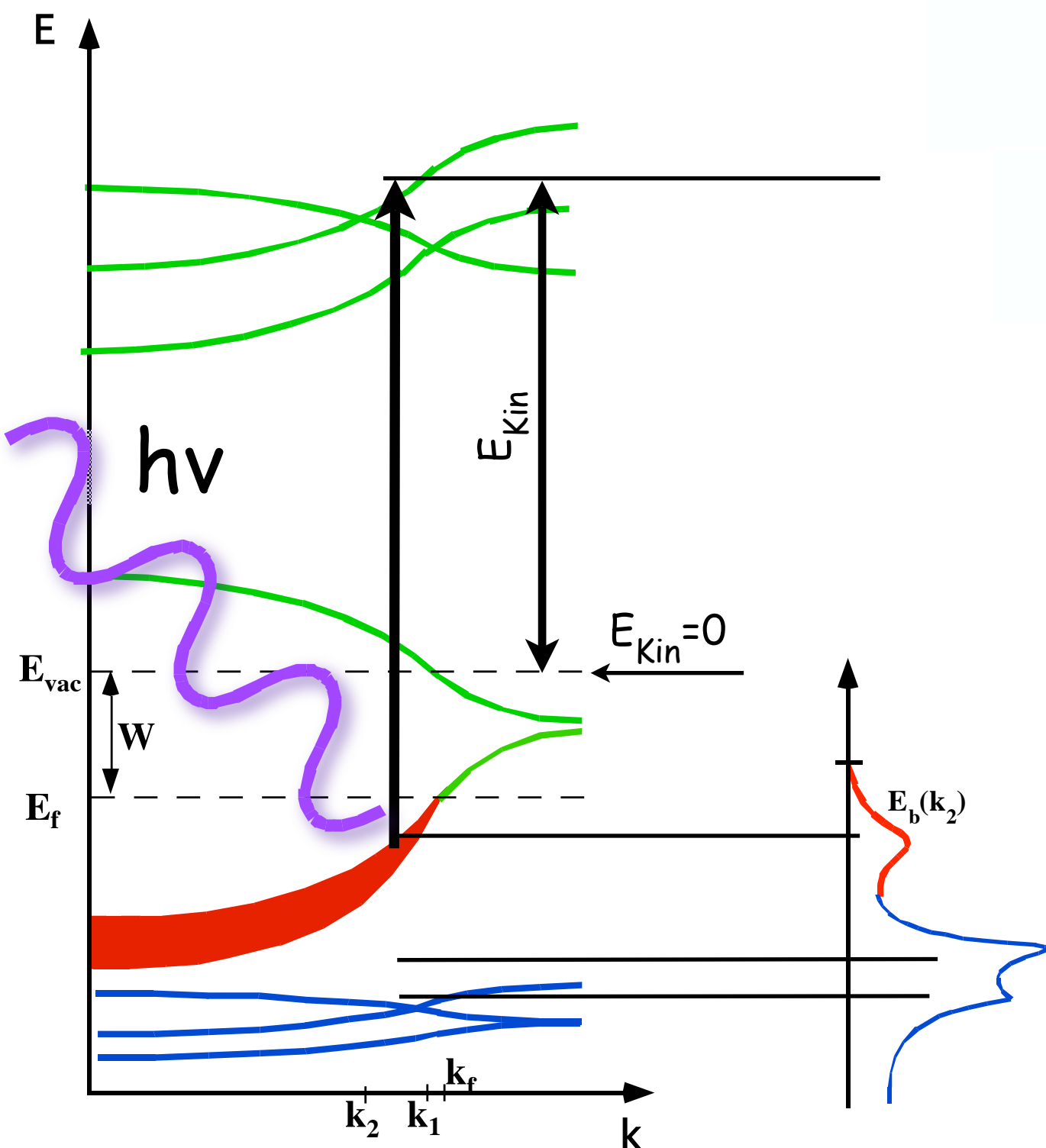
Electronic structure

ARPES spectra



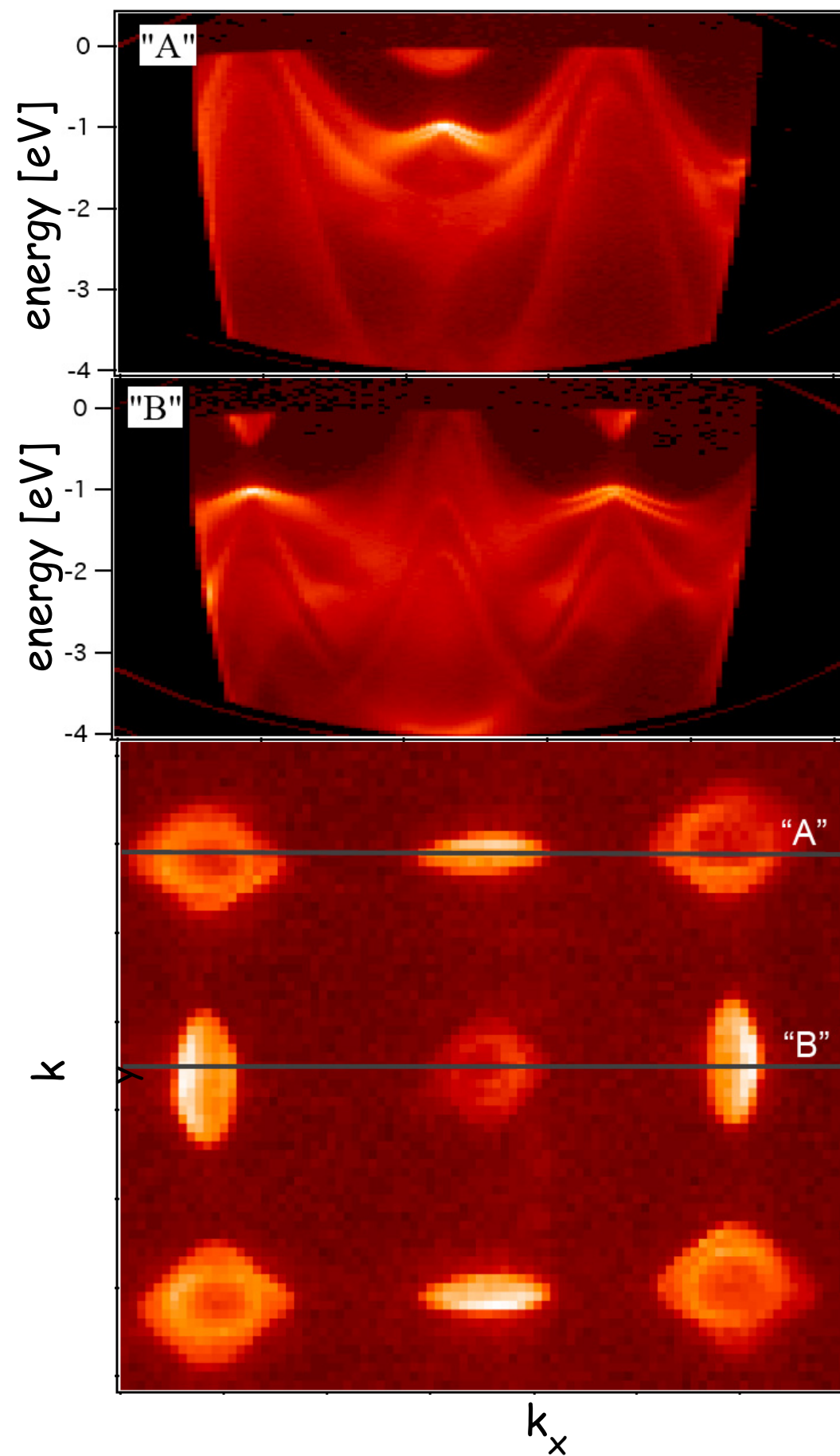
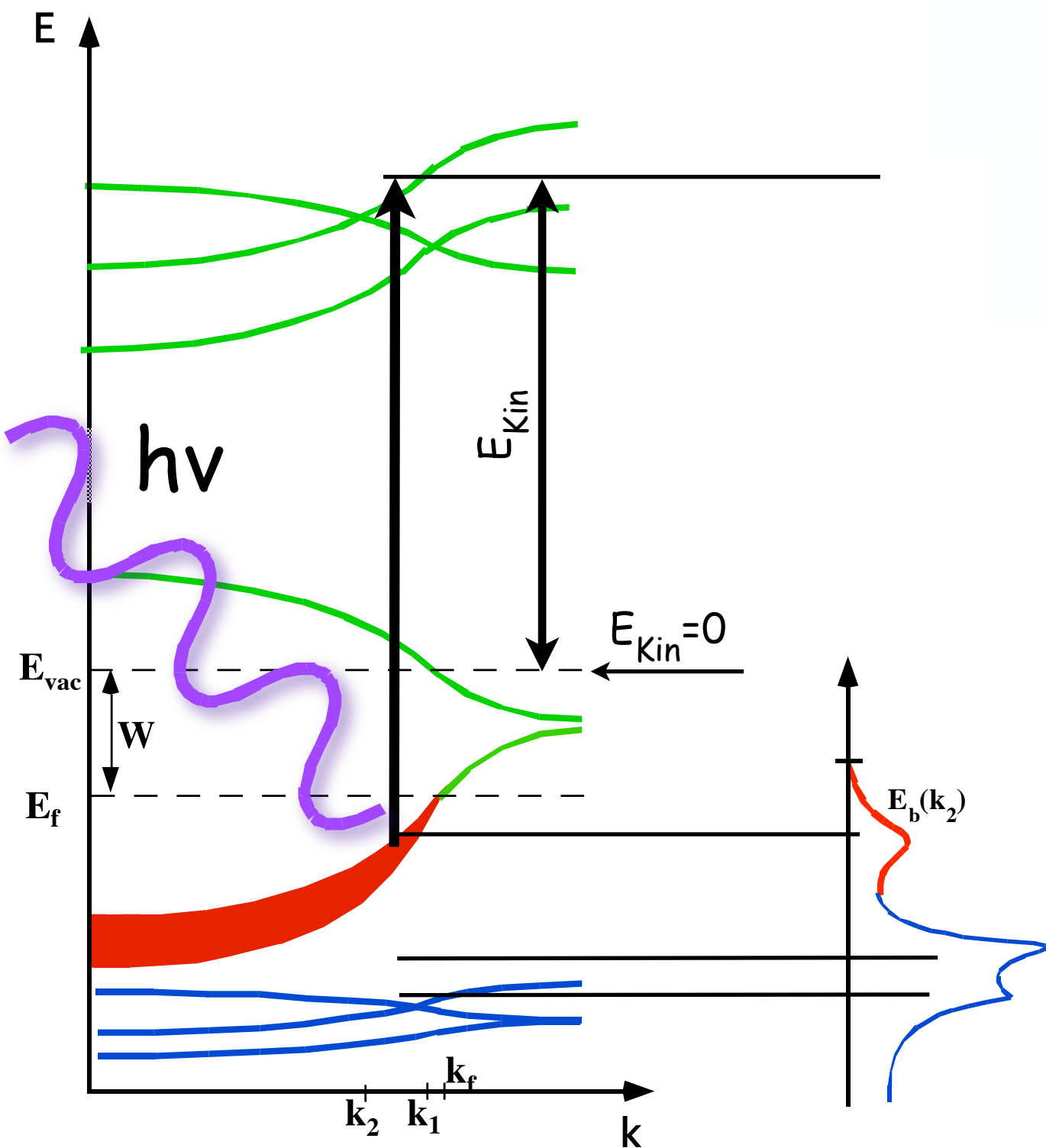
# Electronic structure

# ARPES spectra

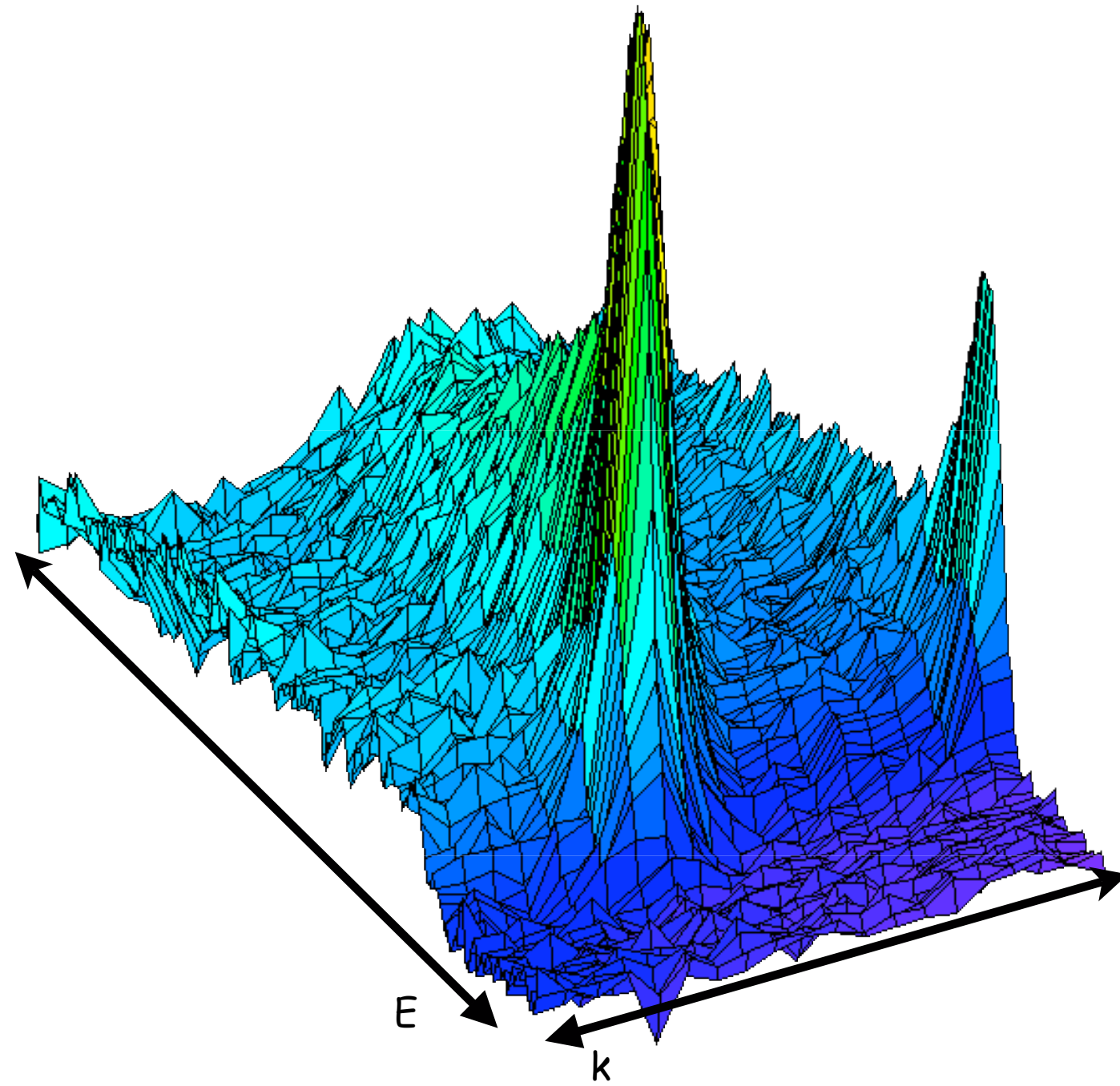


# Electronic structure

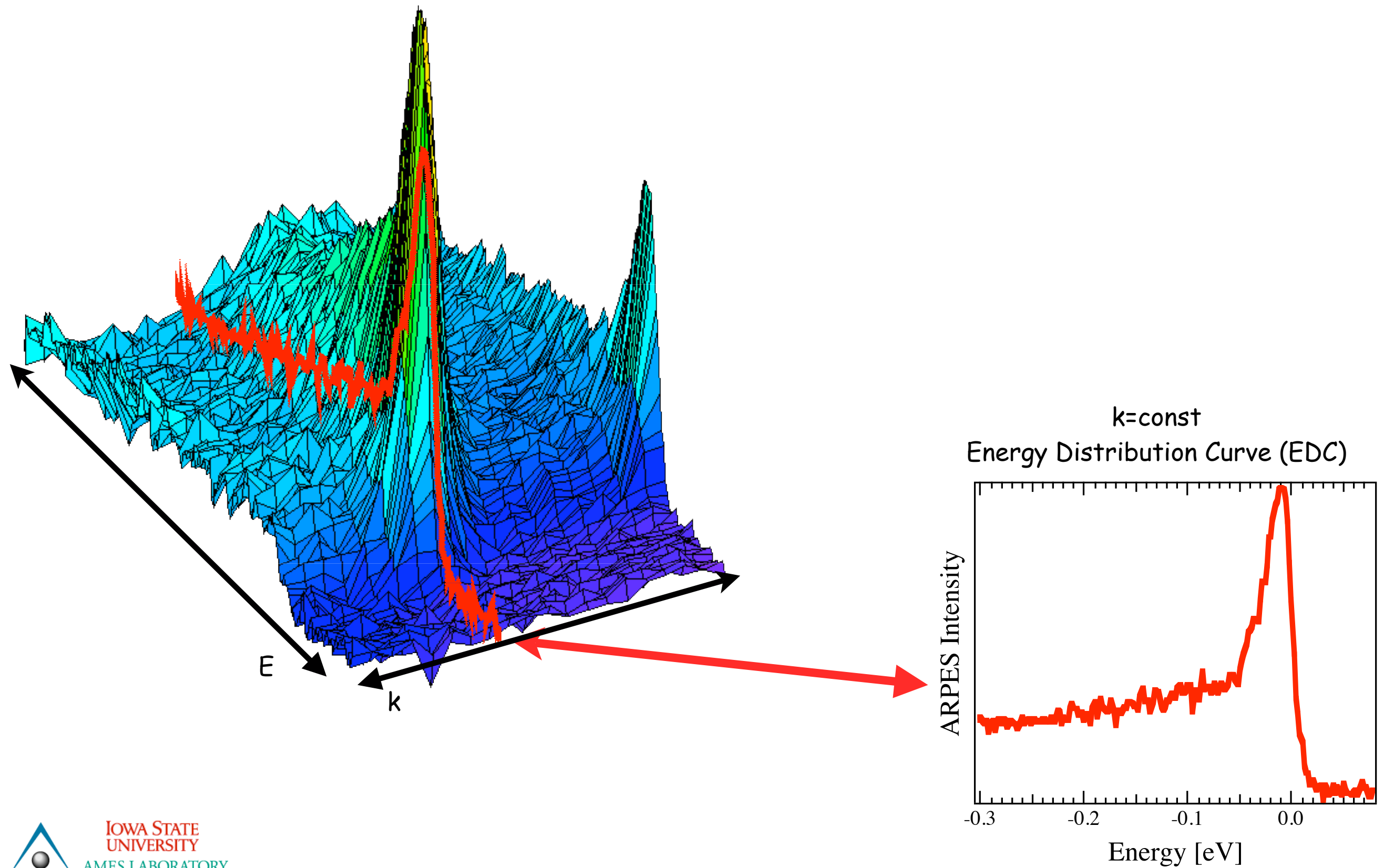
# ARPES spectra



# Typical ARPES data:

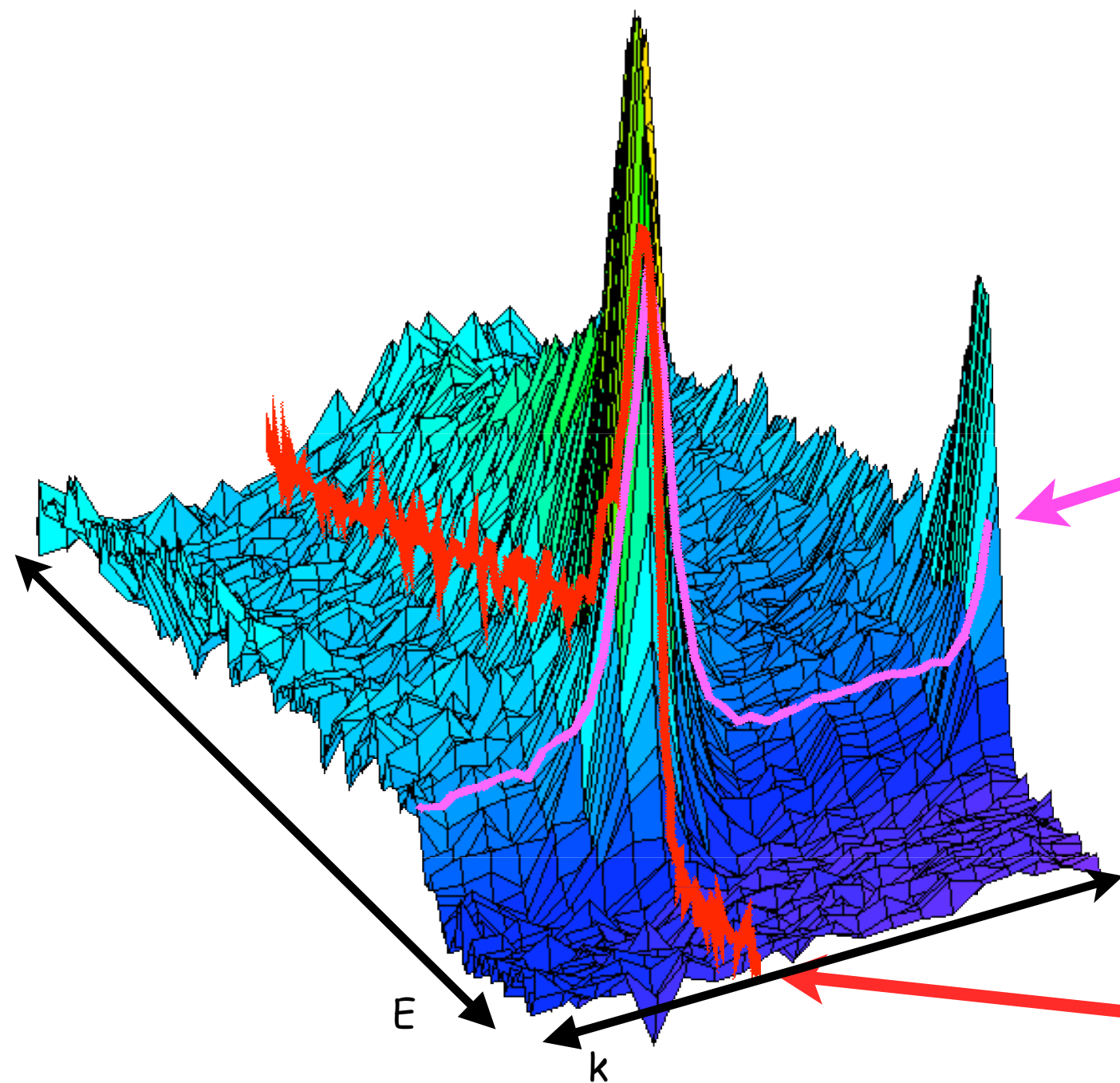


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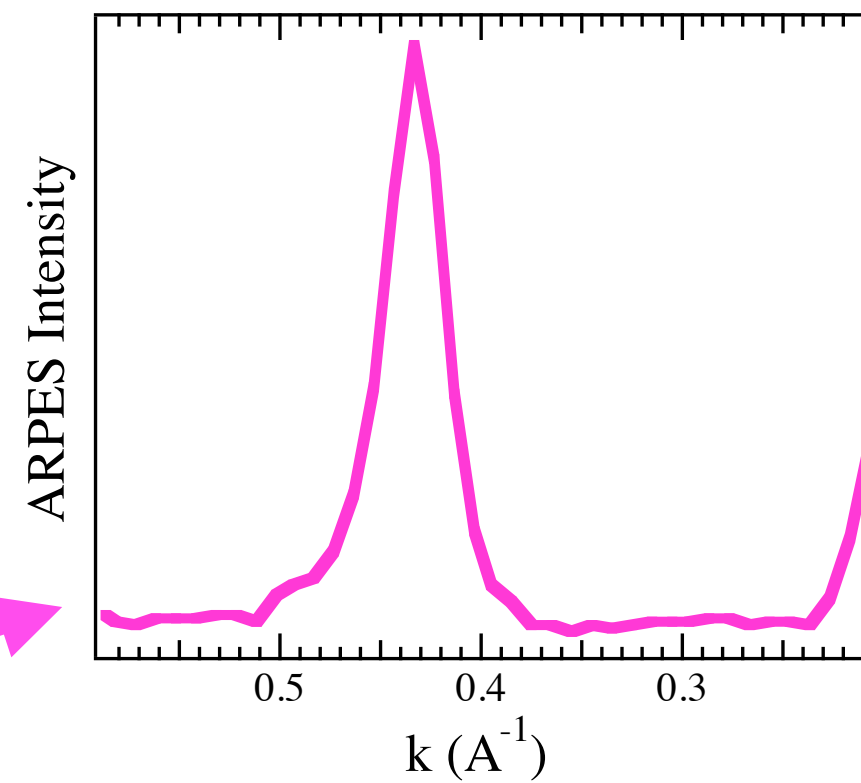




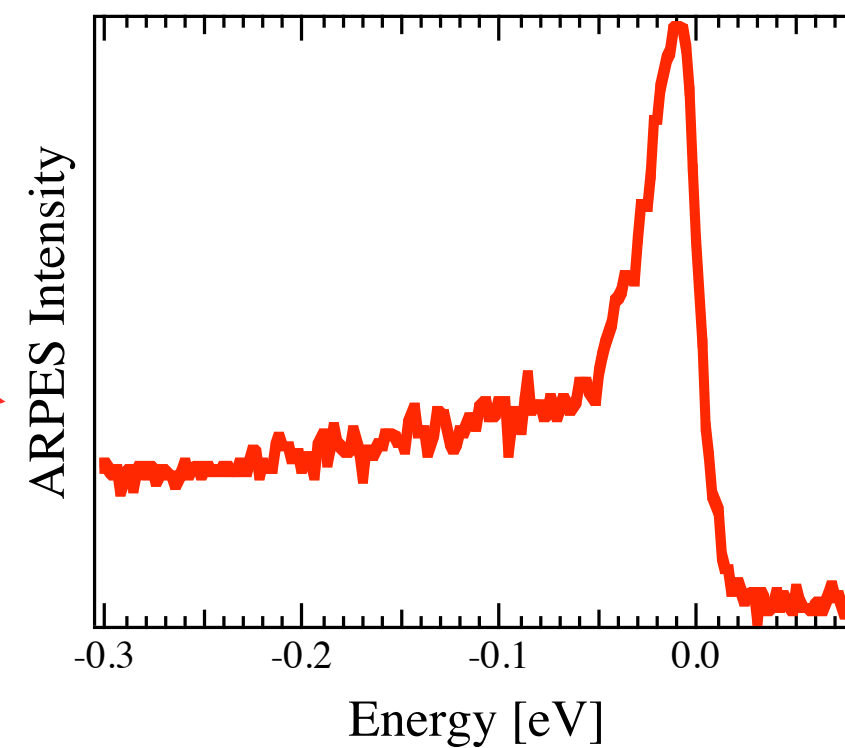
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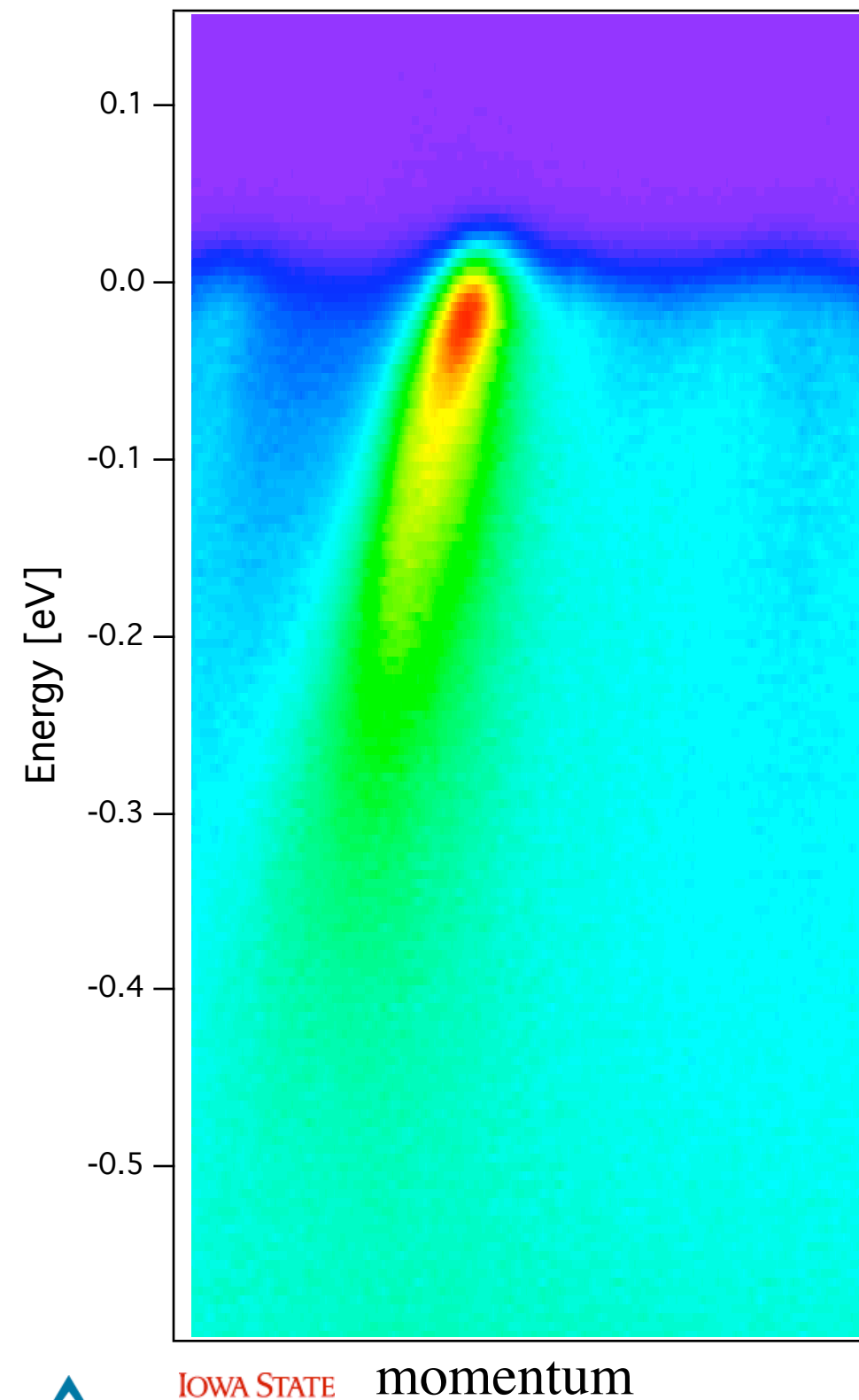
$E = \text{const}$   
Momentum Distribution Curve (MDC)



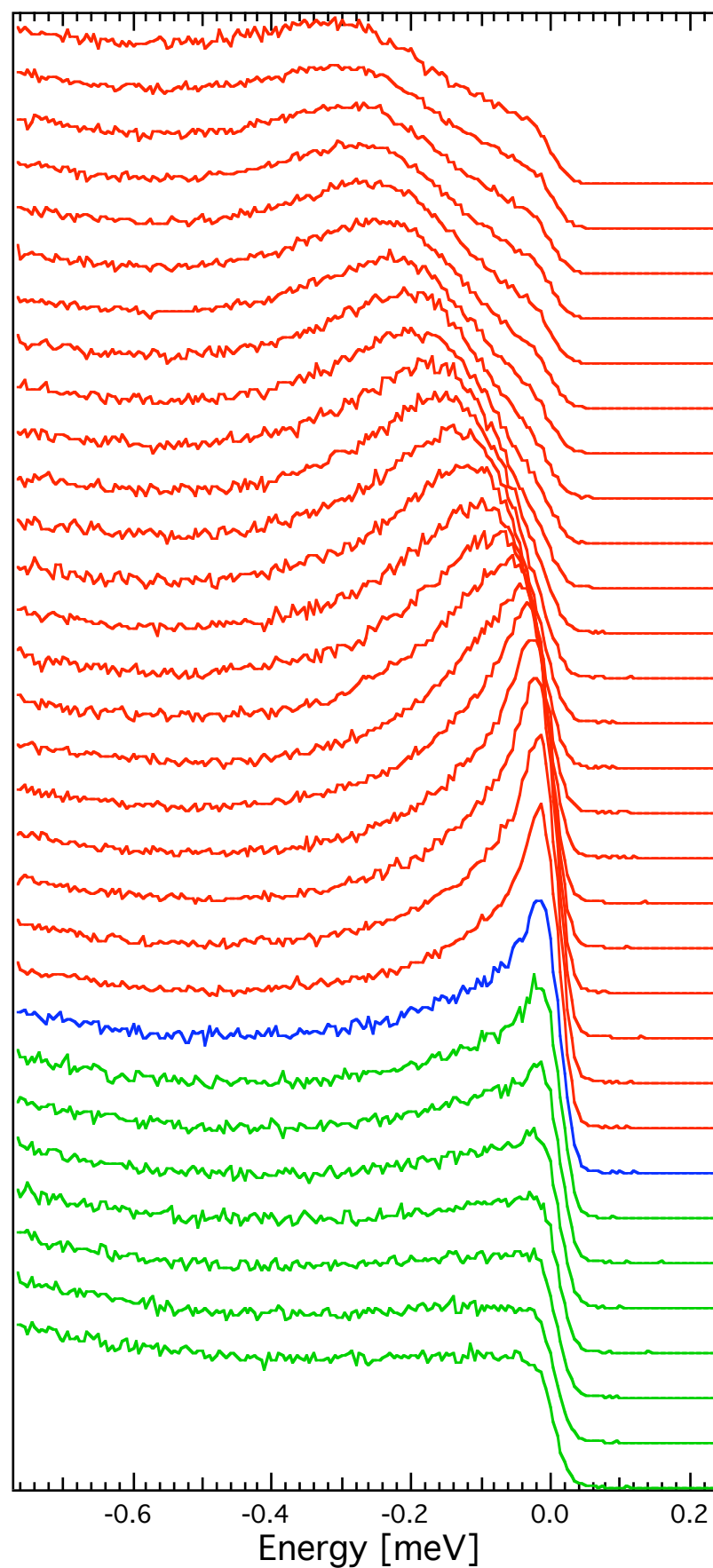
$k = \text{const}$   
Energy Distribution Curve (EDC)



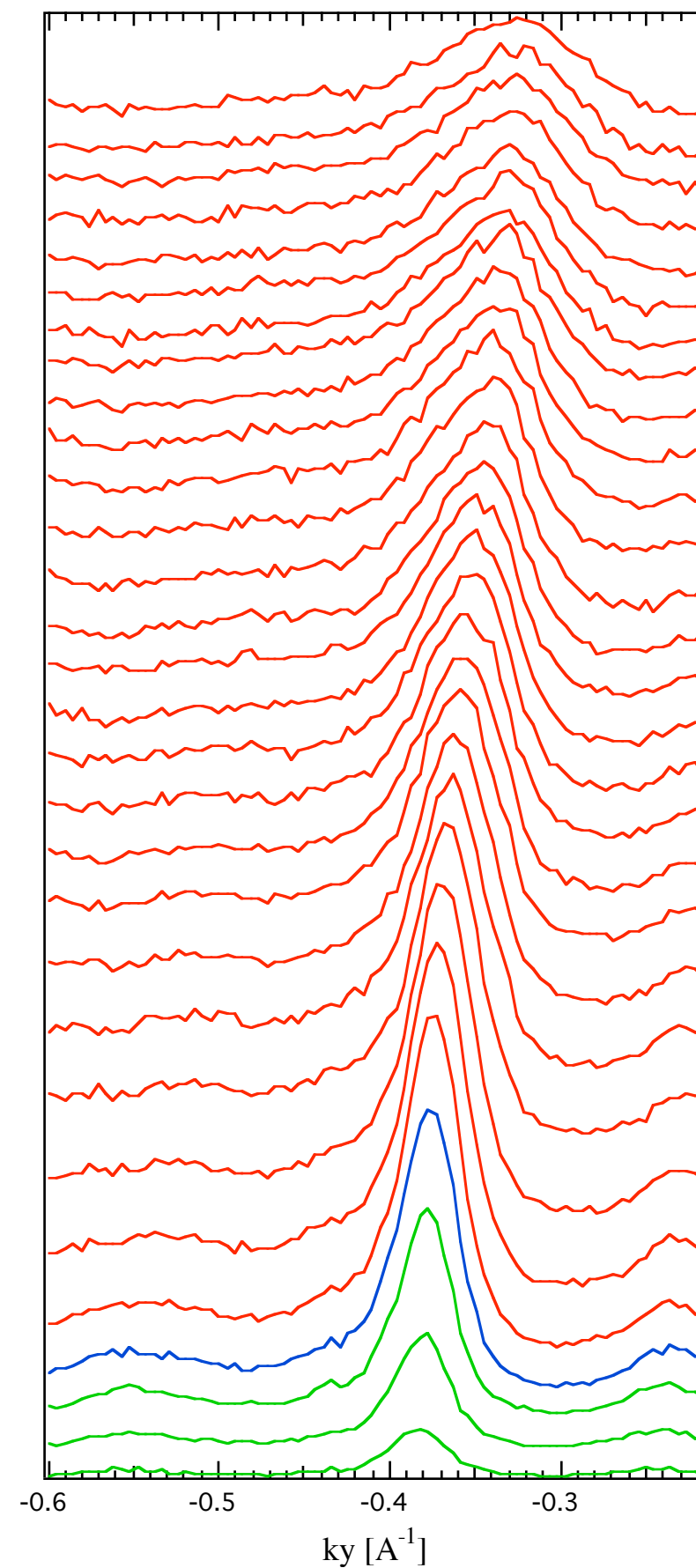
# Intensity plot



## EDC

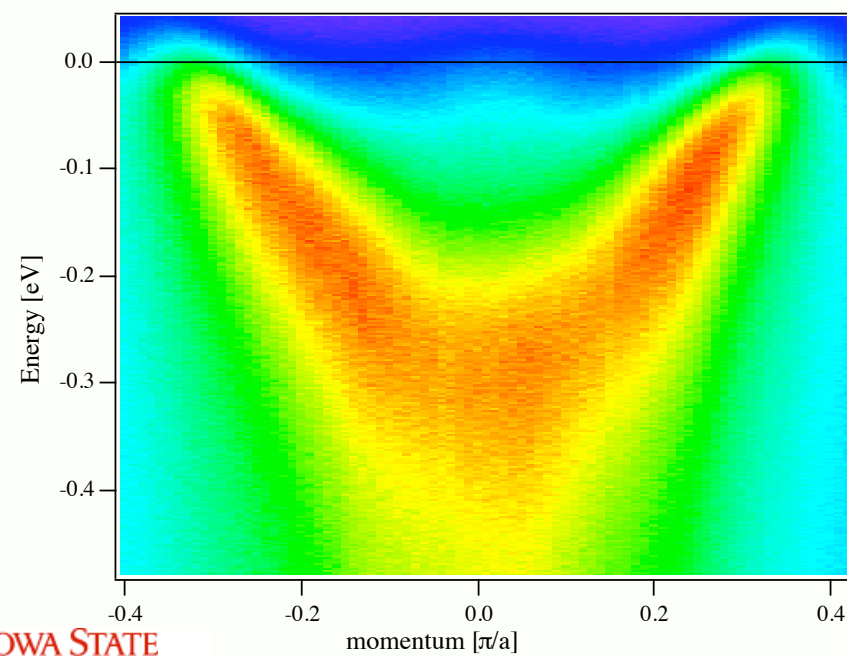
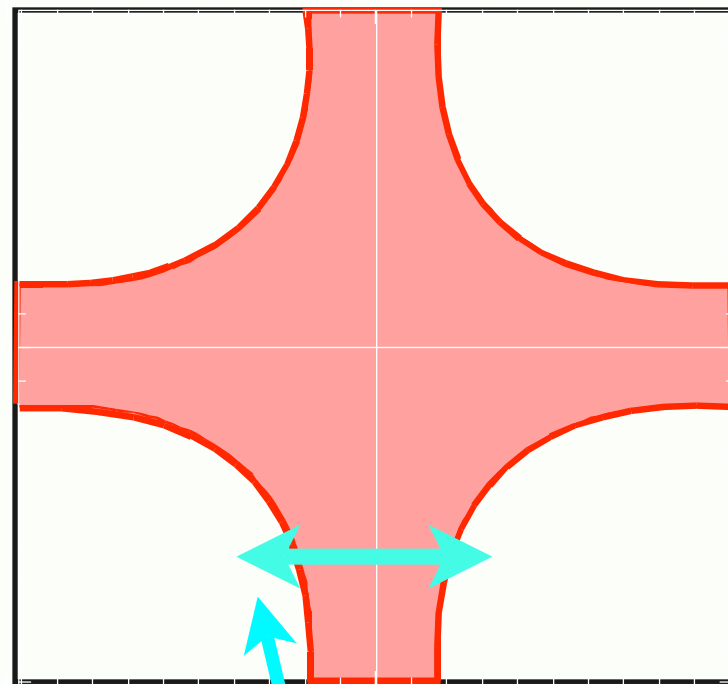


## MDC

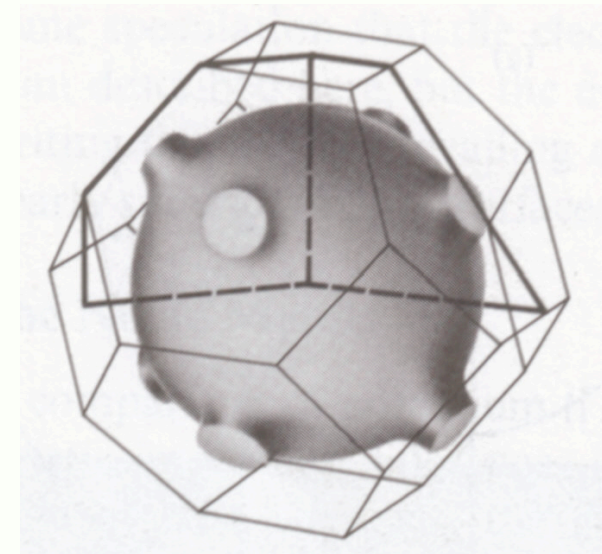




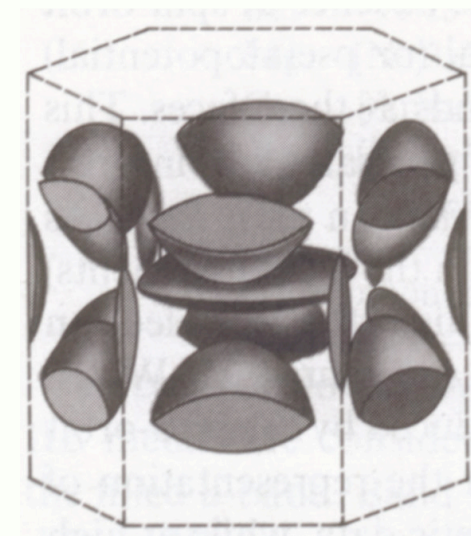
# 2D



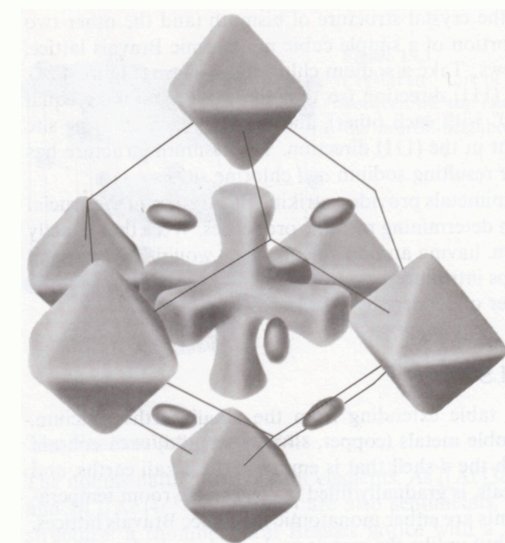
# 3D



Cu



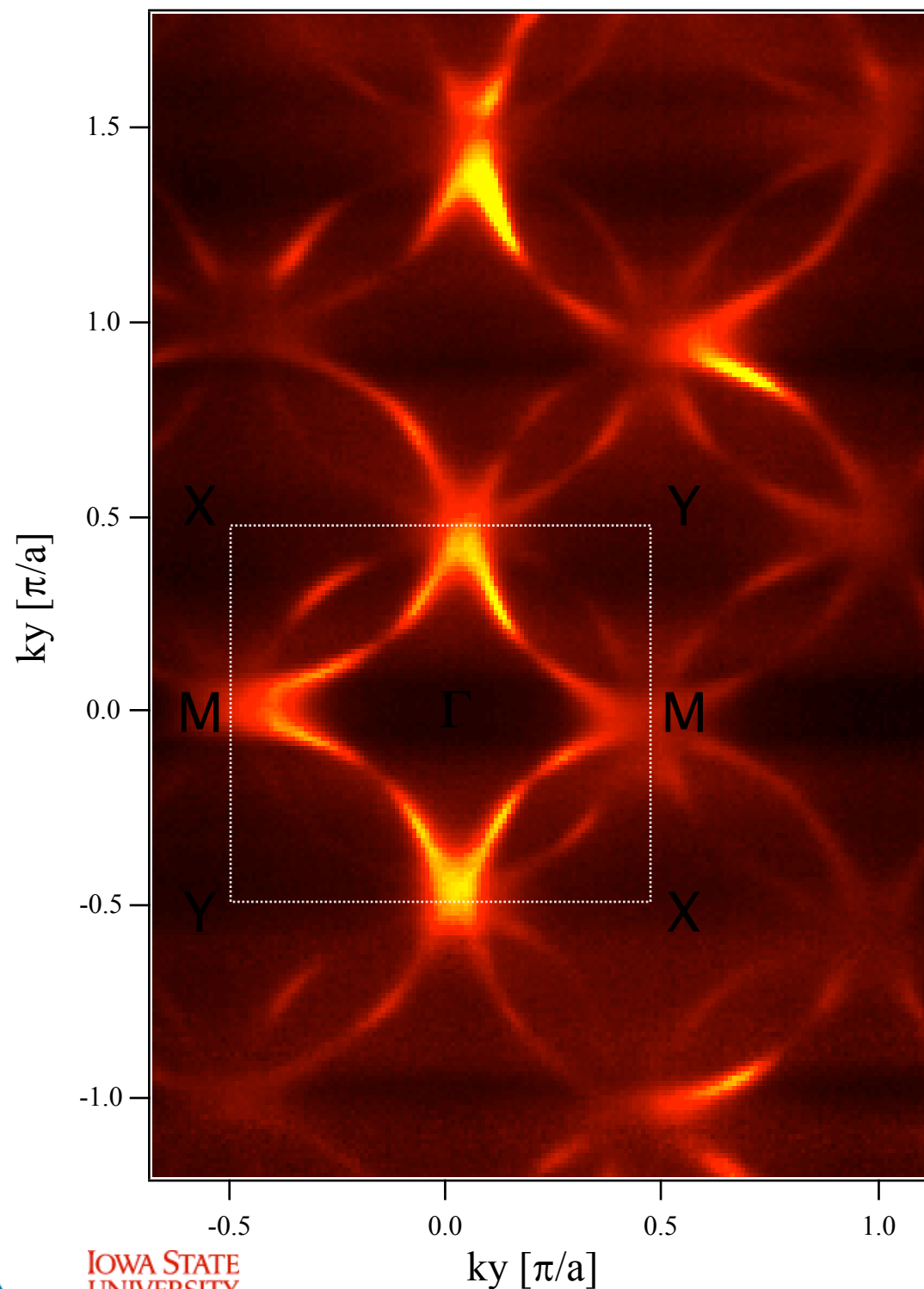
Be



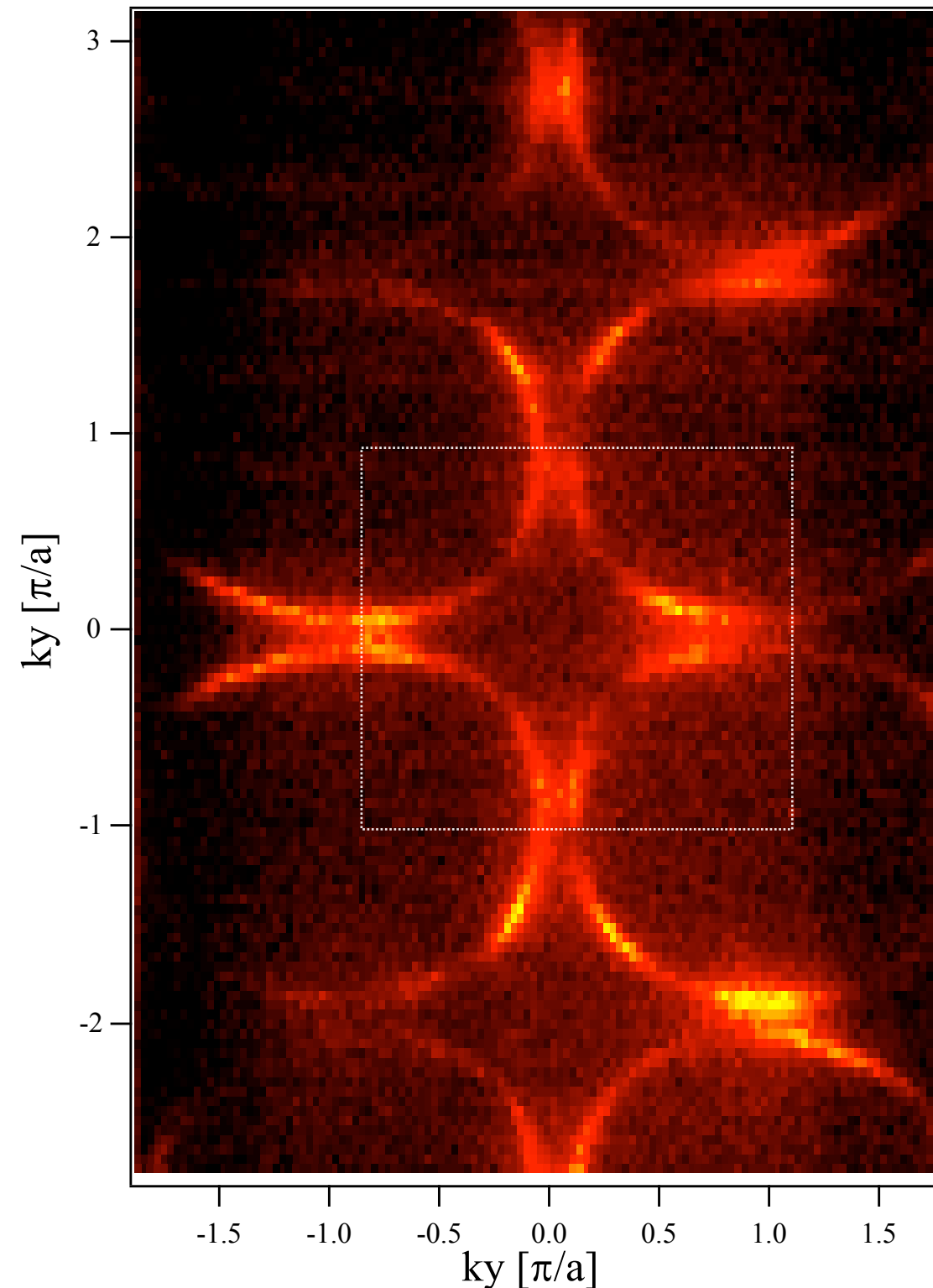
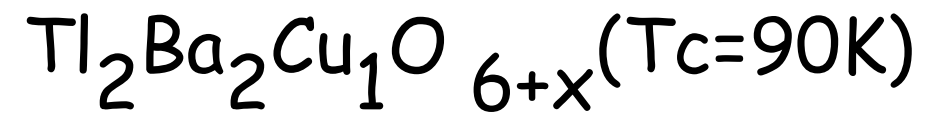
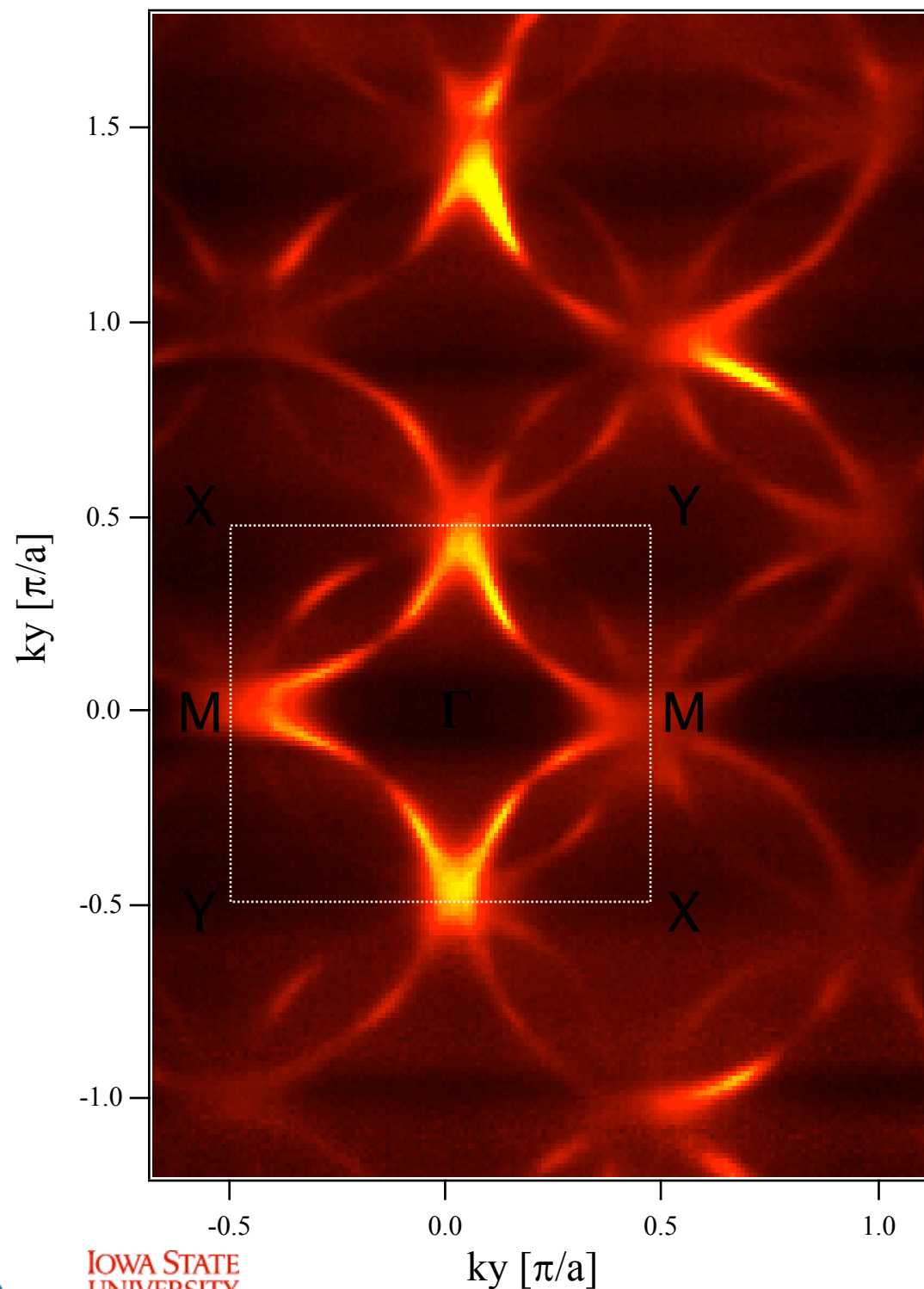
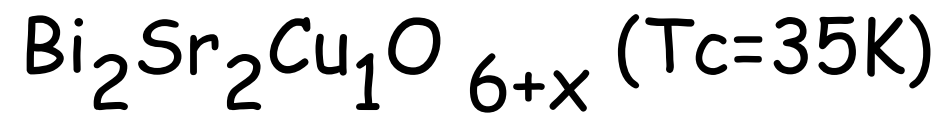
W

# Fermi surface of high temperature superconductor

$\text{Bi}_2\text{Sr}_2\text{Cu}_1\text{O}_{6+x}$  ( $T_c=35\text{K}$ )



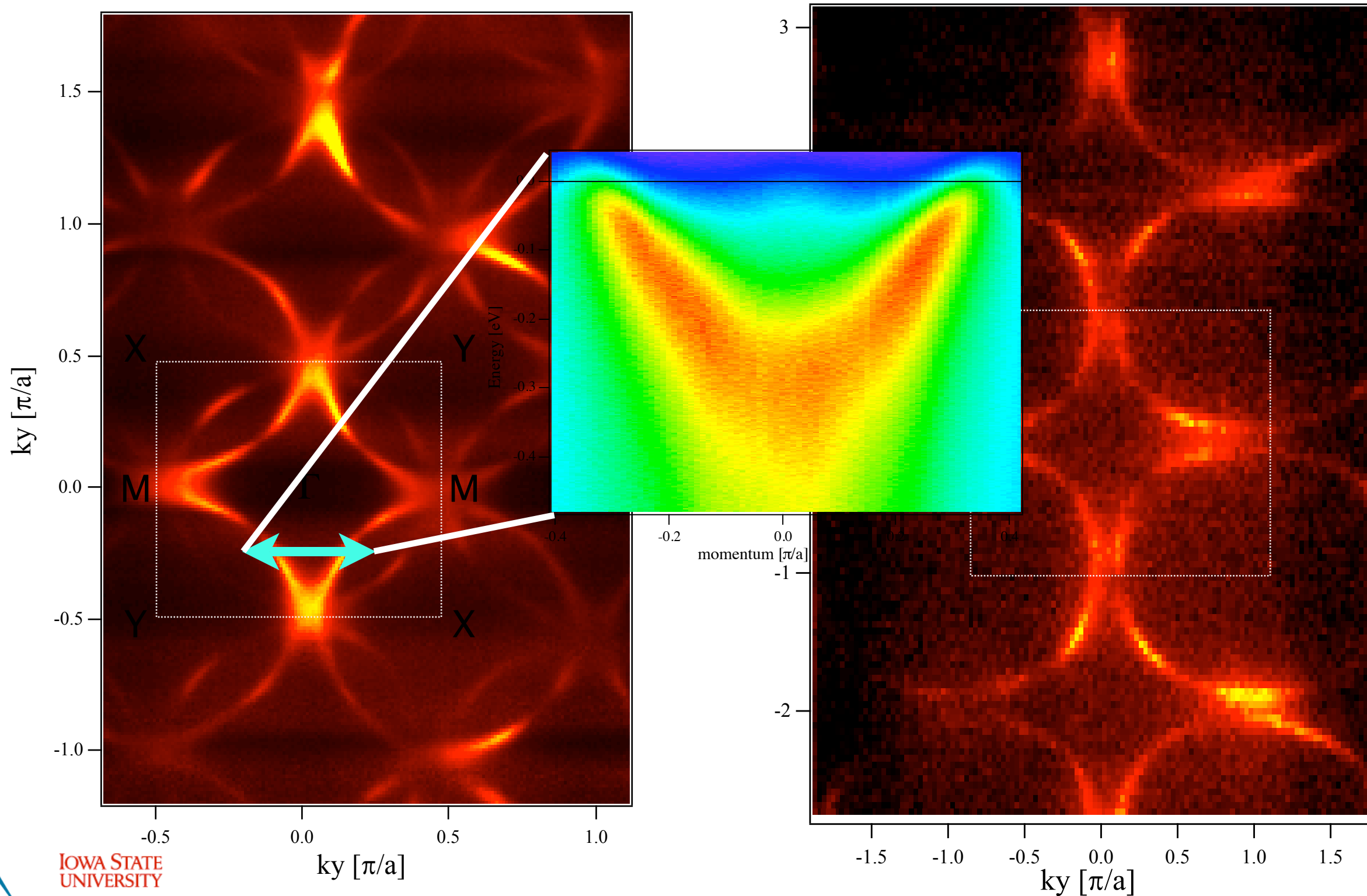
# Fermi surface of high temperature superconductor



# Fermi surface of high temperature superconductor

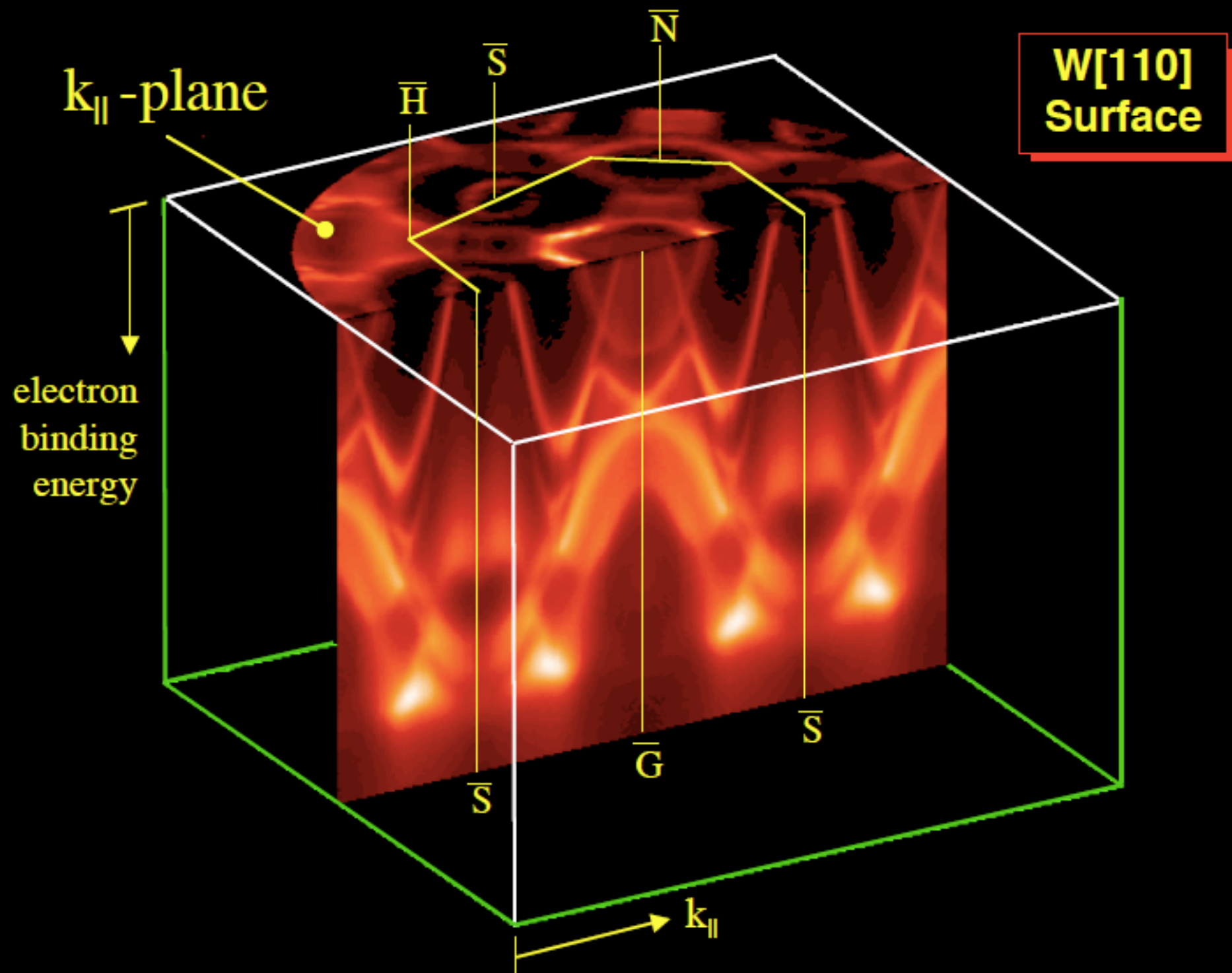
$\text{Bi}_2\text{Sr}_2\text{Cu}_1\text{O}_{6+x}$  ( $T_c=35\text{K}$ )

$\text{Tl}_2\text{Ba}_2\text{Cu}_1\text{O}_{6+x}$  ( $T_c=90\text{K}$ )





# Band Mapping and Fermi Contours



3D case:

$$k_{\perp}^i \neq k_{\perp}^f$$

$V_0$  — *inner potential*

$$|k^i| = \frac{\sqrt{2m(E_k + V_0)}}{\hbar}$$

$$k_{||} = \frac{\sqrt{2mE_k}}{\hbar} \sin\theta$$

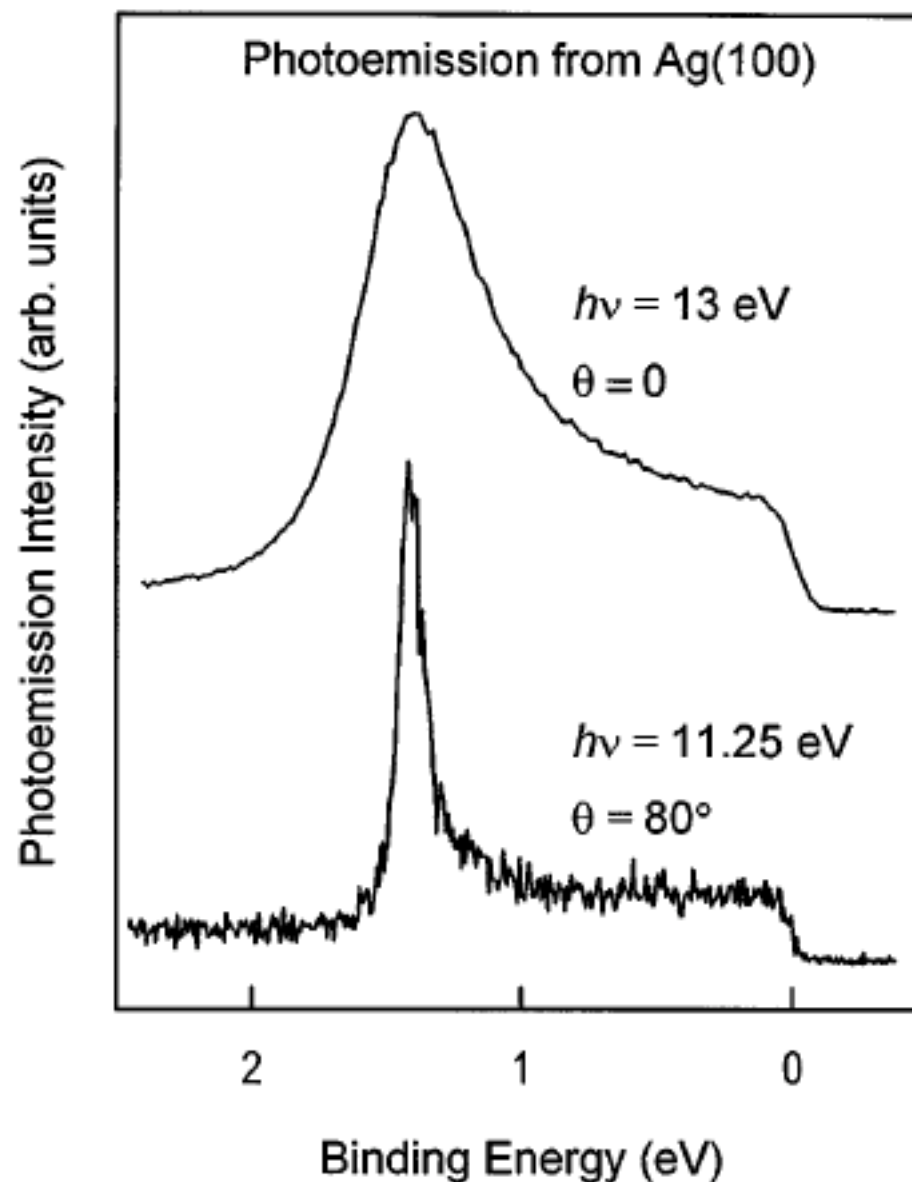
$$k_{\perp} = \frac{\sqrt{2m(E_k \cos^2\theta + V_0)}}{\hbar}$$

# Width of the ARPES peak in 3D case

$$\Gamma = \frac{\frac{\Gamma_i}{|v_{i\perp}|} + \frac{\Gamma_f}{|v_{f\perp}|}}{\left| \frac{1}{v_{i\perp}} \left( 1 - \frac{mv_{i\parallel} \sin^2 \theta}{\hbar k_{\parallel}} \right) - \frac{1}{v_{f\perp}} \left( 1 - \frac{mv_{f\parallel} \sin^2 \theta}{\hbar k_{\parallel}} \right) \right|}$$

# Width of the ARPES peak in 3D case

$$\Gamma = \frac{\frac{\Gamma_i}{|v_{i\perp}|} + \frac{\Gamma_f}{|v_{f\perp}|}}{\left| \frac{1}{v_{i\perp}} \left( 1 - \frac{mv_{i\parallel} \sin^2 \theta}{\hbar k_{\parallel}} \right) - \frac{1}{v_{f\perp}} \left( 1 - \frac{mv_{f\parallel} \sin^2 \theta}{\hbar k_{\parallel}} \right) \right|}$$

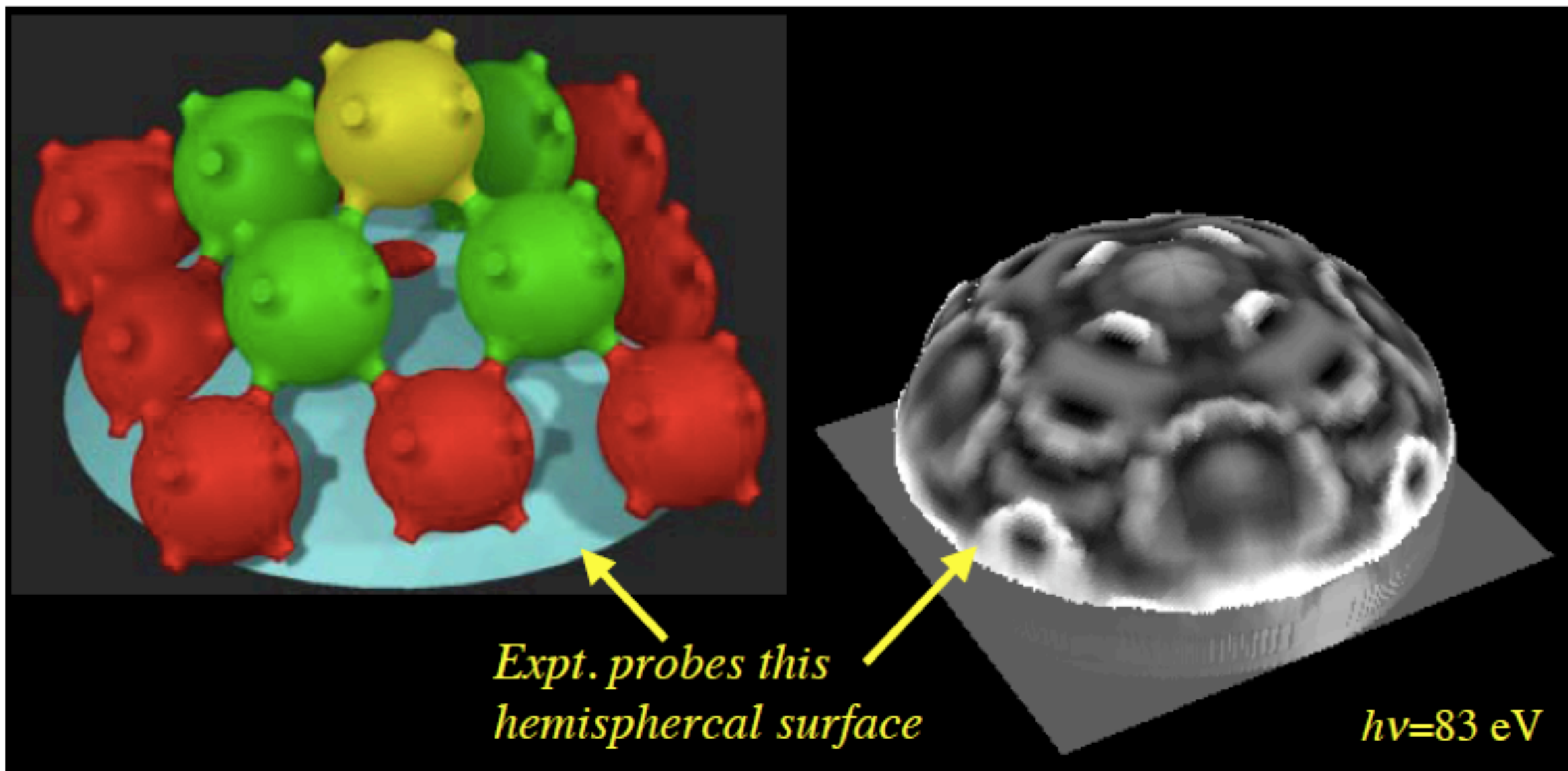


E. D. Hansen et al,  
PRL 80, 1766 (1998)

# Example Cu:

model

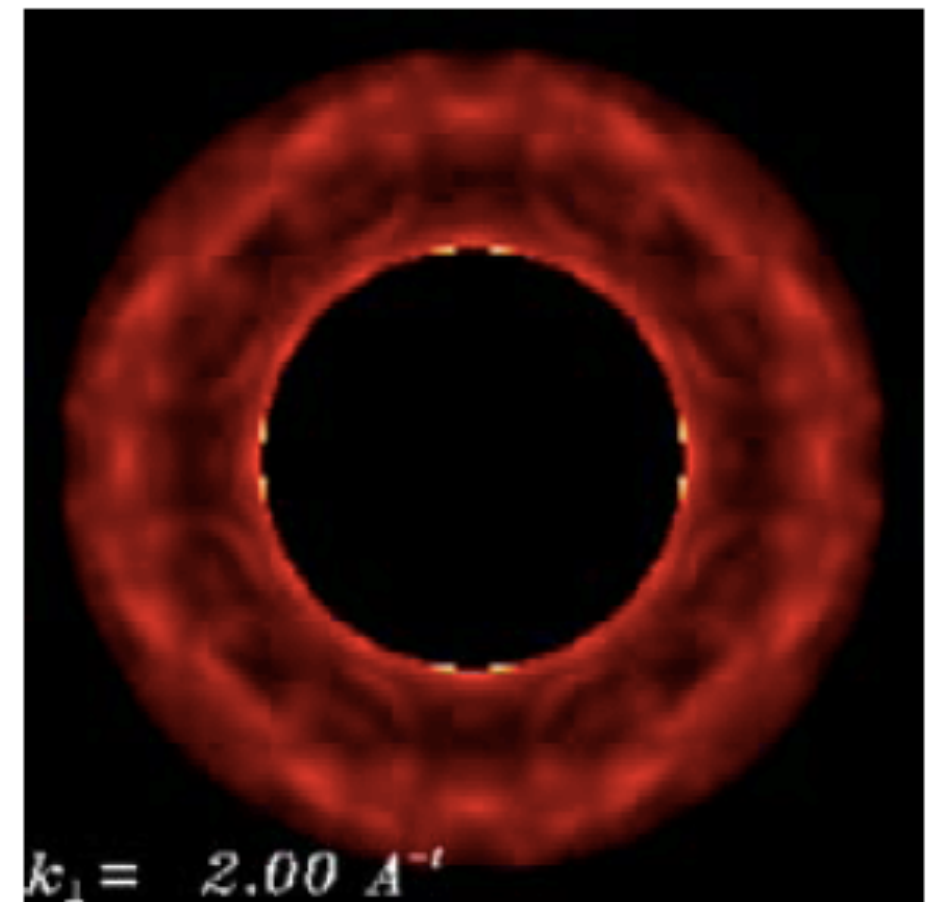
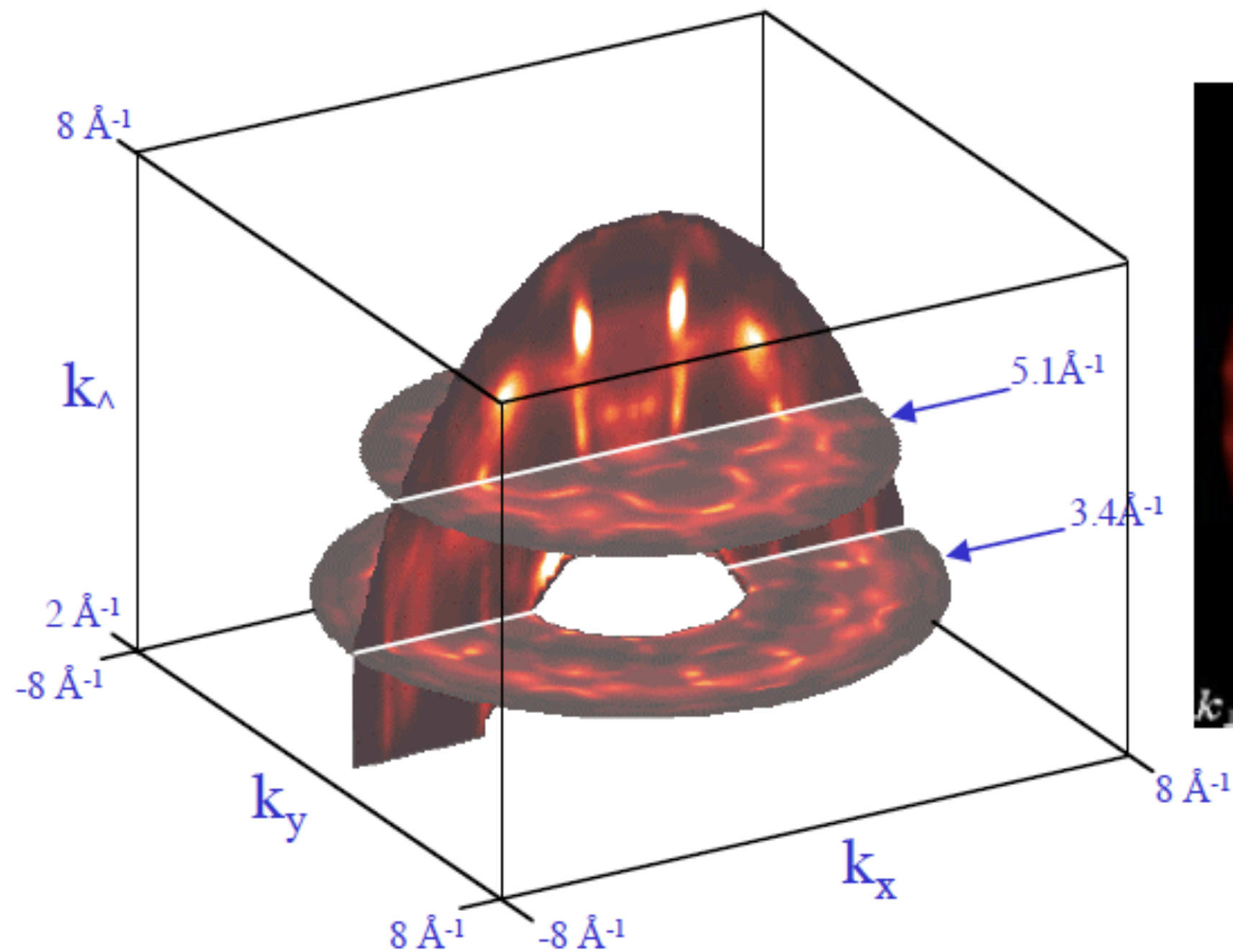
data



E. Rotenberg et al.



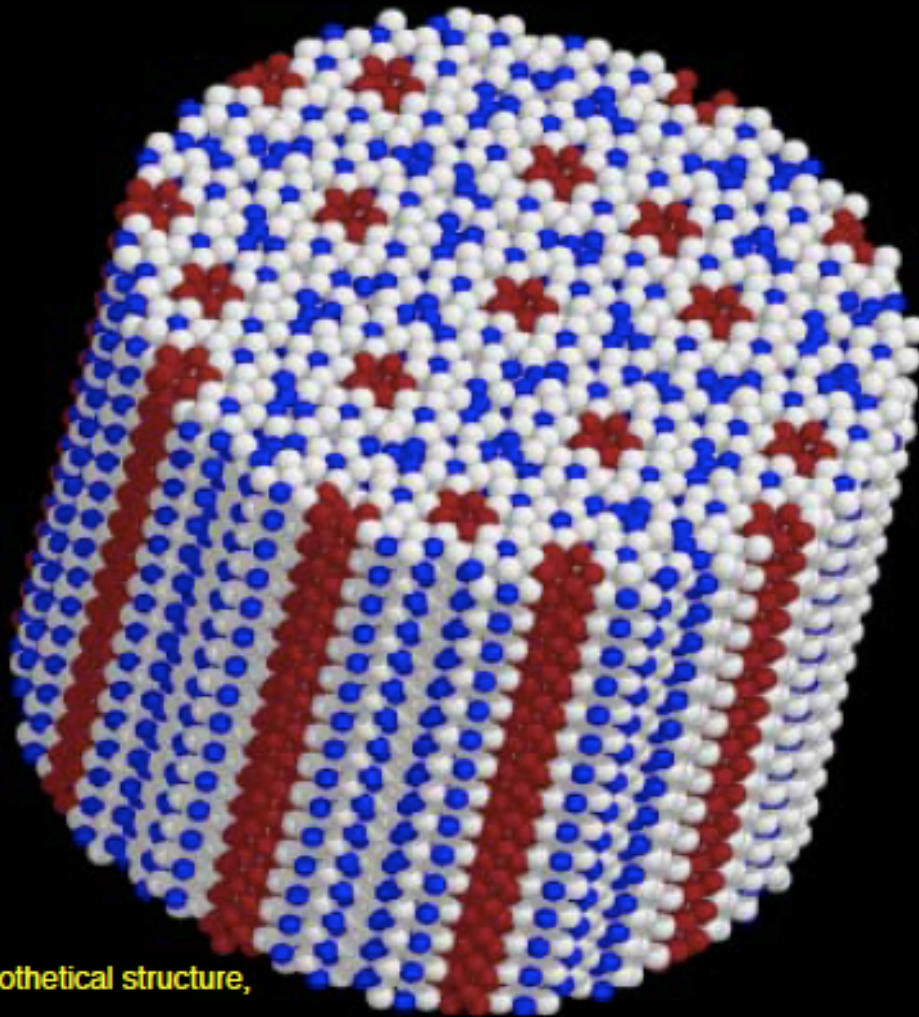
# Example Cu:



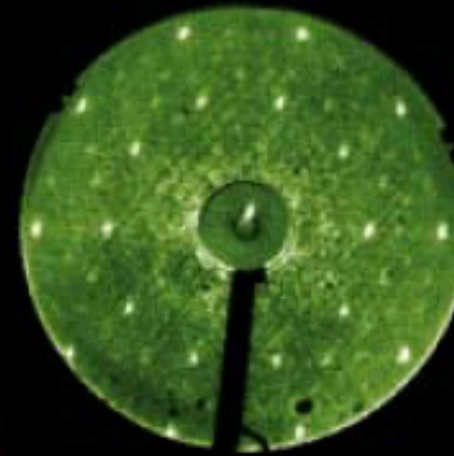
# Quasicrystals:

## Non-periodic materials?

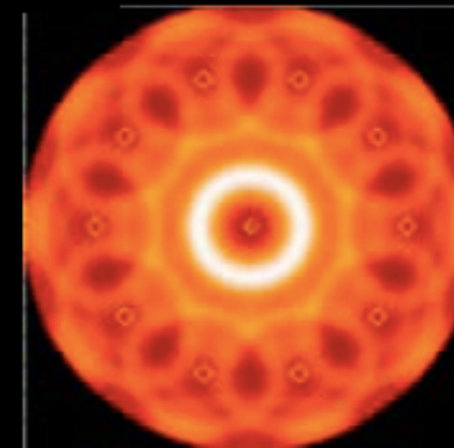
**Perfect long-range order  
without periodicity!**



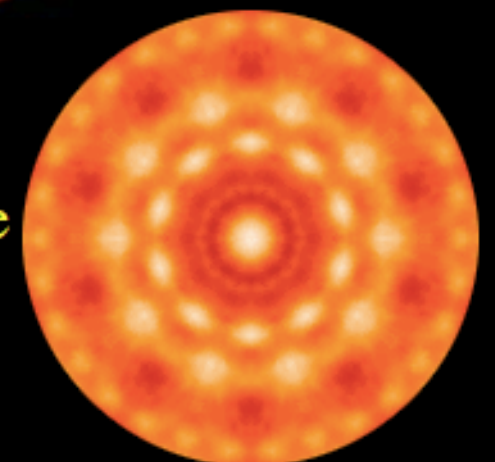
Hypothetical structure,  
after Yamamoto et al



Surface Diffraction



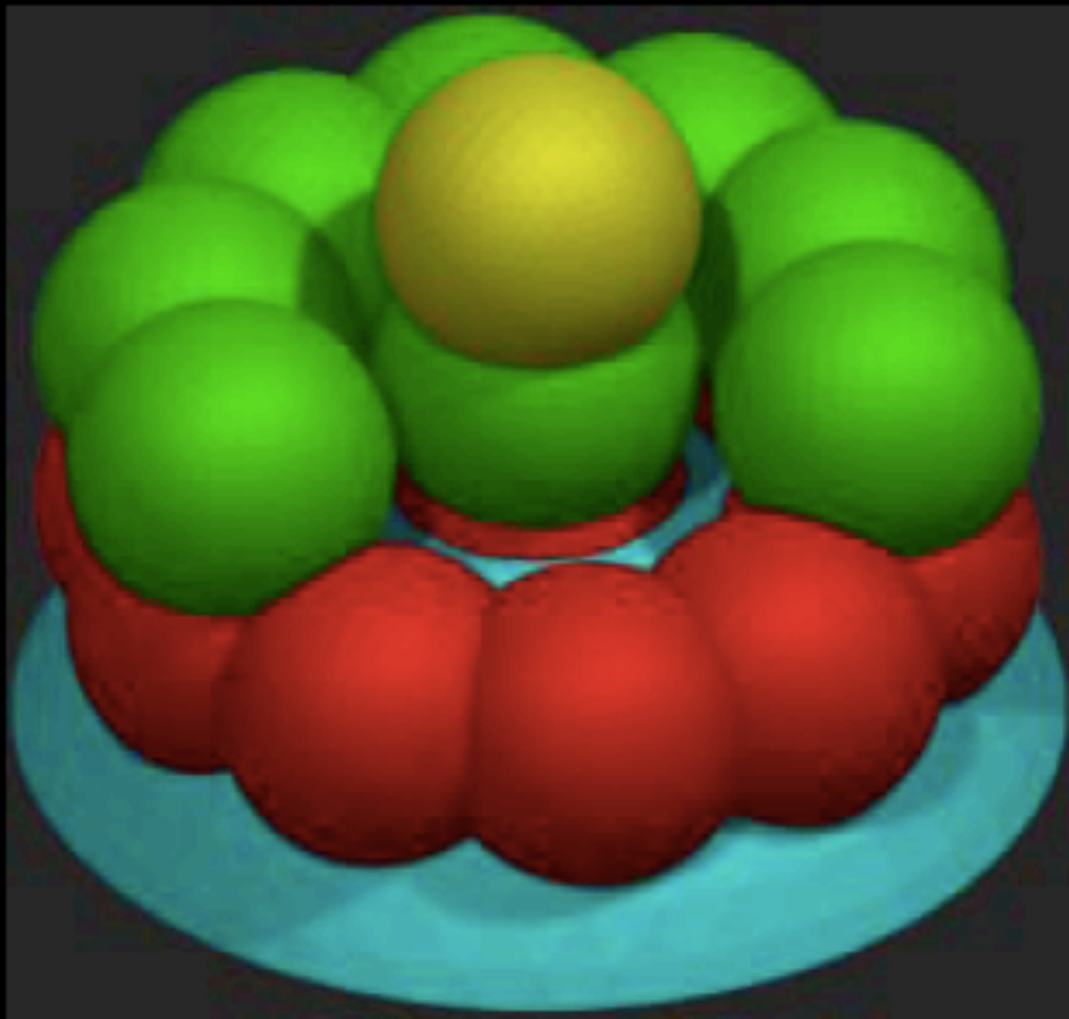
Free-Electron  
(s-p bands)



Fermi Surface  
(d-bands)

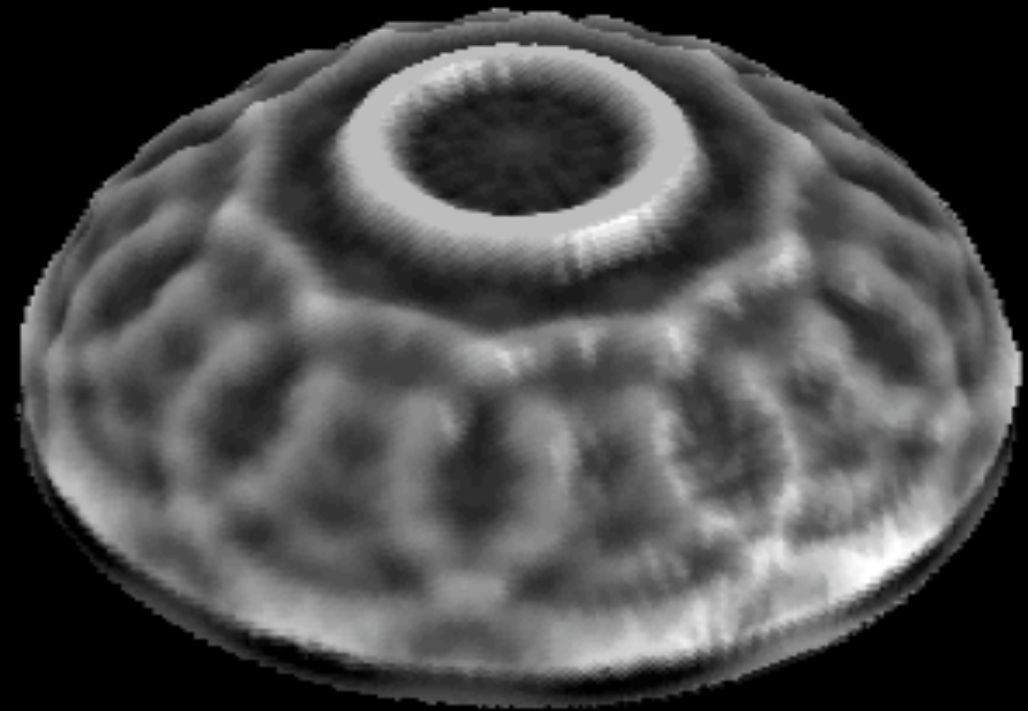
E. Rotenberg, W. Theis, P. Gille, K. Horn, *Nature* **406**, 602 (2000).

# Quasicrystals:



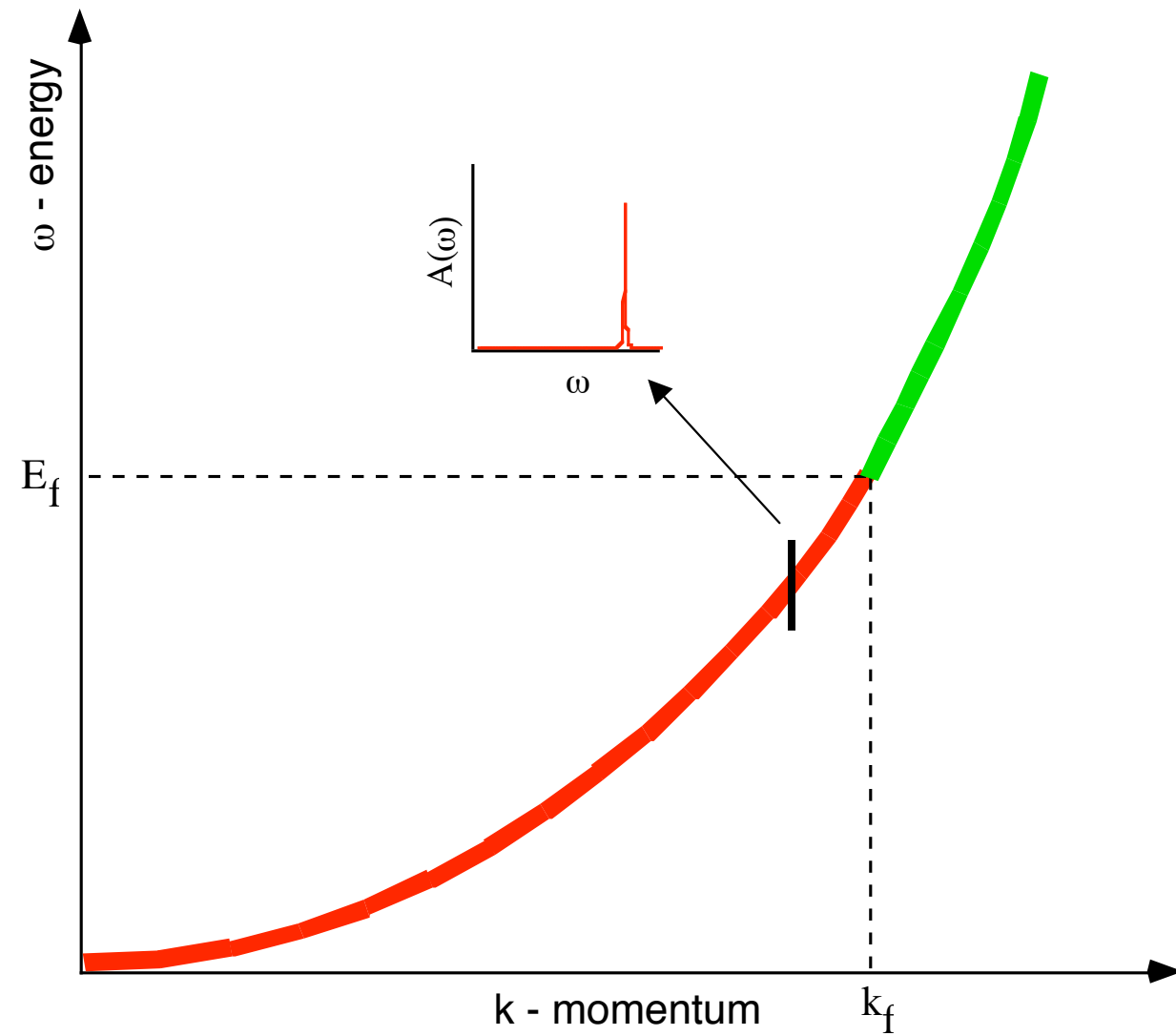
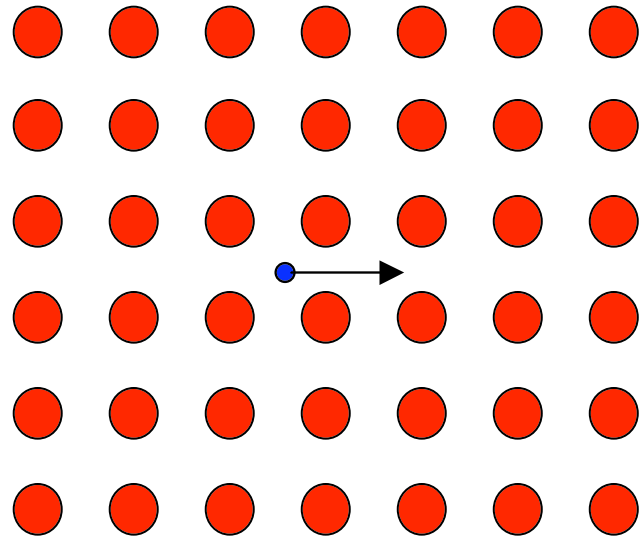
model

data



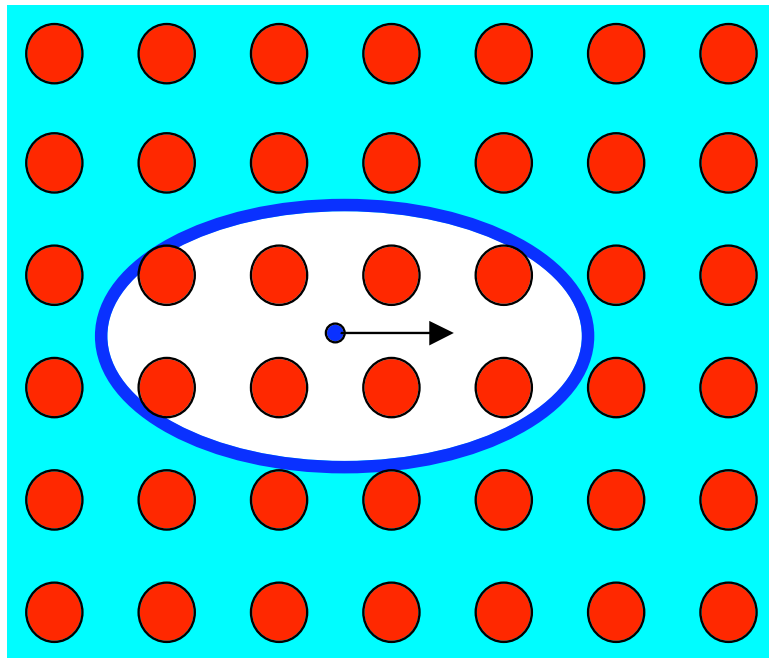
E. Rotenberg et al.

# non-interacting electrons - free electron model





# weakly interacting electrons - Fermi liquid model

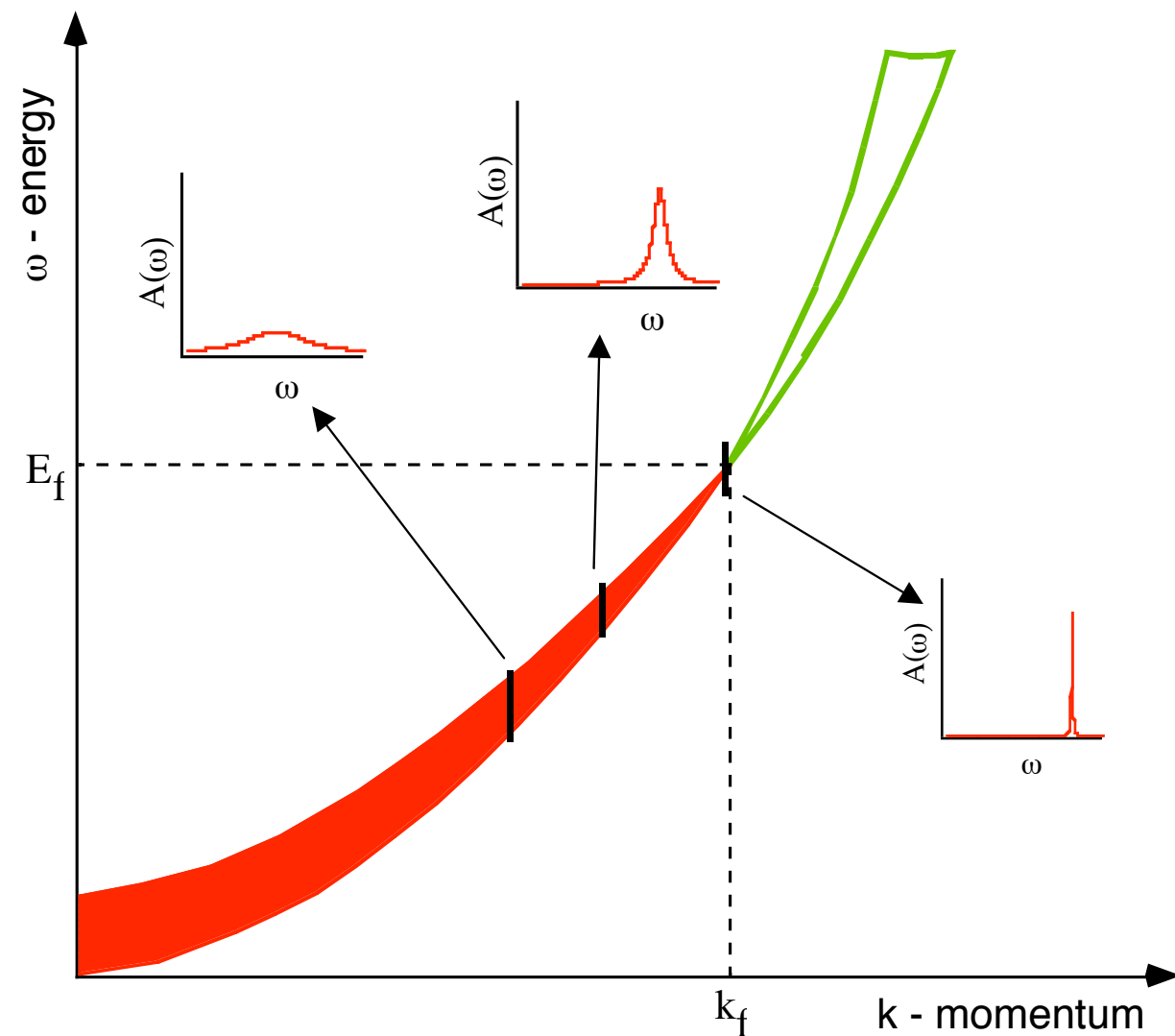


Quasiparticle="renormalized electron"

$m^*, \tau$

$\Sigma$  - self energy

$$\Sigma(k, \omega) = \alpha\omega + i(\beta\omega^2 + \gamma T^2)$$





# What does ARPES measure:

## ARPES intensity

$$I = \langle \psi_i | \mathbf{A} \cdot \mathbf{p} | \psi_f \rangle^2 A(k, \omega) f(\omega)$$

symmetry of  $\psi$

electronic structure  
+  
interactions

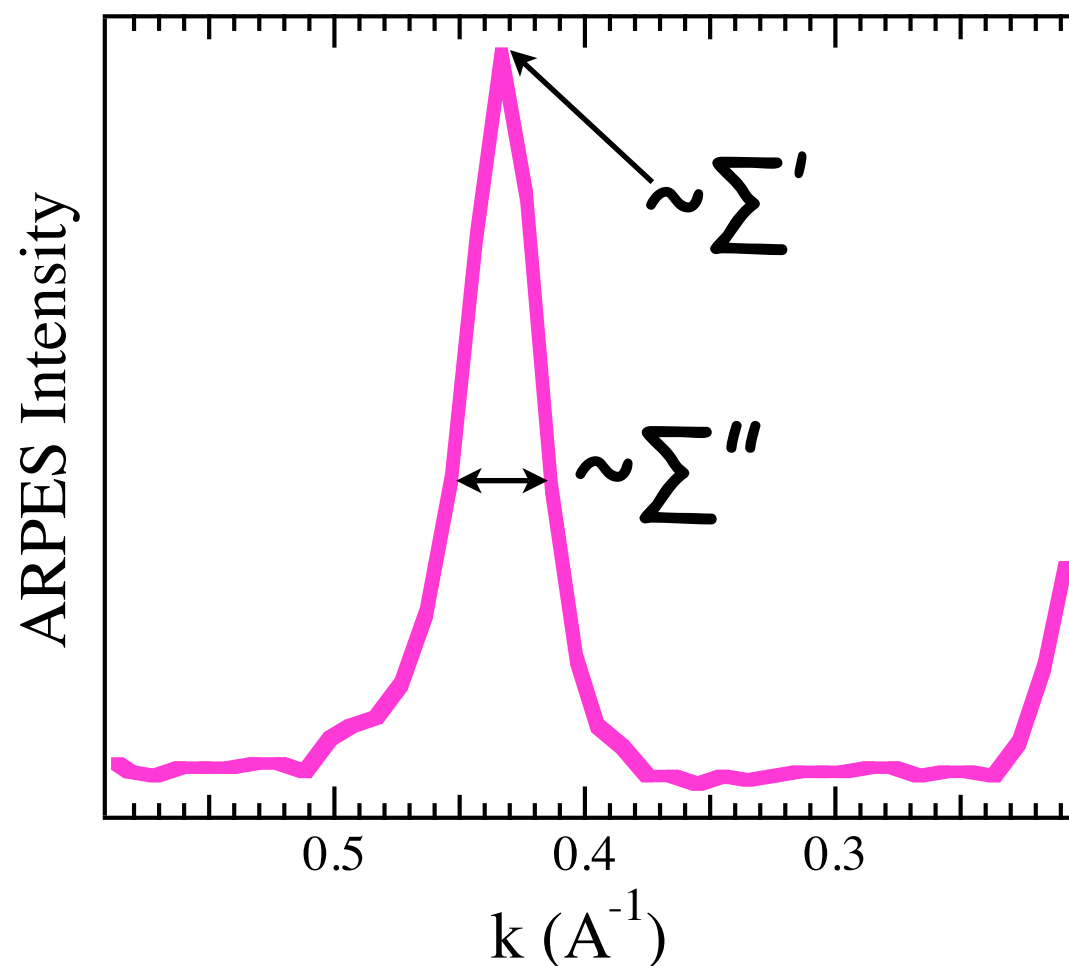
## Spectral function:

$$A(k, \omega) = \text{Im}(G(k, \omega)) = \frac{\Sigma''(k, \omega)}{(\omega - \epsilon(k) - \Sigma'(k, \omega))^2 + (\Sigma''(k, \omega))^2}$$

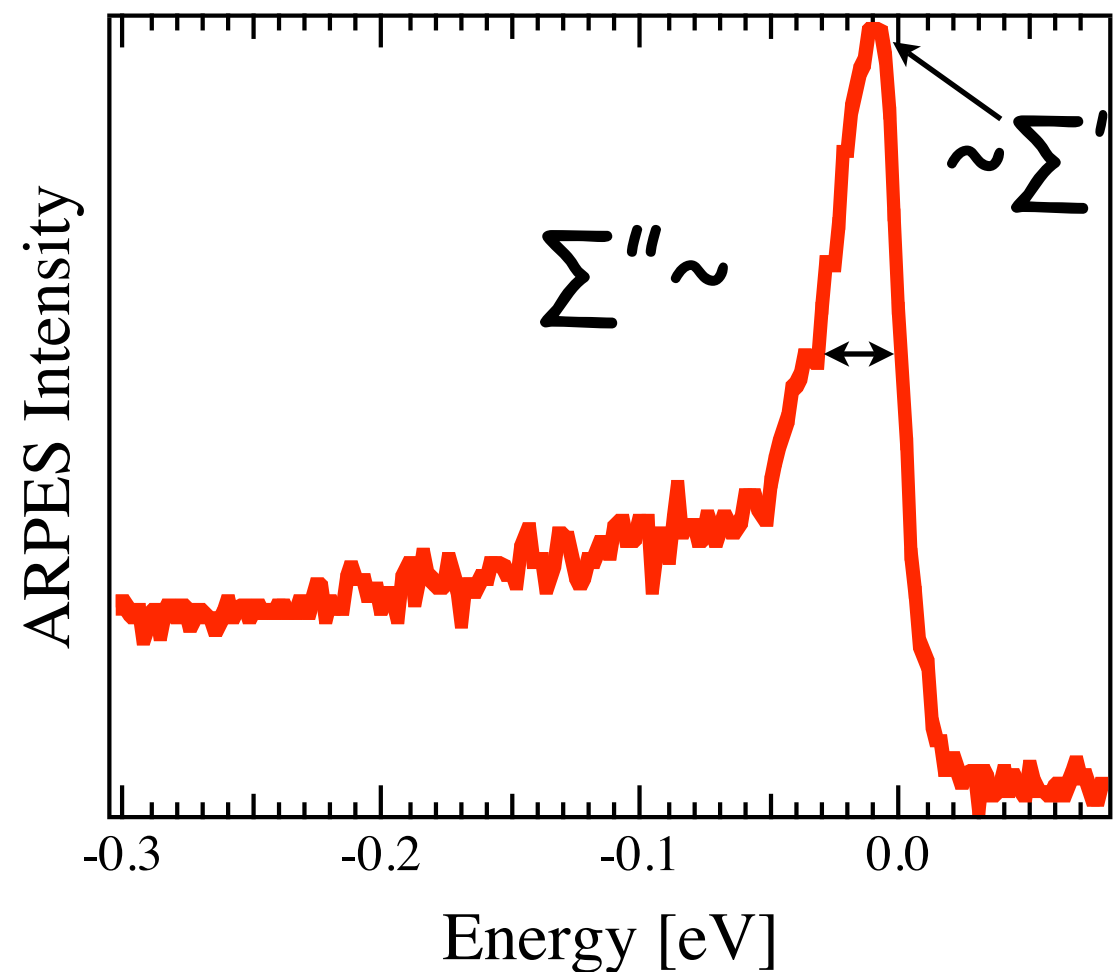
$$A(k, \omega) = \text{Im}(G(k, \omega)) = \frac{\Sigma''(k, \omega)}{(\omega - \epsilon(k) - \Sigma'(k, \omega))^2 + (\Sigma''(k, \omega))^2}$$

Self energy ( $\Rightarrow$  scattering rate)

E=const  
Momentum Distribution Curve  
(MDC)



k=const  
Energy Distribution Curve  
(EDC)



$$A(k, \omega) = \text{Im}(G(k, \omega)) = \frac{\Sigma''(k, \omega)}{(\omega - \epsilon(k) - \Sigma'(k, \omega))^2 + (\Sigma''(k, \omega))^2}$$

